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Laser-induced ultrafast demagnetization and perpendicular magnetic anisotropy reduction in a Co$_{88}$Tb$_{12}$ thin film with stripe domains


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We use time-resolved x-ray resonant magnetic scattering (TR-XRMS) at the Co $M_{2,3}$ and Tb $O_1$ edges to study ultrafast demagnetization in an amorphous Co$_{88}$Tb$_{12}$ alloy with stripe domains. Combining the femtosecond temporal with nanometer spatial resolution of our experiment, we demonstrate that the equilibrium spin texture of the thin film remains unaltered by the optical pump pulse on ultrashort timescales ($<1$ ps). However, after $\sim$4 ps, we observe the onset of a significant domain wall broadening, which we attribute to a reduction of the uniaxial magnetic anisotropy of the system, due to energy transfer to the lattice. Static temperature-dependent magnetometry measurements combined with analytical modeling of the magnetic structure of the thin film corroborate this interpretation.

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I. INTRODUCTION

In their seminal work published in 1996, Beaurepaire et al. demonstrated that femtosecond laser pulses can induce a transient quenching of the magnetic moment of a Ni thin film on sub-ps timescales [1]. This unexpected finding gave birth to a whole new research field, “femtomagnetism,” which aims at unraveling the complex nonequilibrium phenomena at play when magnetic nanostructures and thin films are subjected to ultrashort optical excitations. However, despite more than 20 years of scientific effort, there is still no consensus regarding the underlying microscopic mechanisms and a variety of theories are currently “coexisting” [2–10]. One particularly appealing explanation for the occurrence of laser-induced demagnetization is the creation of spin-polarized currents, resulting from the different mean free paths of majority and minority spin carriers [6,11]. In fact, during the last decade, a plethora of carefully designed experiments have been performed unraveling the importance of such superdiffusive spin flow during ultrafast magnetization loss [12–19].

Magnetic thin films with strong perpendicular magnetic anisotropy (PMA) and presenting alternating domains with “up” and “down” magnetization are a beautiful test bed to gain a better understanding of such ultrafast spin transport phenomena. Indeed, they are ideally suited to perform x-ray resonant magnetic scattering (XRMS) experiments [21,22], which provide intrinsic element selectivity and nanometric spatial resolution. Using appropriate pump-probe geometries, these advantages can be combined with femtosecond temporal resolution, making time-resolved XRMS (TR-XRMS) a powerful tool to study ultrafast spin texture changes. Yet, the results gathered on different magnetic systems remain contradictory and their interpretation controversial. Pfau et al. studied Co/Pt multilayers at the Co $M_{2,3}$ and Tb $O_1$ absorption resonances and found an ultrafast shift of the maximum value of the scattering intensity with a time constant of approximately 300 fs, which they attributed to a superdiffusive spin-current-induced domain wall broadening [13]. In a similar experiment, Zusin et al. scrutinized CoFe/Ni multilayers at the Ni $L_3$ edge and identified a pump-induced shift of the diffraction ring reaching 6% within 1.6 ps which they interpreted as an ultrafast domain dilation, resulting from inelastic electron-magnon scattering [23]. This contrasts with earlier work performed by Vodungbo et al., who studied Co/Pd multilayers at the Co $M_{2,3}$ edges using a fs high-order harmonic generation (HHG) source and reported that the magnetic domain structure remained unaffected during the ultrafast demagnetization process [13]. However, they found a significantly decreased demagnetization time, which they attributed to an ultrafast angular momentum transfer between adjacent domains. Surprisingly, Moisan et al., studying maze patterned Co/Pt and Co/Pd thin films using a time-resolved...
magneto-optical Kerr (TR-MOKE) setup, concluded that hot-electron spin-dependent transfer between adjacent domains does not impact the ultrafast dynamics at all [24]. These examples clearly illustrate the need to conduct additional studies in order to (a) further quantify the impact of ultrashort laser excitation on magnetic thin films with a complex spin texture and (b) clarify the role played by superdiffusive spin currents when changes in the magnetic structure occur on femtosecond timescales.

In the present paper, we describe TR-XRMS experiments on amorphous Co-Tb thin films with magnetic stripe domains conducted at the free-electron laser FERMI. Although several femtomentumagnetism studies have already been performed on ferrimagnetic Co-Tb [25−28], a material system of great technological relevance for future all optical magnetic data storage [29−31], experiments describing the evolution of magnetic domain structures in rare earth−transition metal (RE-TM) alloys following an ultrashort optical pulse are still scarce. Recently, Fan et al. performed a TR-XRMS study on Co88Tb12 samples using a tabletop HHG source but their analysis remained limited to the first magnetic diffraction order at the N edge of Tb (155 eV) [32]. In the present work, we complement their findings using different probe beam energies and deepen the analysis by using an experimental setup that allows us to record the first and third magnetic diffraction order simultaneously. With this, we are able to explicitly monitor the pump-induced evolution of the periodic magnetic structure, i.e., the change of domain size and domain wall width with the highest accuracy up to 120 ps, as will be shown in detail in the following.

II. EXPERIMENTS

A. Sample growth and characterization

The samples consist of Co-rich [33], amorphous Co88Tb12 thin films (nominal concentration) with a nominal thickness h = 50 nm. The magnetic films were sputter deposited on Si3N4 square membranes with the surface 50 μm × 50 μm covered with a buffer layer consisting of 5-nm Pt on top of 5-nm Ta. A 3-nm Pt capping was used to protect the samples from oxidation. After deposition, the samples were subjected to a demagnetization procedure using an oscillating in-plane field with decreasing amplitude [22].

Polar magneto-optical Kerr effect (p-MOKE) measurements were performed to analyze the static magnetic properties of the thin films in the out-of-plane direction. Magnetic force microscopy (MFM) data were gathered on an Asylum Research magnetic force microscope. Temperature-dependent in-plane magnetization curves were obtained using a vibrating sample magnetometry/superconducting quantum interference device (VSM/SQUID) from Quantum Design.

B. Time-resolved x-ray resonant magnetic scattering (TR-XRMS)

The pump-probe experiments were performed at the DiProI beam line of the free-electron laser (FEL) FERMI [34]. The samples were pumped with a laser (λ = 400 nm) with 60-fs pulse duration, then probed by 70-fs short monochromatic circularly polarized XUV pulses delivered by the FEL with photon energies tuned either to the Co M2,3 absorption edges at 20.8 nm (59.6 eV) or to the Tb O1 absorption edge at 27 nm (45.9 eV) with a beam monochromaticity \( \lambda \Delta \lambda \approx O(10^{-3}) \) [full width at half maximum (FWHM)]. The delay line between the two pulses was implemented on the optical path of the pump pulse. A four-quadrant photodiode was used to provide an accurate shot-to-shot measurement of the FEL intensity, and allowed us to normalize the detected scattering intensity by the incoming photon flux (l0) and to monitor the pointing stability of the beam. The scattering patterns were detected with a vacuum compatible charge coupled device (CCD) with 2048 × 2048 px2 and a pixel width of 13.5 μm. To increase the read-out speed, the CCD pixels have been binned 2 × 2, yielding an effective pixel size of 27 μm. The spot size diameter of the probe and the pump beam were equal to 190 × 180 and 400 × 400 μm2, respectively. This focal size ensured a uniform illumination across each single membrane. To block the direct beam, a cross-shaped beam stop was placed in front of the CCD. A schematic of the experimental setup is depicted in Fig. 1(a).

III. RESULTS AND DISCUSSION

A. PMA and creation of stripe domains

Despite their amorphous structure, sputter-deposited RE-TM thin films can exhibit strong PMA as a result of local chemical ordering [35], giving rise to domains with alternating “up” and “down” magnetization [36]. The presence of such domains in our thin films was checked using p-MOKE measurements at room temperature, yielding information about the field dependence of the average magnetization in the out-of-plane direction. As shown in Fig. 2, the hysteresis loop presents a shape that is characteristic for magnetic stripe and maze patterned films [22,24]. Starting from saturation at high external fields, domains start to nucleate and grow upon reduction of H (≃1 Koe). For zero external field, the magnetic moments of “up” and “down” domains compensate, resulting in an almost vanishing remanent magnetization. Reversal and further decrease of H then leads to successive annihilation of domains with \( \mathbf{M} \) pointing in the opposite direction, eventually yielding a saturated monodom main configuration [22].

Information about the spatial distribution of magnetic domains was obtained using MFM measurements. As shown in the inset of Fig. 2, a stripe domain structure resulting from the demagnetization procedure can clearly be evidenced and confirms our MOKE-based analysis. The periodicity determined from a fast Fourier transformation of these scans isΛ ≃ 220 ± 10 nm. This corresponds to an average domain size w = \( \frac{\Lambda}{2} \equiv 110 \pm 5 \) nm.

B. Ultrafast demagnetization

The laser excitation-induced evolution of the magnetization in CoTb was analyzed with TR-XRMS using the stripe domain samples described above. To study the Co and Tb sublattices individually, the probe beam energy was set either to the M2,3 edges of Co, or to the O1 edge of Tb. For every delay value Δt, CCD images were obtained by averaging over 50 pulses (5s acquisition time with the FEL operated at 10 Hz) and then background subtracted. An exemplary inten-
FIG. 1. Schematic of the pump-probe experiment and exemplary CCD data. (a) Resonant magnetic scattering setup: The CoTb samples are pumped using a laser with \( \lambda = 400 \) nm (blue beam) and varying fluences up to \( \Phi = 3.5 \) mJ cm\(^{-2}\). The system is then probed using XUV radiation (magenta beam) tuned either to the Co \( M_{3,2} \) edges (\( \lambda = 20.8 \) nm, \( E = 59.6 \) eV) or the Tb \( O_1 \) edge (\( \lambda = 27 \) nm, \( E = 45.9 \) eV). Changing the delay \( \Delta t \) between the pump and probe pulses allows us to record the temporal evolution of the scattering signal. (b) Magnetic diffraction pattern obtained at the Co \( M_{2,3} \) edges (1024 px × 1024 px)—the first-order magnetic scattering peaks can clearly be identified. The azimuthal angle \( \theta \) used for integration of the signal is sketched as well (the azimuthal maximum of the peak defines \( \theta = 0 \)). Inset: The same data set (1024 px × 1024 px) is plotted using a different intensity scale (same lower bound, but saturated beyond \( I_{\text{sat}} = 500 \) counts) to show the third-order diffraction maxima. Note that the dashed lines enclose the first scattering order in (b), while the third order is highlighted in the inset. The small peaks that can be observed at \( \theta = 90^\circ \) result from an artificial grating structure manufactured prior to the magnetic film deposition on the back side of the sample membrane and are not relevant in the context of this study [20].

FIG. 2. Room-temperature \( p \)-MOKE measurements describing the out-of-plane (OP) magnetization of the sample as a function of the applied external field. Inset: MFM-phase contrast image (2 × 2 µm\(^2\)). The arrow on top of the scan indicates the direction of the external magnetic field applied during the demagnetization procedure.

Thus correspond to the positive and negative first (\( n = \pm 1 \)) and third magnetic diffraction order (\( n = \pm 3 \)). As shown in earlier work for magnetic systems with a perfect square-wave magnetization pattern, their intensity is proportional to the square of the scalar product between the domain magnetization vector \( \mathbf{M} \) and the propagation vector \( \mathbf{k} \) of the x-ray beam [21]. Note that, due to nonparallel in-plane alignment of the stripes in the probed zone, the peaks are smeared along the arc of a circle [Fig. 1(b)], which, for the extreme case of a magnetic maze pattern, would give rise to homogeneous diffraction rings. Applying these considerations to our specific experimental setup results in \( M(\Delta t) \propto \sqrt{I_1(\Delta t)} \), which links the local domain magnetization \( M(\Delta t) \) with \( I_1(\Delta t) \), the total first-order peak intensity after azimuthal integration. We stress that in our approach, we implicitly neglected possible nonmagnetic contributions that might result from charge heterogeneities on nanometer length scales [21]. This was motivated by the absence of any significant signal measured at \( \theta = 90^\circ \), where the magnetic contrast (essentially resulting from defects along the stripe patterns) ought to be negligible.

Figure 3 shows the normalized magnetization \( M(\Delta t)/M_0 \) for Co and Tb atoms obtained with the maximum pump fluence employed in the present work (\( \Phi = 5.5 \) mJ cm\(^{-2}\)). Both curves exhibit a rather similar behavior: The magnetization drops rapidly by approximately 10% during the first hundreds of femtoseconds, and then slowly increases on longer timescales. While the degree of demagnetization is comparable for both elements, the characteristic times associated with the initial quenching and subsequent magnetization recovery clearly differ. To gain further insight into these processes, we fitted the data to the well-established three-temperature model [1] (see Appendix A for details).
The fits, presented in Fig. 3, provide a quantitative description of the demagnetization process and allow to draw several conclusions: First, within experimental resolution (90 fs), we do not observe any significant delay between the demagnetization onset of Co and Tb atoms [37]. Second, the two magnetic sublattices exhibit very similar demagnetization amplitudes. Finally, the demagnetization process in Tb is found to be slower than in Co, which is in agreement with earlier reports on RE-TM alloys [25,26,38]. Surprisingly, from a quantitative perspective, our results show rather poor agreement with the literature data. At the Co edge, we obtain \( \tau_M(\text{Co}) = 110 \pm 30 \) fs (with almost no impact of the employed pump fluence, as shown in Table I), which is slightly smaller than what has been reported so far for pure Co thin films [5], as well as for ferro- [24,39] and ferrimagnetic [25,40,41] Co-based alloys. At the Tb edge, where our fits yield \( \tau_M(\text{Tb}) = 220 \pm 30 \) fs, the discrepancy is even more pronounced. Indeed, this value is two to three times smaller than what has been obtained on CoTb thin films with an almost identical composition [25,32].

It was put forward that decreased values of \( \tau_M \) might be an indicator for superdiffusive spin transport in stripe or maze domain structured films. Observations made by Vodungbo et al. in CoPd alloys with large PMA [13] revealed surprisingly small demagnetization time constants \( (\tau_M \approx 100 \text{ fs}) \), that remained independent of the fluence, and which they attributed to a spin-polarized transport of hot electrons between neighboring domains. However, in the present case, we believe that \( \tau_M \) values alone can hardly serve as conclusive parameters to evidence the presence of ultrafast spin currents, considering (i) the rather large spread of literature values, (ii) the different degrees of quenching obtained, as well as (iii) the variety of experimental techniques (XMCD at different edges, MOKE) employed in previous studies to characterize the pump-induced magnetization drop.

A more reliable strategy to observe superdiffusive spin transfer between domains would consist in unveiling the possible ultrafast changes of the domain wall structure, where an enhanced demagnetization due to an accumulation of minority electrons is expected to take place [15,42]. As will be shown in the next section, our experiments, where the first- and third-order magnetic diffraction peaks are recorded simultaneously, allow us to directly monitor the impact of the pump pulse on the magnetic structure of the CoTb thin films, thereby providing more reliable evidence for the presence or absence of superdiffusive interdomain spin transport.

### C. Pump-pulse-induced changes of the magnetic structure

In the previous section, we have used the first-order magnetic diffraction peak intensity to gain information about the average domain magnetization. In fact, additional spatial information concerning the spin texture of the thin film, i.e., average domain sizes \( w(\Delta t) \) and domain wall widths \( d(\Delta t) \), is encoded in the time-dependent diffraction pattern. To calculate \( w(\Delta t) \), we first translated the CCD data into \( q \) space (Appendix B). After subsequent azimuthal integration, the average domain size was obtained from \( I(q) \) via \( w(\Delta t) = \left( \frac{\pi n}{q_n(\Delta t)} \right) \) being the location of the \( n \)th maximum for a given delay \( \Delta t \). All results presented in the following were obtained from data gathered at the Co edge, using the maximum pump fluence \( \Phi = 5.5 \text{ mJ cm}^{-2} \).

Figure 4(a) shows \( I(q) \) curves gained after azimuthal integration for different delays \( \Delta t \), and Fig. 4(b) the temporal evolution of \( q_1(\Delta t) \) and \( q_3(\Delta t) \), the first-order and third-order maxima. For better readability, the \( q_n \) values were normalized using the unpumped references \( \langle q_1^{\text{unpumped}} \rangle = 0.023 \text{ nm}^{-1} \) and \( \langle q_3^{\text{unpumped}} \rangle = 0.070 \text{ nm}^{-1} \). This corresponds to an average domain size of \( 136 \pm 1 \) nm, which is slightly larger, but still in reasonable agreement with our MFM measurements and close to the values obtained recently on a Co88Tb12 sample with an identical magnetic layer thickness [32]. Careful analysis of the data reveals that there is no ultrafast \( q_n \) variation for the fluences employed in our study: Neither for subpicosecond delays, as reported by Pfau et al. in Co/Pt multilayers \( (\Delta q/q_0 = 4\% \text{ after 300 fs}) \) [15] nor on slightly longer timescales, as shown by Zusin et al. for CoFe/Ni thin films \( (\Delta q/q_0 = 6\% \text{ after 1.6 ps}) \) [23], do we find any significant shift of the magnetic diffraction peaks. It is also instructive to compare our results with the data recently gained by Fan et al. [32], as their XRMS experiments have been performed on a CoTb sample with an identical thickness and concentration [32]. In contrast to our findings, Fan et al. also observe a displacement of the peak maximum.

### Table I. Impact of the pump fluence \( \Phi \) on the maximum demagnetization \( \frac{M_t - M_0}{M_0} \) and characteristic demagnetization time constants at the Co \( M_{2,3} \) edges obtained by fitting the data to the three-temperature model (Appendix A).

<table>
<thead>
<tr>
<th>( \Phi ) (mJ cm(^{-2}))</th>
<th>( \frac{M_t - M_0}{M_0} ) ( \text{max} )</th>
<th>( \tau_M ) (fs)</th>
</tr>
</thead>
<tbody>
<tr>
<td>2.6</td>
<td>0.06</td>
<td>110 ( \pm ) 30</td>
</tr>
<tr>
<td>3.4</td>
<td>0.08</td>
<td>105 ( \pm ) 30</td>
</tr>
<tr>
<td>5.5</td>
<td>0.11</td>
<td>110 ( \pm ) 30</td>
</tr>
</tbody>
</table>
responds to a 5% variation of the peak positions in reciprocal space. The blue background corresponds to a 5% variation of the peak positions in reciprocal space. The positions of the first-order and third-order maxima are highlighted. Fits to the Hellwig model are shown as red dashed lines. (b) Temporal evolution of the first-order and third-order diffraction peaks (blue, solid line and orange, dashed line, respectively) and (b) their ratio $R/R_0$ shown for two different, consecutive delay scans, illustrating the good reproducibility of the measurements. The black arrow shown in (a) indicates the onset of the domain wall broadening.

FIG. 4. Azimuthally integrated intensity in reciprocal space and temporal evolution of the averaged first- ($n = +1$ and $n = -1$) and third-order peaks ($n = +3$ and $n = -3$) with time. (a) The CCD intensity is translated into reciprocal space (Appendix B) and plotted as a function of $q$ on a logarithmic scale after azimuthal integration over $-\pi/24 < \theta < \pi/24$ [see Fig. 1(b), where the white line indicates $\theta = 0$]. The results are shown for three different delays $\Delta t$ (gray circles), and the curves have been shifted vertically for better readability of the data. The positions of the first-order and third-order maxima are highlighted. Fits to the Hellwig model are shown as red dashed lines. (b) Temporal evolution of the first-order (left) and third-order peak maxima (right), obtained from a Gaussian fit and normalized by the unpumped value. The blue background corresponds to a 5% variation of the peak positions in reciprocal space.

In addition to the temporal evolution of the domain periodicity, the simultaneous recording and analysis of more than one diffraction peak allows us to assess the domain wall width, as has been proposed in earlier studies [13]. We show in Appendix C that in a simple linear chain approximation, $R = I_3/I_1$, the ratio of integrated first- and third-order peak intensities depends exclusively on $\eta = d/w$, the ratio of linear domain wall and average domain size. Considering the constant domain size evidenced at the beginning of this section, any change of $R$ must necessarily result from a variation of the domain wall (DW) width. Figure 5(a) shows the time dependency of the integrated first- and third-order intensities, normalized to their unpumped values ($\Delta t < 0$). As can be seen, both exhibit the same temporal evolution during the first several ps. This becomes even clearer when plotting $R(\Delta t)/R(0)$, which corresponds to the ratio of normalized third- and first-order integrated peaks, shown for two independent measurements in Fig. 5(b). As presented in the inset of Fig. 5(b), no change of the DW width, other than random fluctuations (up to 10% for a single measurement), can be identified for delays below 4 ps. This is another central finding of the present study: Cascades of spin-polarized electrons, which are believed to create an ultrafast enhanced demagnetization at the domain boundaries, i.e., a sub-ps broadening of the domain walls, do not seem to play a significant role in the present system. However, what becomes apparent in Fig. 5(a), and even more manifest in Fig. 5(b), is a pronounced decrease of the ratio of third- and first-order intensities for $\Delta t \gtrsim 4$ ps. Indeed, $R(\Delta t)/R(0)$ drops to 0.73 between 4 ps $\lesssim t \lesssim$ 20 ps and then slowly increases again for $\Delta t > 40$ ps, hinting at pronounced modifications of the DW width on picosecond timescales.

In principle, the aforementioned analysis can be used to obtain a quantitative description of the temporal evolution of the DW size (Appendix C). However, this approach is limited due to the presence of the beam stop, which hampers data integration at low $q$. In addition, we stress that the underlying model is unable to account for a finite correlation length of developing on even longer timescales, and eventually reaching 3% of its initial value after roughly 10 ps. While these results seem at odds with our experimental analysis, one must bear in mind that the maximum demagnetization achieved in all three studies [15,23,32] is significantly larger than what we are able to reach ($\Delta M/M_0$ is ranging approximately between 0.3 and 0.7 in the aforementioned work, while in the present case the maximum demagnetization barely exceeds 0.1). In agreement with what has been put forward in Ref. [15], our measurements thus underpin that the peak shift in $q$ space is a nonlinear phenomenon, requiring high pump fluences, i.e., larger demagnetization values, in order to be observed.
the stripe patterns and a distribution of domain sizes, typically encountered in our experiments (see the inset of Fig. 2). To avoid these shortcomings, we fitted our q-space data using the approach proposed by Hellwig et al., specifically dedicated to the description of XRMS experiments on stripe domains [22]. As shown in Fig. 4(a), the quality of the fits is reasonable, although our model systematically overestimates the third-order and underestimates the magnitude of the first-order peak, especially at low q. As shown in Appendix C, our results thus slightly underestimate the real domain wall width. Hellwig’s model relies on the use of five adjustable parameters: \( w \), \( d \), the width of the domain size distribution \( \sigma \), and \( M_c \), which is proportional to the \( z \) component of the magnetization, as well as \( N \), the number of stripes that scatter coherently. To facilitate the fit procedure, \( N \) was fitted for several arbitrarily chosen snapshots and then kept fixed for all remaining delays (\( N = 6 \)). Figure 6 shows the evolution of \( w \), \( d \), and \( \sigma \) as a function of the pump-probe delay \( \Delta t \). \( M_c \) is omitted here: As expected, it reproduces the initial magnetization, as well as \( \sigma \), which is proportional to the \( \sigma \) component of the magnetization, as well as \( N \), the number of stripes that scatter coherently.

D. Lattice heating and PMA decrease

1. Exchange stiffness and anisotropy changes

What causes this pronounced change of the magnetic structure? For the case of a single isolated 180° Bloch wall, an analytical expression linking \( d \) to microscopic magnetic parameters is readily derived by taking into consideration the competing anisotropy and exchange contributions to the total energy [43]. Minimization of the latter with respect to \( d \) results in the well-known expression \( d = \pi \sqrt{\frac{A}{K_u}} \). Thus, pump pulse-induced changes of the exchange stiffness \( A \) (which depends on the exchange integral, the total spin, and atomic distances, as shown in Appendix D) as well as changes of the anisotropy constant \( K_u \) can affect the size of the domain walls. While a variation of \( A \), that stems from a modification of the exchange interaction, is expected to take place on much faster timescales, changes linked to interatomic distances can in principle be observed after several ps. In fact, lattice constant variations can result from energy flow into the phonon bath, requiring a few ps for full equilibration in metals [44,45]. In the present case, though, thermal expansion of the lattice is expected to increase interatomic distances. This would lead to a decreased exchange stiffness and, in consequence, to a reduction of domain wall sizes, in clear contradiction with our results. Note that the rather moderate laser pulse induced heating of the sample \( \Delta T = \frac{80}{C_v} \approx 145 \text{K} \) [calculated from the reflectivity \( R = 0.7 \) of the thin film, heat capacity \( C_v(C_{08}(\text{TM}) \approx C_v(C) = 3.3 \times 10^6 \text{ J/m}^3 \text{K} \), assuming the energy to be distributed homogeneously over the entire film thickness] ensures that the final temperature of the system remains far below the Curie temperature of the alloy [46]. If we assume that a scaling relation similar to the one linking \( A \) and \( T \) in pure Co [47] holds in our Co-rich alloy, we can expect the present temperature-induced change of \( A \) to be negligible. In the following, we will thus exclusively focus on \( K_u \) as the main parameter driving the observed domain wall size increase.

2. T-dependent magnetization measurements and analytical modeling

Static, temperature-dependent magnetization measurements were used to compute \( K_u(T) \) and establish the link between laser-induced heating of the sample and the magnetic structure changes, as will be shown in this section. \( M(H) \) curves were determined via SQUID-VSM measurements in in-plane (IP) geometry, with \( T \) varying between 300 and 600 K, as presented in Fig. 7(a). Qualitatively, the decreasing field values \( H_s \) at which saturation is reached already hint at the change of \( K_u \) and show that higher temperatures result in a smaller anisotropy of the system. Note that the measured values of \( M_s \), presented in Fig. 7(b), increase with temperature, as expected for a TM-rich RE-TM alloy [33].

For further quantitative analysis, we describe the behavior of the magnetization of the thin film upon IP field increase as a coherent hard-axis magnetization process with an effective anisotropy \( K_{eff} \) [43]. It is linked to the work \( \Delta W \) with our earlier determination of the first- and third-order peak values. It does not change during the first 40 ps and then decreases slightly (\( \pm 1 \text{nm} \)) during the following 80 ps (note that the width of the domain size distribution is not affected by the optical pump pulse). Finally, the values of \( d \) confirm what we have put forward earlier in this section: The domain wall width remains constant during the first ps (\( d = 32 \pm 2 \text{ nm} \)). It then starts increasing significantly after 4 ps until saturating at \( 45 \pm 2 \text{ nm} \) after roughly 20 ps, which represents a relative change of 41% of its initial value. For \( \Delta t > 40 \text{ ps} \) the domain wall width finally decreases again at a slow rate of \( \approx 0.06 \text{ nm} / \text{ps} \).

![Fig. 6. Hellwig’s model fitted to the present XRMS data at the Co M_{2,3} edges. Evolution of the fit parameters with delay \( \Delta t \), from top to bottom: domain size \( w \) (orange), domain wall width \( d \) (blue), and width of the domain size distribution \( \sigma \) (green). While \( w \) and \( \sigma \) remain constant over time, a clear increase of the domain wall size can be seen for \( \Delta t > 4 \text{ ps} \) (black arrow).](image-url)
Note that the remanent magnetization at room temperature diamonds. A small, finite hysteresis is observed for at 300 K (blue dots), 400 K (orange squares), and 500 K (green plane via \( K_{\text{eff}} \)). Thus, we perform on the CoTb layer to align the magnetization in IP configuration. (a) Normalized magnetization curves in the OP configuration) without an external field. We calculated the equilibrium energy of the stripe configuration (in the OP configuration) using the analytical model proposed by Virot \[48\]. As shown in Appendix D, \( e_{\text{ex}} \) consists of a sum of magneto-static, anisotropy, and exchange contributions and is obtained by numerical minimization with respect to \( w \) and \( d \). This eventually results in an implicit equation for \( K_u(\Delta V) \). Thus, knowledge of temperature-dependent experimental \( \Delta V_{\text{exp}} \) values [Fig. 7(b)] yield \( K_u(T) \) and, consequently, the equilibrium domain wall width \( d[K_u(T)] \) and domain size \( w[K_u(T)] \). These quantities are plotted in Fig. 8, which summarizes our modeling results.

As shown in Fig. 7(b), \( \Delta V_{\text{exp}} = 3.1 \times 10^5 \) J/m\(^3\) at 300 K, from which we calculate \( K_u = 5.1 \times 10^5 \) J/m\(^3\) (Fig. 8). This is smaller than the available literature data: El Hadri et al. provide a detailed account of uniaxial anisotropy values in amorphous Co\(_x\)Tb\(_{1-x}\) thin films [31] and find \( K_u \simeq 8.1 \times 10^5 \) J/m\(^3\) for \( x = 0.88 \). But their work also illustrates how sensitively \( K_u \) reacts to composition changes. Note that the value of \( M_s \) deduced for the present samples is close to the one reported in Ref. [31] for \( x = 0.895 \), for which \( K_u \simeq 5.9 \times 10^5 \) J/m\(^3\), hinting at a slight departure from the nominal concentration in our sample. This is further confirmed by an analysis of the domain size. Indeed, our data yield \( w = 115 \) nm, which is rather close to our experimental result (within \( \pm 10\% \)). Interestingly, using the aforementioned Co\(_{88}\)Tb\(_{12}\) literature value as an input would result in much too large domain sizes (beyond 200 nm), which has further been cross-checked with the analytical approach by Kooy and Enz \[31,49\] yielding \( w = 134 \) nm.

Finally, \( K_u \) also allows us to calculate the domain wall width. For the case of an isolated wall, we obtain \( d = \pi \sqrt{A/\kappa} \simeq 14 \) nm, which is less than half the experimental value and highlights the need to fully model the stripe structure of the thin film. In contrast, our approach yields \( d = 21 \) nm at room temperature. While this is much closer to the experimental data, it still underestimates the measured width by almost 35\% (which is only a lower bound, we expect our fits to slightly underestimate the true domain wall size, as discussed in an earlier section of this paper). However, it must be kept in mind that the present model has no adjustable fit parameter and relies on a variety of approximations that deserve to be critically discussed: First, several values used as an input to our calculations are prone to large errors. This especially holds true for the exchange stiffness, which directly impacts the energy of the domain wall (Appendix D). Note that literature exchange stiffness values in CoTb alloys show a rather large spread [31,50], \( 0.6 \times 10^{-11} \) A/m \(< A < 1.4 \times 10^{-11} \) A/m. Second, we emphasize that the value of \( d \), as determined in the present work, is only identical with the domain wall size in a thin film with an ideal stripe pattern, i.e., if the system is homogeneous along \( z \). This can become an issue in magnetic layers where the projection of \( M \) along \( z \) changes as a function of the thin-film depth. A stress-induced anisotropy reduction at the interface for example (further enhanced by temperature gradients and differences in thermal expansion coefficients) could give rise to flux closure caps, inducing
an “artificial” increase of \( d \). In addition, our determination of \( d \) from the XRMS data is based on the assumption of a simple linear wall profile, which is certainly a rather crude approximation. Finally, static heating of the thin film might lead to a working temperature exceeding room temperature by several tens of K, yielding larger domain wall widths as well as smaller domains.

Keeping these limitations in mind, we can eventually attempt to link the deposited energy in the lattice and the resulting temperature rise to the anisotropy and domain wall size change. As shown in Fig. 8, a temperature increase of 145 K, as calculated in an earlier part of this paper, results in an anisotropy reduction \( \Delta K_u = -2.2 \times 10^5 \text{ J/m}^3 \) and a domain wall size change of \( \Delta d = 10 \text{ nm} \). While it compares well with our experimental data, this result has to be examined with care though, considering the highly nonlinear evolution of \( d \) with \( K_u \). An identical anisotropy change from \( 4 \times 10^5 \) to \( 1.8 \times 10^5 \text{ J/m}^3 \), for example, would give rise to an absolute change more than twice as large. This problem can be circumvented by taking a closer look at the functional dependency of \( d(K_u) \) and by focusing on relative, instead of absolute, domain width changes. The isolated wall as well as the stripe pattern wall widths exhibit similar power-law behaviors \( d \propto K_u^\alpha \). The exponent \( \alpha \) equals \(-0.5\) for the simple Bloch wall and we find \( \alpha = -0.7 \) using Virot’s model. This allows us to write ratios of domain wall sizes as a simple function of the ratio of \( K_u \) values and to avoid the use of parameters prone to large experimental uncertainties. Using \( d_{\text{max}} = d_i(K_{\text{uni}}/K_u)^{\alpha} \), where \( d_{\text{max}} \) is the maximum domain wall width obtained for the maximum laser-induced anisotropy decrease, we take \( K_{\text{uni}} = 5.1 \times 10^5 \text{ J/m}^3 \) and the domain wall values obtained from our XRMS experiment to calculate an anisotropy decrease \( \Delta K_u = -2.5 \pm 0.3 \times 10^5 \text{ J/m}^3 \) and \( \Delta K_u = -2.0 \pm 0.2 \times 10^5 \text{ J/m}^3 \) for the two different wall types. This agrees with our data and provides additional evidence for an anisotropy-mediated domain wall increase.

3. Characteristic timescales

We close this section with some brief remarks concerning the various timescales linked to the PMA decrease observed in our experiments. It is interesting to compare the time lapse before the onset of the domain wall broadening with the literature data. Zusin et al. [23] report on a domain wall size increase setting in approximately 10 ps after the pump pulse, which they trace back to delayed thermal diffusion through the sample thickness and a change of \( K_u \). Based on the three-temperature model, they provide an estimation of the time constant for heat transfer between the electronic and spin system equal to roughly 5 ps. However, we believe that this characteristic timescale does not help in explaining the present process. In fact, the DW width changes as a consequence of a reduction of anisotropy. It is thus not an increase of the spin bath temperature which triggers the observed broadening (a strain-induced modification of \( K_u \) would, for example, result in a similar DW width change, without requiring any temperature change). At first sight, it appears thus surprising to observe such long delays after the pump-pulse absorption considering that lattice heating can be achieved on much shorter timescales [1]. A possible explanation could be provided by finite spin reorientation times within the domain wall itself. Indeed, this process will not take place instantaneously, but might require several ps, considering the typical propagation speed of spin waves.

A second relevant quantity that can be extracted from our analysis is the time required for the domain wall increase to saturate (\( \Delta t \approx 20 \text{ ps} \)), which corresponds to energy transfer to the lattice degrees of freedom and eventual equilibration along \( z \). In fact, this process will be accompanied by the creation of a strain wave propagating in a direction perpendicular to the thin-film surface. Using the speed of sound of Co as an approximation for the present system [51], we calculate \( \Delta t = 2h/v \approx 21 \text{ ps} \), for the back and forth propagation of the latter through the entire film. This is compatible with our experimental observation, and it would be interesting to study the effect for various film thickness values.

Finally, we can link our experimentally accessible time window to the observed domain size changes in order to calculate DW velocities. In contrast to Zusin et al., who observe a fast increase of the magnetic domain size \( w \) setting in simultaneously with a lattice heating-induced domain wall broadening [23] (\( \Delta t \approx 10 \text{ ps} \)), we only find, as already mentioned, a small reduction of 0.8% of the initial \( w \) value after 120 ps. Note that a decrease of \( w \) as a consequence of a reduction of \( K_u \) is what is predicted by our analytical modeling of the magnetic thin-film configuration [48]. Assuming a homogeneous domain size change [15], which is supported by the absence of any variation of \( \sigma \), we can deduce a maximum domain wall velocity \( \nu_{\text{DW}} \approx 1.3 \times 10^3 \text{ m/s} \). This is two orders of magnitude faster than current-induced DW velocities that have been attained in Co-Tb systems so far [52,53].

IV. CONCLUSION

In this paper, we have shown how TR-XRMS can be used to study the impact of optical femtosecond pulses on the magnetic properties of amorphous \text{Co}_{88}\text{Tb}_{12} thin films exhibiting stripe domains. Our results unravel characteristic demagnetization times that are significantly smaller than what would be expected for a homogeneously magnetized thin film. This has been observed before in similar systems with large PMA exhibiting nanometer-sized domains, and it was surmised that superdiffusive spin currents might be responsible for these accelerated magnetization transients. Our present data challenge this interpretation [24]. Indeed, such currents would give rise to a subpicosecond broadening of the domain walls, while our analysis unequivocally shows that the domain wall width of the thin film remains unaffected up to \( \approx 4 \) ps. On longer timescales, progressive energy transfer to the lattice degrees of freedom results in a successive reduction of the uniaxial anisotropy. This eventually leads to a significant increase of the domain wall width, saturating after roughly 20 ps, the time needed by the system for full phonon equilibration through the entire thin film.

The present results are at odds with recent work, where an ultrafast shift of the scattering peaks was observed [15,23,32]. No such modifications could be seen in our experiments. However, as pointed out in earlier studies, this effect seems to be highly nonlinear and depends sensitively on the pump
fluence, i.e., the maximum demagnetization [15]. This highlights the need for further exploration of the experimental parameter space to provide conclusive quantitative results and understand whether or not the observed shifts can be traced back to a transient domain size dilation. Finally, we stress that the large discrepancy between our data and measurements on CoTb thin films with almost identical composition performed at different edges [25,32] raises central questions concerning a possible impact of the probe energy on the ultrafast magnetic response of the system. Addressing this issue systematically could provide additional useful evidence and help to shed light on the microscopic mechanisms underlying ultrafast demagnetization.

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APPENDIX A: THREE-TEMPERATURE MODEL

The three-temperature model has been extensively discussed in the literature and shall not be reviewed here. We follow the approach given in Refs. [12,24,54,55]. Assuming that the laser excitation triggers an instantaneous increase of the electron temperature and further neglecting the specific heat of the spin system, one can derive the following analytical expression to describe the demagnetization process:

\[
\frac{\Delta M}{M(0)} = \left[\frac{A_1}{\sqrt{\Delta t/\tau_0}} - \frac{(A_2 - A_1)\tau_E}{\tau_E - \tau_M}\right] e^{-\Delta t/\tau_M} \left[\frac{\tau_M}{\tau_E - \tau_M}ight] e^{-\Delta t/\tau_E} \theta(\Delta t) \Gamma(\Delta t).
\]

(A1)

Here, \(A_1\) represents the amplitude of the partial recovery once electrons, spins, and lattice have reached thermal equilibrium, \(A_2\) describes the initial magnetization quenching, \(\tau_M\) is the time constant of this quenching, \(\tau_E\) is the characteristic time of the partial recovery of the magnetization, and \(\tau_0\) is a characteristic time describing cooling by heat diffusion. \(\theta(\Delta t)\) is the Heaviside function, used to ensure causality. Convolution with a Gaussian function \(\Gamma(\Delta t)\) takes into consideration the finite pulse width.

APPENDIX B: TRANSLATING CCD DATA INTO RECIPROCAL SPACE

As described in the main text, the magnetic domains act as a grating for the incoming XUV beam, giving rise to marked diffraction intensity maxima on the detector. These peaks occur at angles satisfying the equation \(n\lambda = \Lambda \sin(\theta) = \Lambda \sin[\arctan(x_0/D)]\), with \(n\) being the diffraction order, \(\lambda\) the wavelength of the incoming light, and \(x_0\) the position of the peak on the CCD. To obtain an accurate estimation of the camera-sample distance \(D\), we used static XRMS data gathered at the Co \(M_{2,3}\) and Tb \(O_1\) edges. This allows us to calculate \(D = 5.9\) cm. Data in reciprocal space are then obtained using \(q = \frac{2\pi}{\lambda} \sin[\arctan(x/D)]\).

APPENDIX C: ONE-DIMENSIONAL MODEL FOR ANALYSIS OF THE SCATTERING PATTERN

The diffraction pattern can be obtained via Fourier transformation of the transmission function of the sample. The latter can be seen as a one-dimensional (1D) periodic object consisting of \(N\) repetitions of a basic magnetic unit cell (Fig. 9) with size \(\Lambda\). The intensity transmitted through the sample depends on the refractive index which can be written as a function of the magnetization \(M(x)\): \(n(x) = 1 - [\delta_0 - \delta_1 M(x)] + [\delta_0 - \beta_1 M(x)]\). Using \(t(x) \propto e^{i\pi n(x)}\), where \(h\) represents the thin-film thickness, we obtain after Taylor expansion \(t(x) \propto t_0 + t_1 M(x)\), where \(t_0\) and \(t_1\) are constants. The transmission function is thus, up to a constant, proportional to the projection of the magnetic profile of the sample. As shown in Fig. 10, we use a linear approximation to describe \(M_{2,3}(x)\) [which, for simplicity, will be termed \(M(x)\) in the following]. Considering the periodicity of the 1D magnetic structure, the latter can be written as the convolution of the magnetic unit cell and delta peaks with periodicity \(\Lambda\),

\[
M(x) = M_{uc}(x) \ast \sum \delta(x - n\Lambda).
\]

(C1)

In reciprocal space, the Fourier transform of \(M(x)\) thus equals

\[
M(q) = M_{uc}(q) \ast \sum \delta(q - \frac{2\pi m}{\Lambda})
\]

(C2)

in the limit \(N \to \infty\). Considering that

\[
\int_{-\Lambda/2}^{\Lambda/2} dx\, M(x) \sin\left(\frac{n\pi x}{w}\right) = -M_{uc} \frac{8w^2}{\pi} \sin\left(\frac{n\pi d}{2w}\right)
\]

(C3)

we eventually obtain the following expression for the third- and first-order integrated peak intensities,

\[
I_3/I_1 = \left(\frac{M_{uc,n=1}}{M_{uc,n=3}}\right)^2 = \frac{1}{81} \sin^2(3\pi \eta/2)
\]

(C4)

with \(\eta = d/w\), the ratio of domain wall width and domain size.
The magnetostatic energy per unit volume is equal to
\[
e_{ms} = \frac{\mu_0 W}{\pi h} \sum_{k \text{ odd}} |C_k|^2 \frac{1}{k} \left[ 1 - e^{-\pi k h/w} \right],
\]
with Fourier coefficients
\[
C_k = \frac{2M_s}{k^2 \sin \left( \frac{k \pi d}{2w} \right)}.
\]

The exchange contribution equals
\[
e_A = \frac{\pi^2 A}{d w},
\]
while the anisotropy energy density is written as
\[
e_K = \sum_i \frac{1}{2w} \int_0^{2w} K_u(i) \cos[\theta(x)]^2 dx,
\]
where \(\theta(x)\) describes the angle between the local magnetization and the y axis, changing linearly along the domain wall width (see Fig. 10). In their paper, Virot et al. only consider \(i = 1\). We additionally take into consideration the next-order term (\(i = 2\)). However, considering \(K_{u2}\) to be smaller than \(K_{u1}\), the original first-order result of Virot et al., \(e_K = \frac{K_u d}{2w}\), can still be used with \(K_u = K_{u1} + K_{u2}\). In the present case, it represents a reasonable approximation to the anisotropy energy density (less than 6% relative error for \(K_{u2} < K_{u1}/3\)). Using the aforementioned energy contributions, \(e_{tot}\) is obtained by numerical minimization of Eq. (3) with respect to \(w\) and \(d\). This eventually allows us to obtain the equilibrium values \(w(K), d(K)\) shown in Fig. 7. Note that the calculation of \(e_K\) requires knowledge of \(A\), the exchange stiffness of the system. We calculated this quantity via [56]
\[
A = \sum_{i,j} 2|J_{ij}| P_{ij} S_i S_j / a_{ij}.
\]
Here, the two sums are taken over the atomic species, Co and Tb, respectively. The \(J_{ij}\) represent the exchange integrals (\(J_{CoCo} = 2.1 \times 10^{-21} J\), \(J_{CoTb} = -2.4 \times 10^{-22} J\), and \(J_{TbTb} = 0.2 \times 10^{-22} J\) [57]). \(P_{ij}\) corresponds to the probability of having a given atomic pair \(ij\) and can thus be linked to the concentration (considering that the alloy is randomly mixed), \(S_i\) is the average spin value of species \(i\) \((S_{Co} = 0.73\) and \(S_{Tb} = 5.05\) [57]), while \(a_{ij}\) denotes the average interatomic distances between atoms of type \(i\) and \(j\) \((a_{CoCo} = 2.5\ \text{Å}, a_{CoTb} = 3.0\ \text{Å}, \text{and } a_{TbTb} = 3.5\ \text{Å})\). With these data, we obtain \(A \simeq 1.0 \times 10^{-11} J/m\).

APPENDIX D: ANALYTICAL DESCRIPTION OF MAGNETIC STRIPE STRUCTURES

The creation of magnetic stripe structures has initially been treated by Kittel [36]. However, his model is limited to the description of systems, where the domain wall width can be neglected, when compared to the domain size \((d \ll w)\) and where the domain size is much smaller than the film thickness. This does not hold in our CoTb thin films. In the present work, we thus stick to the sine wave model (SWM) proposed by Virot et al., which permits us to circumvent these problems [48]. The total energy of the thin film is written as a sum of magnetostatic, anisotropy, and exchange contributions,
\[
e_{tot} = e_{ms} + e_K + e_A.
\]

FIG. 10. (a) One-dimensional spin chain with domains of size \(w\) and Bloch walls (width \(d\)) and (b) linear approximation used to describe the normalized \(z\) component of the magnetization \(M_z\). (c) Total magnetic energy density of the striped thin film as a function of anisotropy (gray solid line). The magnetostatic contribution \(\frac{1}{2} \mu_0 M^2_c\) is shown as a red dashed line. For \(Q = \frac{2x}{w \cos^2 \theta} > 1\), the equilibrium magnetization will point in the out-of-plane direction, irrespective of the thin-film thickness.

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where \(\theta(x)\) describes the angle between the local magnetization and the y axis, changing linearly along the domain wall width (see Fig. 10). In their paper, Virot et al. only consider \(i = 1\). We additionally take into consideration the next-order term (\(i = 2\)). However, considering \(K_{u2}\) to be smaller than \(K_{u1}\), the original first-order result of Virot et al., \(e_K = \frac{K_u d}{2w}\), can still be used with \(K_u = K_{u1} + K_{u2}\). In the present case, it represents a reasonable approximation to the anisotropy energy density (less than 6% relative error for \(K_{u2} < K_{u1}/3\)). Using the aforementioned energy contributions, \(e_{tot}\) is obtained by numerical minimization of Eq. (3) with respect to \(w\) and \(d\). This eventually allows us to obtain the equilibrium values \(w(K), d(K)\) shown in Fig. 7. Note that the calculation of \(e_K\) requires knowledge of \(A\), the exchange stiffness of the system. We calculated this quantity via [56]
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