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Determination of optical properties of percolated nanostructures using an optical resonator system

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In this work, methods are introduced to the determination of optical properties of thin silver films and nanostructures. We present an optical resonant system consisting of a mirror, a transparent layer and a thin silver film. The layer sequences and the nanostructure of the thin films are investigated by optical methods consist of reflectance measurements. The structures are analyzed by atomic force microscopy and scanning electron microscopy. The optical properties are determined by modeling the reflectance data. We have found that the growth mechanisms of the silver layer are correlated to its optical properties. It also found that temperature treatments produce isolated particles with a narrow plasmon resonance. © 2012 American Institute of Physics. [<http://dx.doi.org/10.1063/1.4768202>]

I. INTRODUCTION

Optical properties of thin metal films may provide an important clue about their internal properties;^{1–4} yet they are difficult to analyze and the determination of their properties remains relevant. In this paper, we study nanostructured thin layers of silver deposited on top of an optically resonant layer system (ORL).⁵ By independently measuring the morphology of the layer, we investigate its effect on the optical spectra. In particular, under the condition that certain geometrical patterns are formed on the surface and the percolation over metallic particles is set up, the real part of the dielectric function gets a negative value. As a consequence, this film can serve as a building block for the development of new metamaterial devices.⁶

The ORL consists of a transparent layer (SiO₂ or ZnO), of approximately 100 nm thickness, which roughly corresponds to one fourth of the wavelength, coated on a metallic Ag mirror.⁷ On top of the transparent layer, the silver layers to be studied are deposited; their thickness varied from 1 to 90 nm (see Fig. 1). In this optical system, the incident light passes through the thin layer and the transparent layer to be reflected by the mirror. Because of the $\lambda/4$ condition, a constructive interference of the field strength occurs in the thin top layer. This interference increases the absorption of the thin metallic top layer.

The topography of the metallic top layer could be influenced by a post-annealing treatment.^{8,9}

The surfaces are examined by atomic force microscopy (AFM) and scanning electron microscopy (SEM). The optical properties were investigated by reflectance measurements. The optical properties of metallic bulk material were already studied in the literature in detail.¹⁰ In this work, we demonstrate that thin metallic layers on the nanoscale range shows completely different reflection properties than bulk materials. Some discussions are already given.^{11–13} Three questions

seem to be interesting, (1) which is the critical layer thickness for the change to the optical properties? (2) What is the impact of the topography? (3) How the ORL influences the reflectance spectra.

The answers to the questions should be given to the following approach: (1) The structures will be integrated into an optical resonant structure; therefore small structural changes provide significant measurement signals. (2) The topography will be measured. The change in the topography will be compared to the change in the reflection. (3) The optical system will be fit by standard routines to get the optical properties.

II. MATERIAL AND METHODS

A. Sample preparation

The metallic layer, the metallic nanostructures, the SiO₂ layers, and the Ag mirror were produced by thermal evaporation in an UV chamber at a pressure of 10^{−6} mbar. The SiO₂ layers were thermal treated after depositing at 450 °C for 10 h in a furnace at a pressure of approximately 10^{−5} mbar. Tests with acetone have shown that the SiO₂ layers were chemically stable and ellipsometric measurements revealed that the layers were completely oxidized. The refractive index of well-known SiO₂, i.e., the same as native oxide on silicon wafer, was obtained by ellipsometry but not given here. The thickness of the mirrors was 300 nm. The distance between evaporation sources and sample was 500 mm for the fabrication of the SiO₂ layer. For the production of the metallic nanostructures, the metallic layers and the mirror distance was 350 mm. The support of the mirrors was a plate of standard laboratory glass or polycrystalline silicon. Mixture of different nanoparticle materials in the course of the manufacturing process was prevented by carefully cleaning the vacuum chamber prior to evaporation of a new metal. For test reasons some nanostructures layers were also made by sputtering. The nominal thicknesses were measured by quartz oscillator. The ZnO layers were made at the Research Center Jülich as described in previous publications.^{14,15}

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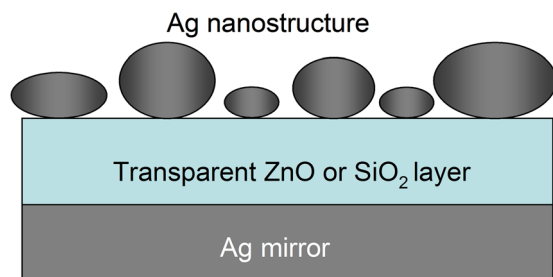


FIG. 1. Schematic presentation of the layer system.

B. Optical and structural measurements

The reflectance measurements were carried out close to backscattering geometry on a reflectometer at incidence angle of 8° in the 190 nm–1100 nm wavelength range. The scattered light was also measured in an integral sphere (Ulbricht sphere) to control our measurements and to analyze the diffuse light.¹⁶

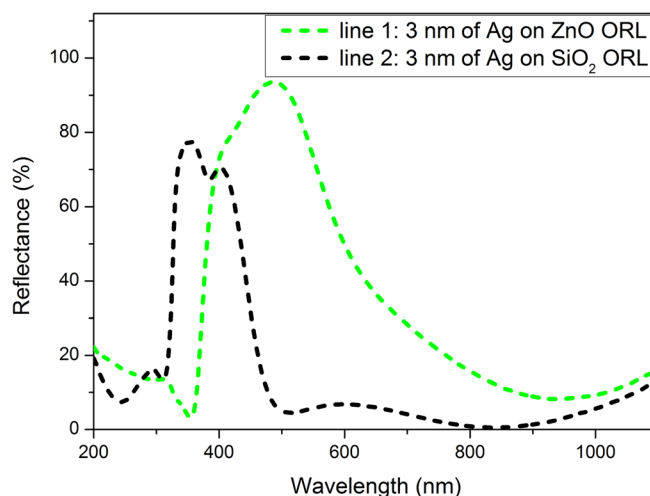
The separated nanoparticles and the metallic layers were analyzed by AFM (nanoscope Nano R² Pacific nanotechnology) and by a scanning electron microscope. Since SiO₂ is an insulator, SEM images are only recorded from Ag deposited on ZnO ORL or on a c-Si substrate with a naturally thin SiO₂ layer.

III. RESULTS

A. Reflectance measurements on thin metal layers

The influence of the nominal layer thickness on the optical properties can be recognized clearly in the reflection measurement as can be seen in Figs. 2(a) and 2(b). Fig. 2(a) shows the results from Ag layer of 17 nm, 33 nm, 50 nm, and 90 nm nominal thicknesses applied on the ORL, consisted of a silver mirror and a transparent layer of 100 nm ZnO. With a 90 nm nominal silver thickness, the influence of the ORL is barely visible. Fig. 2(b) shows the results from Ag layer of 1 nm, 2 nm, 3 nm, 4 nm, 5 nm, and 6 nm nominal thicknesses applied on the ORL.

For wavelengths shorter than 400 nm, the reflection decreases dramatically for all samples because of internal properties of ZnO and the interband threshold of silver. The thinnest layer, of 1 nm Ag, exhibits the reflectance almost indistinguishable from that of the underlying 100 nm thick ZnO without Ag; only that around 570 nm a slight dip in the

FIG. 3. Experimental reflectance spectra obtained from Ag layer of 3 nm nominal thicknesses applied on the ZnO and SiO₂ ORLs.

reflectance is visible. On the contrary, Figs. 2(a) and 2(b) show that thicker Ag layers exhibit large change. For a 4 nm layer, the reflectance drops to almost zero at 800 nm wavelengths. Obviously, a certain change in behavior happens between 4 nm (Fig. 2(b)) and 17 nm (Fig. 2(a)) layer nominal thickness. For a 17 nm-thick Ag layer, a pronounced minimum in reflectance occurs at around 600 nm wavelengths. This minimum becomes sharper, deeper, and shifts to shorter wavelength for 33 nm-thick Ag layer. It persists also for thicker layers but it becomes ever less deep as the nominal layer thickness increases, until it ultimately disappears for 90 nm. This minimum provides from the destructive interference between light waves reflected by the upper and lower ORL boundaries. In other words, the ORL is narrow notch filter structure which filters a narrow spectral range.

B. Comparison between reflectance measurements on SiO₂ and ZnO ORL

Fig. 3 shows comparison between the experimental reflectance spectra of 3 nm Ag layers deposited on a ZnO ORL and on a SiO₂ ORL. Both spectra have similar features such as a minimum and a maximum in reflectance in the 800–1000 nm and 350–500 nm wavelength ranges, respectively, providing from the destructive and the constructive interference between the incident and the reflected light on the ORL. However, due to the lower refractive index of SiO₂ than

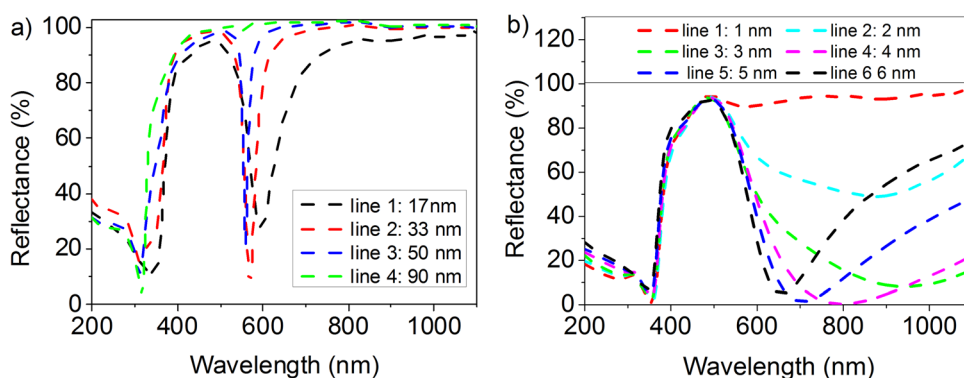


FIG. 2. Experimental reflectance spectra obtained from Ag layer of (a) 17 nm, 33 nm, 50 nm, and 90 nm and (b) 1 nm, 2 nm, 3 nm, 4 nm, 5 nm, and 6 nm nominal thicknesses applied on the ZnO ORL.

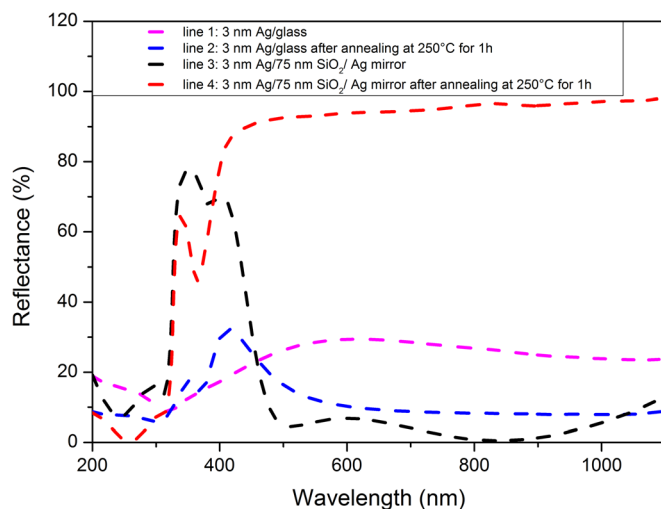


FIG. 4. Experimental reflectance spectra of silver layers on SiO_2 substrates (lines 1 and 2) or a SiO_2 ORL (lines 3 and 4) before (lines 1 and 3) and after (lines 2 and 4) annealing.

ZnO , the minimum and the maximum in reflectance of the Ag layer on the SiO_2 ORL are both blueshifted by nearly 120 nm.

A slight dip in reflectance at 380 nm, attributed to the plasmon resonance of silver nanoparticles is also observed for the SiO_2 ORL. This feature is not present on the ZnO ORL reflectance spectra probably due to a substrate dependence of the silver island shape and nucleation rate.

C. Reflectance measurements before and after annealing

We turn now to the discussion of annealing effects on the optical properties of metal layers. Two systems have been taken for such an analysis: (i) a 3 nm Ag layer on a laboratory glass and (ii) the same Ag layer, but deposited on 75 nm-thick SiO_2 layer and a thick Ag mirror behind it (all this mounted on a laboratory glass as well). The reflectance spectra of both systems before and after annealing at 250 °C during 1 h are shown in Fig. 4. As shown in Fig. 4, the reflectance dispersion curves of the second systems present higher variations. The ORL structure improves the sensitivity to both, the morphology and the optical properties of the Ag film. The system after annealing (line 4) shows a stronger dip in reflectance at 380 nm than unannealed system. It has the same reflectivity spectrum in the range from 400 to 1100 nm as the same

system without deposited upper layer (spectrum not shown), whereas for the freshly deposited Ag layer of system, the reflectivity is very different (line 3). Please note that the topography of the nanostructures is changed by heating (see Sec. III D) and that the structures are investigated by a resonant system, which works very well for line 3.

It is worth to note that the SiO_2 layers are very stable and contains negligible levels of impurities;^{14,15} therefore we can exclude the diffusion of silver into the SiO_2 .^{17,18}

The reflectance decreased to zero, in all cases if we used a 3 nm evaporated silver layer on top of a transparent layer (ZnO or SiO_2) coated on Ag mirror.

D. Topographic measurements

Concerning the discussion of layer topography, it is shown in Fig. 5 the SEM images of 3 nm, 10 nm, and 20 nm-thick silver layers on ZnO ORL.

The 3 nm-thick silver layer is composed of nearly percolated silver islands with complex elongated shape and randomly orientations (Fig. 5(a)). SEM image of a 10 nm Ag layer (Fig. 5(b)) reveals that the Ag islands tend to percolate, forming a continuous film. Above a 20 nm thickness, silver completely covers the ZnO surface (Fig. 5(c)).

Figs. 6(a) and 6(b) shows the SEM images of 10 nm nominal thick silver on top of c-Si and Figs. 6(c) and 6(d) shows a 3 nm nominal thick Ag on top of ZnO , each before and after annealing.¹⁴ On the c-Si substrate exists a naturally SiO_2 layer, which has the same refractive index as the ORL SiO_2 layer (ellipsometric measurements are not shown). Therefore, we can expect similar nanostructures on c-Si as on laboratory glass of SiO_2 or on evaporated SiO_2 layers.

Considering a 10 nm thick Ag layer, silver islands on SiO_2 (Fig. 5(b)) are smaller and less percolated than on ZnO ORL (Fig. 6(a)). This is in agreement with the slight dip in reflectance observed at 380 nm in Fig. 3 (line 2) attributed to the plasmon resonance of some isolated silver islands. In other words, the layer on the SiO_2 ORL consists in an intermediate system between isolated and percolated silver islands. The shape of silver islands depends on the ability of adatoms to diffuse on the substrate surface suggesting a substrate nucleation rate dependence.

Comparing to the SEM images of unannealed samples (Figs. 6(a) and 6(c)), silver islands become less elongated and their average size increases after the annealing step

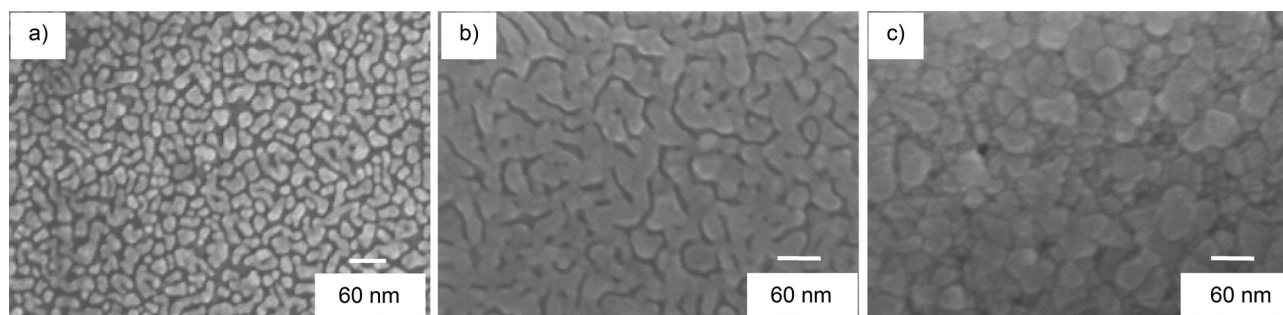


FIG. 5. (a) SEM images of a 3 nm, (b) 10 nm, and (c) 20 nm-thick Ag layer on a ZnO ORL.

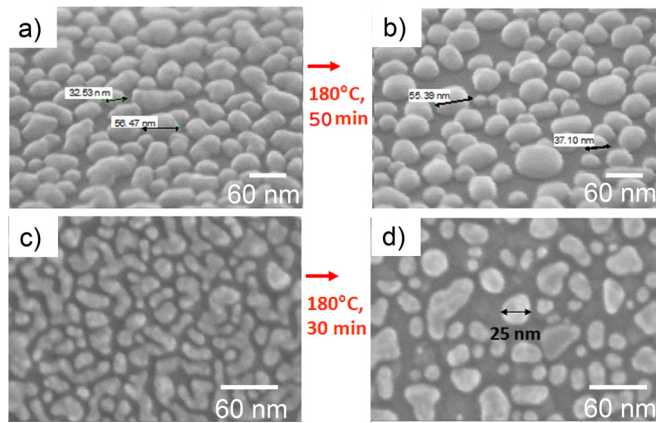


FIG. 6. SEM images of metallic island films obtained by thermal evaporation of 10 nm Ag on c-Si before (a) and after (b) annealing treatment at 180 °C during 50 min. SEM images of metallic island films obtained by thermal evaporation of 3 nm Ag on ZnO before (c) and after (d) annealing treatment at 180 °C during 30 min.

(Figs. 6(b) and 6(d)). For a 3 nm thick film, the surface density of Ag islands is also reduced from 62% to 38% on ZnO ORL. Thus, the annealing generates more isolated silver nanoparticles. The formation of these isolated silver nanoparticles is attributed to different thermal expansion coefficients between Ag islands and the transparent layer and to the relaxation of the thermal stress during the annealing.^{8,9}

An AFM image of the same Ag layer on a glass after annealing is shown in Fig. 7. It is important that layer consists of well pronounced isolated nanoparticles even after annealing, showing a tendency of sintering. Namely, their measurements indicate that the Ag surface is smooth and the thickness is higher than the nominal thickness. Contrary to AFM measurement, the microbalance underestimates the thickness since the film is not homogeneous but composed of isolated Ag islands. This means the film density is lower than the bulk silver density taken to determine the nominal thickness.

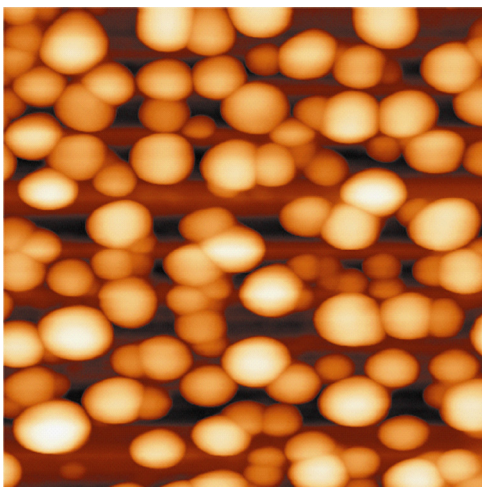


FIG. 7. AFM image of 3 nm Ag on laboratory glass on an area of 1 μm \times 1 μm after annealing (250 °C for 1 h). The nanoparticles are separated. The nanoparticles have an average height and diameter estimated at 30 nm and 120 nm, respectively.

IV. DISCUSSION

The measured reflectance spectra compared to the theoretical ones are also performed. The theoretical model is based on the calculation of reflectance from a model which consists of three layers: the Ag mirror, the ZnO or the SiO₂ layer and top layer composed of a mixture of Ag and void. Effective medium approximation determines the effective dielectric functions of a composite medium as a mathematical combination of the dielectric functions of its constituent. Maxwell Garnett (MG)¹⁹ and Bruggeman effective medium approximation (BMA)²⁰ formulated, respectively, by below equations,

$$\frac{\varepsilon_{eff}(\lambda) - 1}{\varepsilon_{eff}(\lambda) + 2} = f \frac{\varepsilon_{Ag}(\lambda) - 1}{\varepsilon_{Ag}(\lambda) + 2}, \quad (1)$$

$$0 = (1 - f) \frac{1 - \varepsilon_{eff}(\lambda)}{1 + 2\varepsilon_{eff}(\lambda)} + f \frac{\varepsilon_{Ag}(\lambda) - \varepsilon_{eff}(\lambda)}{\varepsilon_{Ag}(\lambda) + 2\varepsilon_{eff}(\lambda)}, \quad (2)$$

are used and compared. Where ε_{Ag} is the dielectric function of Ag and ε_{eff} is the effective dielectric function of the medium composed of a mixture of silver and void, f the volume fraction of Ag and λ the wavelength. MG theory gives a realistic description of a medium when the volume fraction of inclusions, weakly interacting with each other, is smaller than that of the host material. BMA describes the optical properties of composite mediums where inclusions and host material have similar roles in the effective medium.

Considering the size of Ag islands, surface damping effect can be neglected.²¹ The Ag dielectric function was taken from the literature as for bulk silver.¹⁰ The ZnO and SiO₂ dielectric function was also extracted from the literature without any additional fitting. Only three parameters are fitted: the ZnO or SiO₂ film thickness, the Ag film thickness, and the volume fraction f of Ag. Some examples of such comparison are given in Fig. 8. Close to the UV range (200 nm to 300 nm), the measured and calculated spectra show only a trend line. In this spectral region where the reflectance is essentially attributed to both, the interband transitions of Ag and the ZnO layer, further detailed studies are necessary. However, from 300 nm, the resulting curve is in fair agreement with the measured one. It was not possible to find a serious fit of the reflectance without the ORL for the lines 1 and 2 in Fig. 4. Contrary to these spectra, the reflectance for lines 3 and 4 provides from the multi absorption and multi reflection in the ORL. This suggests that the ORL structure improves the sensitivity to the optical properties of the top layer.

For the 1 nm nominal thick Ag layer, MG and BMA (not shown) can both be used to model the reflectance spectra indicating a threshold condition between both models. However, BMA gives a slightly better fit. Above 1 nm, MG effective medium approximation fails to predict the reflectance spectra of the as-deposited Ag film while the calculated spectrum from BMA is in agreement with the measured one (Fig. 8). MG works well for isolated particles embedded in a host matrix. As shown in Fig. 5(a) for a 3 nm thick Ag layer, both compound, i.e., Ag and void, plays a symmetric rule,

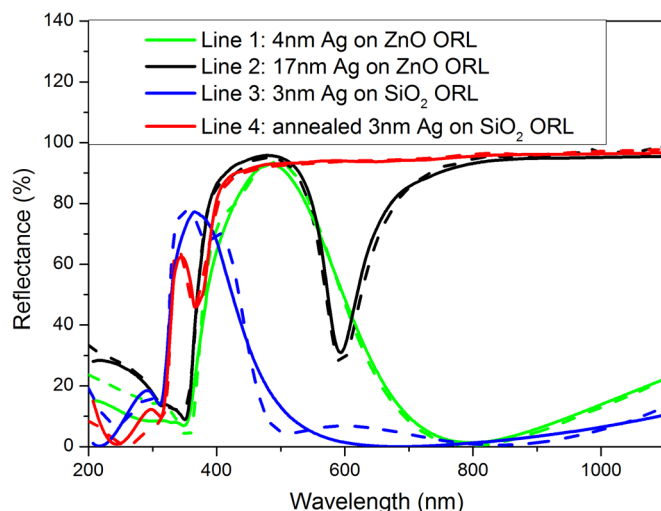


FIG. 8. Reflectance measurements (dash lines) and calculated spectra (solid lines) for 4, 17 nm-thick Ag layers on ZnO ORLs and 3 nm-thick Ag layers on SiO₂ ORLs before and after an annealing treatment.

suggesting that the reflectivity spectra must be interpreted in term of BMA (Fig. 8). Above 17 nm, the experimental data can be analysed thanks to a simple homogeneous silver film without void. As expected, the Ag islands tend to percolate (Fig. 5(b)), forming a continuous film (Fig. 5(c)).

As shown in Fig. 9, the thickness of the Ag layer on the ZnO ORL, deduced from reflectance measurement, is higher than the nominal thickness but is in agreement with AFM measurements (Fig. 7). As we introduced previously, microbalance measurements underestimate the film thickness. We will discuss now the dynamics of nucleation, percolation and the early stages of bulk Ag film. In the initial stages of film formation, the thickness measured by reflectivity and the volume fraction of silver both increase rapidly. Beyond a 4 nm nominal thickness, the thickness slightly decreases and remains constant in the nominal thickness range of 6 nm–17 nm. This behaviour was observed by Little *et al.*,²² and indicates that the film grows in a Volmer-Weber mode.^{23–25}

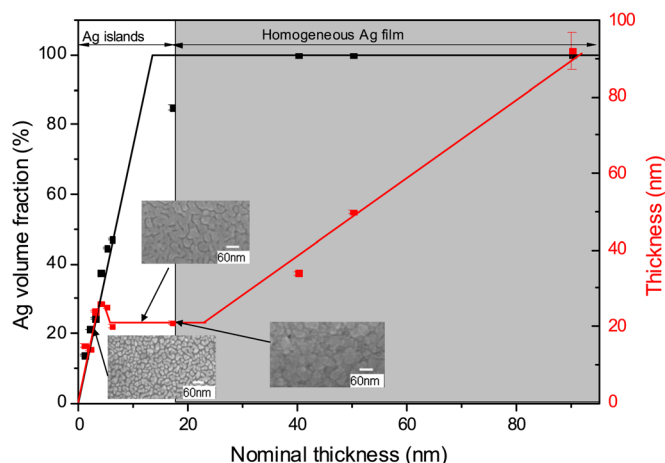


FIG. 9. Ag volume fraction and thickness of the deposited layer on the ZnO ORL, calculated by fitting the experimental reflectance spectra, versus the nominal thickness estimated from mass measurements. The dots are the results of the fits. SEM images of a 3 nm, a 10 nm, and a 20 nm-thick Ag layer on a ZnO ORL are included to facilitate the analysis.

Adatoms migrate on the surface until they nucleate on other adatoms resulting in the formation of Ag islands (Fig. 5(a)). Further deposition fills empty space between the islands (Fig. 5(b)). At this step, the volume fraction of the film increases without any modifications of the film thickness until the islands begin to agglomerate and form a percolated network.²³ Once the surface is completely covered, the film thickness starts to increase linearly with the nominal thickness suggesting that the film grows like a layer by layer in a Frank–Van der Merwe mode.^{24,26} Finally, a homogeneous Ag layer is formed (Fig. 5(c)).

The real part of the effective dielectric function (Fig. 10(a)) decreases monotonously when the nominal film thickness increases. When the nominal thickness becomes higher than 4 nm, the real part of the effective dielectric function takes negative value in the visible spectral range. As reported by Oates *et al.*,²⁶ the percolation threshold can be determined from the effective dielectric function of the Ag layer. It corresponds to the nominal thickness where the real part of the effective dielectric function falls below zero. In agreement with SEM investigations (Figs. 5(a) and 5(b)), for this nominal thickness estimated between 4 nm and 6 nm, the silver volume fraction varies between 38% and 48%, and the film transits from a dielectric to a conductor. The imaginary part of the effective dielectric function (Fig. 10(b)) of the 1 nm Ag layer has a wide band centred at 500 nm which is attributed to the plasmon resonance of the composite layer.²⁷ Due to the electro-magnetic interactions between islands, this band is redshifted and becomes progressively wider as the film grows.²⁷ The imaginary part of the effective dielectric function of a 4 nm thick Ag film is larger than the Ag bulk one. This high absorption induces that the reflection goes to the zero line in the visible range. Beyond a 4 nm film thickness, the opposite trend is observed. The plasmon band is blueshifted and becomes progressively narrower as the film grows. Finally, for high nominal film thickness, the dielectric function tends toward the Ag bulk one.

Before annealing, the optical properties of the silver composite layer deposited on the SiO₂ ORL are nearly described by the BMA approximation (Fig. 8, line 3). Some deviations between the experimental data and the calculated ones, attributed to the presence of isolated islands in the nearly percolated network (Fig. 6(a)), are observed. It suggests that other effective medium models need to be developed to describe the optical properties of silver layer in the intermediate state between percolated and nonpercolated silver islands. The post-annealing process alters significantly the structural properties (Figs. 6(b) and 6(d)) and the optical properties (Fig. 4) of the film.⁸ It produces isolated Ag nanoparticles with nearly spherical shape (Figs. 6(b), 6(d), and 7). After the annealing, important deviation between BMA and the experimental data are observed (not shown). As shown in Figs. 6(b)–6(d) and Fig. 7, the concentration of silver islands is sufficiently low to consider them as completely isolated inclusion. Indeed, for a 3 nm thick film, the surface density of Ag islands is reduced from 62% to 38%. Thus, MG approximation well describes the optical properties of the annealed Ag layer (Fig. 8). The imaginary part of the effective dielectric function of the Ag layer presents a

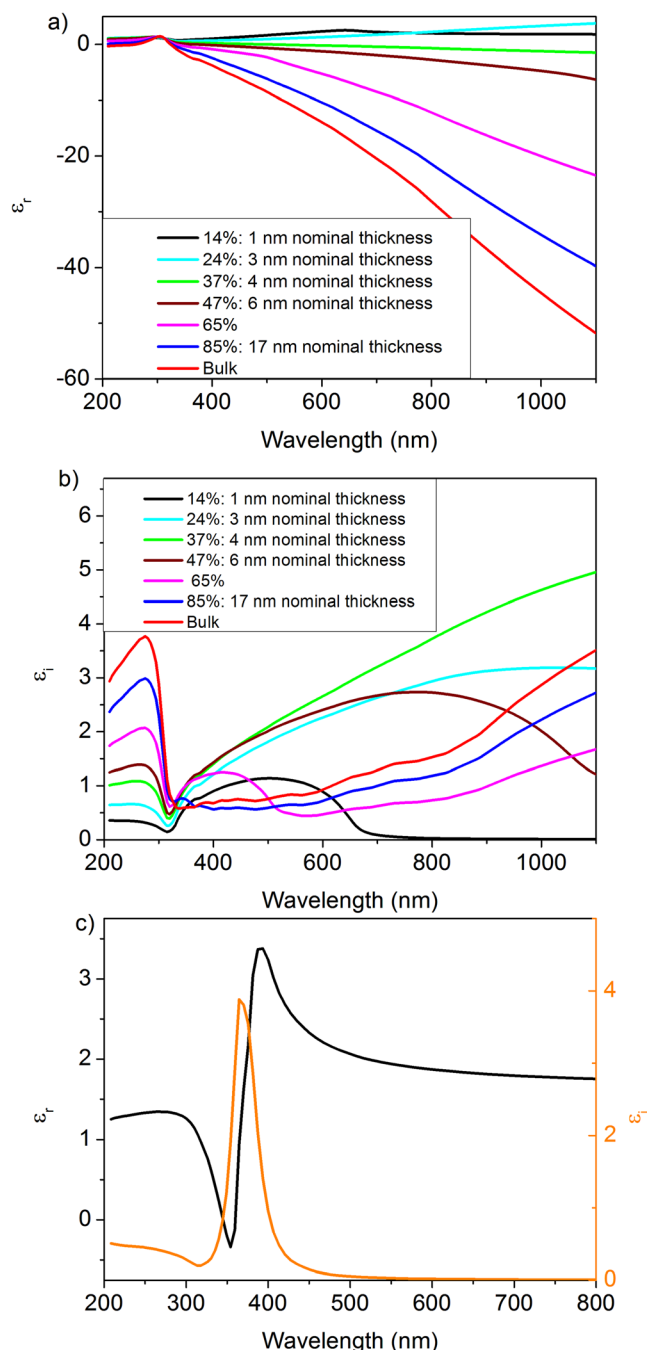


FIG. 10. Variations of the real part (a) and imaginary part (b) of the effective dielectric function of the Ag layer during the deposition on a ZnO ORL. The curves calculated for 65% of Ag volume fraction is added to facilitate the interpretation. (c) Real part and imaginary part of the effective dielectric function of the 3 nm thick Ag layer on a SiO₂ ORL after the annealing.

narrow band centred at 380 nm (Fig. 10(c)). This band is the plasmon resonance of the isolated metallic islands.^{4,28} This absorption induces a decrease in reflectivity at 380 nm (Fig. 8). In accordance with Kramers-Kronig relations,²⁹ the real part of the effective dielectric function of the Ag layer varies strongly close to the plasmon resonance wavelength. As the complex dielectric function is weakly disturbed beyond this wavelength, the reflectivity in the visible spectral range is similar to that of the structure before the Ag deposition (not shown).

Thus, the effective dielectric function can be tuned by varying the nominal thickness or by using a post-annealing process. Its real part can take a negative value which is suitable for designing new metamaterial devices.^{27,30,31}

V. CONCLUSION

This work shows that reflectometry on the ORL is a straightforward measurement to study the percolation of thin silver films and their modification by annealing. The ORL enhances the sensitivity to the optical properties of the thin top layer. The modeling with the effective medium approximation highlights the growth mechanisms of the silver layer. In the first step it grows in a Volmer-Weber mode and after a complete coverage of the surface, it grows in a Frank-Van der Merwe mode. From the model, the percolation threshold can be estimated to a nominal thickness of nearly 4–6 nm. The annealing of silver layers generates isolated silver particles with a narrow plasmon resonance. The studies have shown that the effective dielectric is negative in the visible range for percolated silver films, which is useful for optical applications.

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- ¹R. W. Cohen, G. D. Cody, M. D. Coutts, and B. Abeles, *Phys. Rev. B* **8**, 3689 (1973).
- ²R. S. Sennett and G. D. Scott, *J. Opt. Soc. Am.* **40**, 203 (1950).
- ³S. Yoshida, T. Yamaguchi, and A. Kinbara, *J. Opt. Soc. Am.* **61**, 62 (1971).
- ⁴K. L. Kelly, E. Coronado, L. L. Zhao, and G. C. Schatz, *J. Phys. Chem. B* **107**, 668 (2003).
- ⁵G. A. N. Connell, R. J. Nemanich, and C. C. Tsai, *Appl. Phys. Lett.* **36**, 31 (1980).
- ⁶D. R. Smith, J. B. Pendry, and M. C. K. Wiltshire, *Science* **305**, 788 (2004).
- ⁷S. Ducourtieux, V. A. Podolskiy, S. Gresillon, S. Buil, B. Berini, P. Gadanne, A. C. Boccara, J. C. Rivoal, W. A. Bragg, K. Banerjee, V. P. Safo-nov, V. P. Drachev, Z. C. Ying, A. K. Sarychev, and V. M. Shalaev, *Phys. Rev. B* **64**, 1654031 (2001).
- ⁸R. S. Moirangthem, M. T. Yaseen, P.-K. Wei, J.-Y. Cheng, and Y.-C. Chang, *Biomed. Opt. Express* **3**, 899 (2012).
- ⁹S. A. Little, T. Begou, R. W. Collins, and S. Marsillac, *Appl. Phys. Lett.* **100**, 051107 (2012).
- ¹⁰E. D. Palik, *Handbook of Optical Constants of Solids* (Academic Press Handbook Series, New York, 1985).
- ¹¹J. Sukmanowski, J.-R. Vigié, B. Nörling, and F.-X. Royer, *J. Appl. Phys.* **97**, 104332 (2005).
- ¹²A. Leitner, Z. Zhao, H. Brunner, F. R. Aussenegg, and A. Wokaun, *Appl. Opt.* **32**, 102 (1993).
- ¹³R. R. Singer, A. Leitner, and F. R. Aussenegg, *J. Opt. Soc. Am. B* **12**, 220 (1995).
- ¹⁴E. Moulin, J. Sukmanowski, P. Luo, R. Carius, F. X. Royer, and H. Stiebig, *J. Non-Cryst. Solids* **354**, 2488 (2008).
- ¹⁵E. Moulin, P. Luo, B. Pieters, J. Sukmanowski, J. Kirchhoff, W. Reetz, T. Müller, R. Carius, F.-X. Royer, and H. Stiebig, *Appl. Phys. Lett.* **95**, 033505 (2009).
- ¹⁶J. Sukmanowski, C. Paulick, O. Sohr, and F. X. Royer, *J. Appl. Phys.* **88**, 2484 (2000).
- ¹⁷Y. Battie, N. Destouches, F. Chassagneux, D. Jamon, L. Bois, N. Moncoffre, and N. Toulhoat, *Opt. Mater. Express* **1**, 1019 (2011).
- ¹⁸W. Li, S. Seal, E. Megan, J. Ramsdell, K. Scammon, G. Lelong, L. Lachal, and K. A. Richardson, *J. Appl. Phys.* **93**, 9553 (2003).
- ¹⁹J. C. M. Garnett, *Philos. Trans. R. Soc. London, Ser. A* **203**, 385 (1904).
- ²⁰D. A. G. Bruggeman, *Ann. Phys.* **416**, 665 (1935).

- ²¹U. Krebig and M. Volmer, *Optical Properties of Metal Clusters* (Springer, Berlin, 1995).
- ²²S. A. Little, R. W. Collins, and S. Marsillac, *Appl. Phys. Lett.* **98**, 101910 (2011).
- ²³T. W. H. Oates, L. Ryves, and M. M. M. Bilek, *Opt. Express* **16**, 2302 (2008).
- ²⁴H. T. Beyene, J. W. Weber, M. A. Verheijen, M. C. M. Van de Sanden, and M. Creatore, *Nano Res.* **5**, 513 (2012).
- ²⁵S. Marsillac, S. A. Little, and R. W. Collins, *Thin Solid Films* **519**, 2936 (2011).
- ²⁶T. W. H. Oates and A. Mücklich, *Nanotechnology* **16**, 2606 (2005).
- ²⁷J. Sancho-Parramon, V. Janicki, and H. Zorc, *Opt. Express* **18**, 26915 (2010).
- ²⁸A. L. Gonzalez and C. Noguez, *Phys. Status Solidi C* **4**, 4118 (2007).
- ²⁹R. de L. Kronig, *J. Opt. Soc. Am.* **12**, 547 (1926).
- ³⁰J. B. Pendry, *Phys. Rev. Lett.* **85**, 3966 (2000).
- ³¹N. Fang, H. Lee, C. Sun, and X. Zang, *Science* **308**, 534 (2005).