

## Microstructure scale modelling of the WC and Co phases plastic behaviour in the WC-Co composite with different cobalt contents and for different temperatures. Comparison of the Drucker-Prager and Mises models

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1	Microstructure scale modelling of the WC and Co phases plastic behaviour in the WC-Co
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3	Drucker Prager and Mises models
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9	Abstract

Despite several years of research and development works, the understanding of the tungsten carbide 10 11 (WC-Co) behaviour under complex thermomechanical loading is not yet complete. Indeed, data is quite 12 rare for the elevated temperatures encountered in the various applications and makes the description of 13 this material a difficult task. In the present work, the elastoplastic behaviour of various grades of WC-14 Co composites are simulated numerically from room temperature up to 900°C thanks to the creation of realistic microstructures. This microstructure-level model allows to determine the representative volume 15 element (RVE) considering the two phases tungsten carbide (WC) and cobalt (Co) to reproduce the real 16 macroscopic behaviour of the composite under compression loading. The elastoplastic behaviour of the 17 18 Co phase has been identified from the literature and the yield criterion of WC phase estimated at different 19 temperatures by the introduction and determination of two temperature functions  $\alpha_1(T)$  and  $\alpha_2(T)$ . These two functions represent the dependence of the yield stress and hardening, respectively. A 20 21 comparison between the von Mises and Drucker Prager criteria applied to the WC phase has been also 22 discussed. A good agreement is obtained between the numerical simulation results and experimental 23 data.

Keywords: WC-Co hard metal, Microstructure model, Plastic deformation, Temperature dependent
behaviour, Finite element analysis.

26

## **1. Introduction**

Tungsten carbide (WC) is the main material used for more than 70% of cutting tools and tooling materials due to its high hardness, mechanical strength and abrasion resistance [1]. WC-Co cemented carbides are the most common basic composition for cutting tools. Almost 95 years after the first Schroter's WC-Co composite having low porosity and good toughness [2], this material has been extensively developed to respond to industrial needs, and has resulted in all the grades known today. The high mechanical and thermal performance of WC-Co are the result of a combination of ductile

- Cobalt (Co) binder and hard-brittle carbide (WC) grains [3–5] which is sintered around 1400°C [2].
- 35 Thus, the mechanical properties depend on many parameters such as the increase in hardness as the
- 36 WC grain size and the weight percentage of Co (wt.%) decrease. In general, the WC grain size of
- 37 ranges from 0.5 to  $2 \mu m$  with a cobalt weight percentage ranging from 5 to 16% [6]. However, for
- 38 some specific applications, such as the machining of metals or hard superalloys for example, the
- 39 percentage by weight of cobalt is most of the time lower than 10%, according to the literature.
- Many researches and development works mainly experimental have been conducted on the whole the 40 supply chain of the initial WC-Co tool, from their manufacturing process to their breakdown (the end 41 of their lifetime) [7-9]. Several authors have been particularly interested in behaviour of these WC-Co 42 tools under extreme thermal and mechanical loadings [10-12] encountered in machining. For instance, 43 in the investigation led by Davies et al. [13], a temperature of 1000°C along the tool-chip contact was 44 achieved due to an intense friction during the machining of the AISI 1045 steel with a cutting speed of 45  $605 m.min^{-1}$  and uncut chip thicknesses of 133  $\mu$ m. In addition, a temperature gradient in the tool 46 was observed especially from the tool tip to the end of the tool-chip contact and also to the center of 47 48 the tool where the temperature decreases. Many studies have been carried out on the WC-Co 49 behaviour under large range of temperatures between 25 °C and 1000°C. Ueda et al. [11] and Emani 50 et al. [14] identified three main temperature ranges where the WC/Co carbide tool exhibits different mechanical behaviours. In the range of 25 °C to 527 °C, Mari [15] observed a brittle and elastic WC-51 52 Co behaviour explained by the multiple intersections of stacking faults in the cobalt phase blocking the crystal lattice and inhibiting any movement [16]. From 527 °C to 827 °C, an increase of toughness 53 induced by the softening of cobalt with a limited plastic deformation were observed. For temperatures 54 55 over 827 °C and below 1000°C, the sliding of the WC grain boundaries is one of the mechanisms involving the softening of WC-Co subjected to larger plastic deformations. 56
- In parallel with the experimental studies, the numerical simulation approach was also used to analyse the contribution of each phase in the mechanical behaviour of WC-Co at the microstructure scale. This work can be classified into two groups. The first group concerns the simulation of damaged WC-Co [17, 18]. The second one models the elasto-plastic behaviour of WC-Co prior to damage and on which the present study focuses. Without being exhaustive, some significant studies of this second group are recalled in the following, before introducing the subject of this paper.
- 63 In 1972 Jaensson et *al.* [19] proposed the first finite element simulations to compute the Young's
- 64 modulus and Poisson's ratio of the WC-Co composite from 2D representative volume elements (RVE).
- 65 These RVE were created from realistic microstructures composed of 20-30 carbides grains. Each
- 66 phase has an elastic behaviour. A good agreement between experimental data and simulation results
- 67 for different percentages of cobalt (1-30wt.%) was found. Thereafter, this work was extended by
- 68 Sundstrom [20] to simulate the elasto-plastic behaviour of the composite in compression. Elasto-

plastic and elastic models were used for cobalt and WC, respectively. The results revealed that the 69 plastic deformations are possible in the cobalt binder despite the presence of WC hard matrix phase. In 70 71 addition, local plastic strains can reach twice times the value of the effective plastic strain. Twenty 72 years later, Poech et al. [21] evaluated the possible impact of the microstructural parameters such as 73 the shape and arrangement of the binder phase on the elasto-plastic behaviour of the WC-Co. The 74 results show that these parameters have a slight influence on the strain-stress curves. The authors 75 analysed the effect of the mesh geometry, mesh density and model size on the results. They showed that the yield stress of the composite decreases to a constant value for the densest meshes. Later, and 76 77 thanks to more computing power, Sadowski et al. [22] performed numerical simulations on several 78 sizes of representative surface features (RSE) or 2D RVE much larger than those used in previous 79 works. They contain many grains (>120 grains for a RSE size of  $10x10 \mu m$ ) and are created from real 80 microstructures. The best fit to the experimental data was obtained with the largest RSE (40x40  $\mu m$ ) under conditions of generalized plane strain. In a continuation of previous work, Chen et al. [23] 81 82 proposed a statistical method for defining the minimum size of the 2D representative volume element 83 of the WC-Co alloy and found that the RVE for a plastic study must be larger than that for an elastic study. The mean value of each parameter considered as the effective elastic constants or the 84 85 anisotropic parameter converge from a RVE size of  $30x30 \ \mu m$  but their respective standard deviation 86 decreases further. From the obtained results, a RVE size of  $40x40 \ \mu m$  is recommended by the authors. 87 However, in the previous studies, the compression of the WC-Co is limited to strains lower than 0.6%. According to Poech et al. [21], after the initial plasticity of the composite, it is necessary to consider 88 both the plastic and damage processes in the carbide phase. Tkalich et al. [24] proposed to simulate 89 90 only the plasticity of the carbide with Drucker-Prager's isotropic model. This model is able to 91 reproduce the difference in strength of the WC material under compression and tension. In their work, 92 the elasto-plastic behaviour of the composite was simulated using a 2D RVE based on realistic 93 microstructures and under generalized strain plane conditions. The decrease in strain rate after initial 94 plasticity, often observed in the literature, is well reproduced. The authors then extended their model in another study [25] to an idealized 3D RVE created from an algorithm based on Voronoi cells. 95 96 Several complex mechanical loads were applied on this RVE to estimate the shape of the initial 97 elasticity surface of different WC-Co composites which is similar to a Drucker-Prager surface with a 98 cap. However, for all numerical studies presented in this introduction, the simulations were performed 99 at room temperature. As mentioned above, the WC-Co cutting tool is subjected to high temperatures 100 up to 1000°C, which can change the mechanical behaviour of the composite. Recently, Faksa et al. 101 [26] simulated the elasto-plastic behaviour of the WC-6wt.%Co composite in compression for the 102 temperature range of 20 to 900 °C using a 2D RVE. Due to a lack of data, the pure Co was substituted 103 by a cobalt alloy. The first results of the study showed that only the elasto-plastic behaviour of Co is 104 insufficient to represent the plasticity of the composite for strains above 0.6% in the case of elastic 105 WC behaviour. Therefore, a plastic behaviour was assumed for the WC phase. The stress-strain curves

- of the WC are inversely reconstructed from the composite behaviour. However, this study is limited toWC-6wt.%Co composite.
- 108 This state of the art reveals the need to clarify the different behaviours of the tungsten carbide phase
- 109 used in the literature. Although data on the elasto-plastic behaviour of WC are scarce, it is possible to
- identify it by an inverse approach similar to that adopted by Faksa et *al.* [26] with a pure cobalt phase.
- 111 Finally, a finite element analysis of the elasto-plastic behaviour of WC-Co hard metal at the
- 112 microstructural scale needs to be developed for different temperatures and cobalt contents. These
- shortcomings, mentioned above, are the subject of the present study.
- 114 This paper is structured as follow:
- 115 In Section 2, the elasto-plastic models to simulate the behaviour of the cobalt and WC phases are
- 116 presented. For the carbide phase, the von Mises and Drucker Prager criteria used in the work of
- 117 Tkalich et *al.* [24, 25] are proposed but only at room temperature. Then, in Section 3, an algorithm to
- 118 generate idealized WC-Co microstructures is described. The advantage of this strategy is to control the
- 119 cobalt content and the number of WC grains. In Section 4, a study is carried out to establish the
- 120 number of WC grains necessary to build an RVE for the elasto-plastic behaviour of the composite at
- 121 room temperature. Then, in Section 5, a temperature-dependent hardening law for the WC phase is
- determined from the behaviour of the composite WC-6 wt.%Co and the pure cobalt. The model is
- tested for a WC-10.5wt.% Co composite in uniaxial compression and the results are compared with
- 124 literature data. Finally, a comparison between the von Mises and Drucker-Prager criteria applied to the
- 125 WC phase is carried out. Some conclusions from this study are then given.
- 126 **2.** Modelling of the Co and WC phases behaviour
- 127 The modelling of the WC-Co elastoplastic behaviour at the microstructure scale requires suitable128 behaviour models dedicated to the Co and WC phases.
- 129 **2.1 Elastic behaviour**
- The ductile phase of the cobalt is polycrystalline with a crystallite size of 3 times larger than that of the WC grains [27]. Its elastic behaviour is assumed to be isotropic. The Young's modulus and thermal expansion as a function of the temperature are taken from data given by Betteridge in [28] and Fine and Ellis in [29], see Figure 1. The Poisson's ratio is taken equal to 0.31 from the work of Poech et *al.* [21] since Teppernegg et *al.* [30] have shown its insensitivity to the temperature evolution.
- 135 The WC phase consists of several grains. Each grain has a transversely isotropic elastic behaviour due
- to its hexagonal crystal structure. However, most studies in literature [31, 32] using microstructural
- 137 simulations of the WC-Co composite assume that each grain has the isotropic elastic behaviour of the
- 138 polycrystal WC. This hypothesis is also chosen in the present study. The Young's modulus and

thermal expansion as a function of temperature are given in Figure 2 and are taken from [21] and [33].The Poisson's ratio taken insensitive to the temperature is equal to 0.194 [21].

### 141 **2.2 Plastic Model**

142 In this section, the elasto-plastic model for the cobalt is presented. As mentioned in Introduction, in

the models, the plasticity of the composite is mainly due to the plasticity of the cobalt phase, whereas

the WC phase is often considered as an elastic medium. However, some authors [24, 26] assumed an

elasto-plastic behaviour of the WC phase justified in the literature by the presence of slip marks

- observed in WC grains [34–36] or by a disorientation of WC grains observed in a deformed WC-
- 147 6wt.%Co sample indicating some extension of plastic deformation [26]. Two elasto-plastic models of

the WC used by these authors are also introduced in the following and will be compared and discussedlater in this paper.

## 150 2.2.1 von Mises criterion for Cobalt and WC phases

The von Mises criterion usually used for metallic materials is adopted here for the cobalt phase. In a first approach, von Mises criterion can be transposed to the carbide phase. Faksa et *al.* [26] also adopted a plastic behaviour for both phases in ABAQUS software [37] that is based on the von Mises criterion. In the elasto-plastic regime of a phase "*i*" (i = carbide phase WC, cobalt phase  $C_o$ ), von Mises criterion is chosen to describe its yield surface which is defined by:

156 
$$f_i(\boldsymbol{\sigma}, \boldsymbol{p}) = I_2(\boldsymbol{\sigma}) - (R_i + 1)$$

$$f_i(\boldsymbol{\sigma}, p) = J_2(\boldsymbol{\sigma}) - (R_i + Y_i(p)) \tag{1}$$

157 with  $J_2(\sigma) = \sqrt{\frac{3}{2}s:s}$  the von Mises stress computed operator from  $s = \sigma - \frac{1}{3}$ trace( $\sigma$ ) the deviatoric 158 part of the stress tensor  $\sigma$ . Bold letters are used to denote vectors and tensors.  $R_i$  and  $Y_i(p)$ ,

respectively, the yield stress and the isotropic hardening with p is the accumulated plastic strain which is defined by:

$$p = \int_0^t \sqrt{\frac{2}{3}} \dot{\boldsymbol{\varepsilon}}^p : \dot{\boldsymbol{\varepsilon}}^p \, dt \tag{2}$$

162 with,  $\dot{\epsilon}^p$  the plastic strain rate tensor and ":" the double contraction operator.

163  $\dot{\varepsilon}^p$  is calculated from the following associate flow rule:

164

165

161

 $\dot{\boldsymbol{\varepsilon}}^{\boldsymbol{p}} = \dot{\lambda} \frac{\partial g_i}{\partial \sigma} \tag{3}$ 

166 with  $\dot{\lambda}$ , the plastic multiplier and  $g_i$  flow potential defined which is equal to  $f_i$  from Equation (1).

167 The term  $R_i + Y_i(p)$  describes a plastic stress-strain curve that can be obtained from a tensile or

- 168 compression test. For the Co phase, these curves were measured in compression by Park et *al.* [38] for
- different temperatures, see Figure 3, and then described by a series of points written in a table in the
- 170 ABAQUS software. The intermediate data between two points are calculated by linear interpolation.
- 171 In the case of WC (i = WC), the term  $R_{WC} + Y_{WC}(p)$  is taken from Tkalich et *al.* [24] where the
- 172 isotropic hardening  $Y_{WC}(p)$  is defined as follows:

$$Y_{WC}(p) = Q_{WC}[1 - \exp(-b_{WC}p)]$$
(4)

174 where  $Q_{WC}$  and  $b_{WC}$  are the hardening constants. The values of parameters Rwc = 4000 MPa,

175 Qwc = 3000 MPa and bwc = 10 are given for a uniaxial compression loading of the WC.

## **176 2.2.2 Drucker Prager criterion for the carbide WC phase**

Tkalich et al. [24] used the Drucker Prager model [39] for the WC phase initially developed for soil 177 mechanics. Thanks to its dependence on pressure, this model can reproduce the difference in 178 behaviour between tension and compression. This difference is highlighted by the experiments carried 179 out by Doi et al. [40] where tensile tests not exceed 0.7% of deformation and a maximal tensile stress 180 181 of 210 MPa while compression tests reach the maximum of 4% of deformation and a maximal compressive stress of 335 MPa for a WC-20wt.% Co with a WC grain size of 2.1 µm. In the present 182 work, this criterion, already implemented in ABAQUS code, is also adopted for the carbide phase to 183 184 compare it with the von Mises criterion presented above.

## 185 The Drucker Prager criterion is defined as follows:

186

173

$$f_{WC}(\boldsymbol{\sigma}, p) = \sigma_{eq} - (R_{WC} + Y_{WC}(p))$$
(5)

187 where the equivalent stress is  $\sigma_{eq} = \frac{I_2(\sigma) + I_1(\sigma) \tan(\phi_{WC})/3}{1 - \tan(\phi_{WC})/3}$  with  $I_1(\sigma) = \operatorname{trace}(\sigma)$  is the stress tensor 188 trace and  $\phi_{WC}$ , the friction angle that is set to 45°, implying that the yield stress in uniaxial tension is 189 half as large as in compression [24]. In Equation (5), the term  $R_{WC} + Y_{WC}(p)$  is given by Equation (4). 190 The accumulated plastic strain p which is defined by :

191 
$$p = \int_0^t \frac{\sigma \cdot \dot{\epsilon}^p}{\sigma_{eq}} dt$$
(6)

192 the plastic strain rate  $\dot{\varepsilon}^p$  is calculated from the following non-associated flow rule :

193 
$$\dot{\boldsymbol{\varepsilon}}^{\boldsymbol{p}} = \dot{\lambda} \frac{\partial g_{WC}}{\partial \sigma} \tag{7}$$

194 with  $\dot{\lambda}$ , the plastic multiplier and  $g_{WC}$  flow potential defined as :

195 
$$g_{WC}(\boldsymbol{\sigma}) = J_2(\boldsymbol{\sigma}) + \frac{1}{3}I_1(\boldsymbol{\sigma})tan(\psi_{WC})$$
(8)

196 where  $\psi_{WC}$  is the dilatation angle. In this paper an associate flow rule is considered, i.e.  $\psi_{WC} = \phi_{WC}$ .

197 In the Drucker Prager model, the hardening parameters and yield stress must be determined from a

198 stress-plastic strain curve obtained in monotonic uniaxial compression test. It is interesting to note that 199 under this loading condition, the yield function is identical for both elastoplastic models:

200 
$$f(\boldsymbol{\sigma}, p) = \left| -\sigma_{comp} \right| - R - Y(p)$$
(9)

as well as the cumulated plastic strain *p* computed as follows (see the proof in **Appendix A**):

202 
$$p = \int_0^t \left| -\dot{\varepsilon}_{comp}^p \right| dt$$

where  $\sigma_{comp} > 0$  and the  $\dot{\varepsilon}_{comp}^{p} > 0$  are the normal stress and plastic strain rate in the direction of the compression.

(10)

In the following of this study, the von Mises criterion for both phases will be used in the development of this microstructural model. The results of the model will be compared to those calculated from the von Mises and Drucker-Prager criteria applied respectively to the Co and WC behaviours in Subsection 5.4.

209

### 210 **2.3 Interfaces**

211 In the composite, two types of interfaces can be observed: WC/Co and WC/WC. In simulations

dealing with the behaviour of composites at the microstructure scale, the WC/Co interfaces are

represented geometrically. These interfaces are considered as a perfect contact because of the good

adhesion between these two phases [24, 25]. This good adhesion can be justified during sintering by a

low interfacial energy which leads to an excellent wetting of the cobalt on the WC grains [41].

216 Regarding WC/WC interfaces, Csanadi et *al.* [42] concluded from micro-bending tests that their

217 bending strength is generally lower than that of the WC grains. Sometimes, these interfaces are

represented geometrically in some models but there are considered generally as perfect [24–26]. Their

elasto-plastic models, like those presented in Subsection 2.2, are dedicated to polycrystalline materials.

220 Therefore, the influences of grain boundaries are implicitly included in the parameters of these

221 models. The WC/WC interfaces that will be represented in the present work are also considered as

- 222 perfect.
- 223

## **3.** Creation of the microstructure

Simulations are based on a geometrical representation of the microstructure. However, various
complex geometries of the WC-Co microstructure are represented in the literature. In several
investigations lead by Sadowski et *al.* [22, 32], the composite consists of polygonal WC grains
surrounded by a thin layer of cobalt. Faksa et *al.* [26] have also adopted this description in part of their
work, which is named "Co-matrix model". Nevertheless, in most representations of the WC-Co
microstructure, the WC grains are in contact to form a WC skeleton with WC/WC interfaces that are

excluded in the "Co-matrix model". The presence of such skeleton was first formulated by Dawihl and 230 Hinnüber [43], observing that the samples maintained their shape after the cobalt had been attacked by 231 232 boiling HCl. The existence of this skeleton, if any, is conditioned by the cobalt content. However, the 233 percentage of cobalt above which the skeleton is no longer obtained is not well defined. For instance, 234 Exner [3] fixed that limit to 30 wt.%Co while it is about of 11 wt.%Co for Dawihl and Hinnüber [43]. 235 In 2D observations, the cobalt phase seems to be isolated in small areas, especially when the weight 236 percentage of Co is low. Faksa et al. [26] also adopted this description which is named "WC-matrix model". According to the results of their research, this microstructural description is more appropriate 237 238 to represent the elastoplastic behaviour of the composite. However, the hypothesis of an isolated Co 239 phase is no longer necessarily true in the case where the weight percentage of Co increases. Some 240 authors have shown continuous Co skeletons on several WC-Co grades in 3D space [44]. In addition, the distribution of cobalt in the WC-Co composite is not uniform. List et al. [45] observed, on the rake 241 242 face of an uncoated carbide insert (geometry type K4, Sandvik) H13A grade (K20, 6%Co), based on a

243 SEM images, some areas rich in cobalt and others in carbide grains.

244 Due to the complexity of the WC-Co microstructure, most microstructural simulations in the literature generally use a 2D geometric representation of the microstructure generated from microscopic images. 245 246 For example, Zhu et al. [31] have structured this process in their research in six steps: noise reduction, image binarization, WC grain segmentation, WC grain boundary definition, WC grain boundary 247 248 vectorization and meshing. Recently, Jiménez-Piqué et al. [44] have reconstructed a 3D microstructure 249 from a sequence of images obtained by FIB (Focused Ion Beam Tomography). However, these studies 250 are limited by the number of micrographs and obtaining them is a long process. Alternatives are also 251 proposed in the literature where an idealized WC-Co microstructure is rapidly generated from an algorithm for a given wt.% of Co. For example Park et al. [38] proposed an algorithm to build a 2D 252 WC-Co microstructure. In their work, a single WC grain is defined by a quadrangle controlled by four 253 254 parameters: a centroid, a major axis, a minor axis and the orientation angle measured between a major 255 axis and a horizontal reference line. The values of these parameters are defined from statistical distributions determined on real microstructures. The quadrangles are randomly distributed to generate 256 a WC skeleton. The voids between the WC grains are filled by the Co phase. Kayser et al. [46] used 257 258 truncated prisms for the WC grains and generated a 2D microstructure which is extruded in the third

259 direction.

- 260 In the present paper, 2D square microstructures have been created in Matlab using the algorithm
- proposed by Tkalich et *al.* [25]. The microstructures are generated from the Voronoi cell pattern. Then
- each cell is divided into two parts by a line. Each part of the cell contains either the WC phase or the
- 263 Co binder. The temporary crossing point of this line is randomly placed on an edge of the cell. The
- line makes a randomly imposed angle  $\alpha$  with the horizontal in the interval  $[0; \pi]$ . Then, the shortest

- distance between the farthest cell vertex and the line is iteratively calculated such that the predefinedsurface fraction of the binder phase is reached with an accuracy of more than 98%.
- Finally, RVE is extruded to over 1/10 of its lateral length in the third direction as in [47] to perform a 3D computation (see Figure 4). This algorithm makes it possible to rapidly generate a large number of idealized microstructures (or RVE) with different Co contents to analyse its effect on the elasto-plastic behaviour of the composite. Nevertheless, it is necessary to define a minimum number of cells to generate RVEs that will allow to represent the elasto-plastic behaviour of the WC/Co with a good accurate. This cell number is studied in following section.
- **4. RVE determination**

274 In the literature, the RVE is often defined by the number of WC grains, although their behaviour is 275 that of a polycrystalline WC in the numerical simulations. The number of WC grains and Voronoi 276 cells are identical and controls indirectly the distribution of the cobalt phase. Thus, a large number of 277 WC grains leads to a more homogeneous distribution and smaller islets of cobalt in the microstructure, 278 as shown in Figure 5. In this work, 8 groups of microstructures comprising 5, 50, 100, 150, 200, 279 250, 275, 300 WC grains are studied for composites of WC-6wt.%Co and WC-20wt.%Co. These two compositions have been chosen to determine an RVE covering a wide range of cobalt content used in 280 281 cutting tools. For each group, 4 different microstructures have been generated. For all microstructures, 282 simulations have been performed using the finite element method implemented in the ABAOUS 283 Software [37]. Each RVE is subject to kinematic boundary conditions showed in Figure 6 to simulate 284 a uniaxial compression test. This test allows the comparison between the results of the simulation and 285 the experimental data in the literature. As shown in Figure 6, at the left, on the bottom and at the back 286 of the sides of the microstructure, displacements are fixed in the x, y and z directions, respectively. On the upper side (at the left side), a negative displacement  $-u_v(-u_x)$  is imposed to performed uniaxial 287 compression in the y (and x) directions. The remaining sides, a relationship between nodes could be 288 289 applied to impose straight sides. However, Sadowski et al. [22] compared this solution with that of 290 free sides and obtained the same results. In the present study, these sides are free. The element type 291 used is a linear prismatic element C3D6 with 6 nodes. A suitable mesh size has been selected from 292 convergence studies for each RVE. For illustrative purposes, Figure 7 shows the normalized Young's modulus and dissipated plastic energy computed with different mesh sizes on RVE of 275 grains. The 293 tested element sizes are 0.042, 0.031, 0.012, 0.007 and 0.005 of the RVE size corresponding to 3595, 294 4868, 35280, 65631 and 101418 elements. In the following of this study, the third mesh size has been 295 296 selected.

The criteria to determine the RVE are partly inspired by those proposed by Chen et *al.* [23]. The first criterion is the ratio  $E_x/E_y$  where  $E_x$  and  $E_y$  are the apparent Young's moduli of each microstructure obtained from simulations of uniaxial compression in the x and y directions, respectively. If this 300 criterion is close to one, then the microstructures are considered isotropic. In Figure 8, the averages of 301 ratio  $E_x/E_y$  for each group of microstructures are plotted as a function of the number of grains. For 302 composites containing 6 wt.%Co, this ratio is approximately equal to 1 with an error of less than 1% 303 regardless the number of grains, whereas for its counterpart containing 20wt.%Co, this error is reached from 100 grains upwards. Moreover, for all groups of microstructures larger than 100 grains, as shown 304 in Figure 8, the dispersion of this criterion in each group is low since its standard deviation is less than 305 306 0.01. A low standard deviation means that the apparent properties of the RVE are not affected by different microstructures containing the same number of grains. For microstructures with less than 307 100 grains, the standard deviation is higher because the distribution of the cobalt phase is very 308 309 heterogeneous.

- 310 The second criterion is defined as the ratio  $E_i/E_{300}$ , where  $E_i$  and  $E_{300}$  are the mean Young's moduli
- of the microstructure groups containing *i* and 300 grains, respectively. Microstructures composed of
- 312 300 grains are taken as a reference since they have the largest number of grains in this study.
- 313 Moreover, it is likely that their apparent mean Young's modulus already converges to the effective
- Young's modulus of the composite as observed by Chen et *al.* in [23]. The  $E_{300}$  values for the WC-
- 315 6wt.%Co and WC-20wt.%Co composites are 623 and 480 GPa, respectively. Figure 9 shows a
- variation of the ratio  $E_i/E_{300}$  and its standard deviation as a function of the number of grains. As for
- 317 the previous criterion, from 100 grains upwards, all ratios  $E_i/E_{300}$  are close to 1 with an error of less
- than 1% and a standard deviation of less than 0.01. In other words, the ratio converges quickly, and the
- apparent Young's modulus of the microstructures is close to the values of  $E_{300}$ . The same trends are
- also observed for Poisson's ratio and thermal expansion. However, as mentioned by Chen et *al.* in
- reference [23], the RVE defined with the elastic phases cannot be sufficient to perform a plastic study
- 322 of the composite due to the development of the overall non-linearity of the material. It is therefore
- 323 necessary to continue this study by selecting a criterion for the determination of the RVE taking into
- account the plastic behaviour of each phase.
- 325 The third criterion is the P/U ratio where P and U are respectively the average plastic energy
- dissipated and the external work, for a total deformation of 2% obtained by simulating a uniaxial
- 327 compression test. Figure 10 shows the mean value of the P/U ratio and its standard deviation as a
- function of number of grains for the two cobalt grades. The P/U ratio begins to converge towards the
- 329 value of about 0.46 and 0.38 from 200 grains for microstructures containing 6 and 20 wt.% of cobalt,
- respectively, with standard deviations less than 0.01. As suspected, the number of grains where this
- 331 criterion converges is greater than that observed in the elasticity studies.
- 332 Note that a final criterion often used in the literature to determine an RVE can also be applied. This is
- the Hill's criterion, which is independent of the mechanical behaviour under consideration. According
- to Chen et *al.* [23], this criterion can be written as follows :

335 
$$\psi = \max\left(\frac{\langle \sigma \rangle : \langle \varepsilon \rangle}{\langle \sigma : \varepsilon \rangle}, \frac{\langle \sigma : \varepsilon \rangle}{\langle \sigma \rangle : \langle \varepsilon \rangle}\right)$$
(11)

If this criterion tends towards 1, then the RVE is correctly defined. Figure 11 shows the mean value of 336

337  $\psi$  and its standard deviation as a function of the number of grains.  $\psi$  is equal to 1 for the composite

- WC-6wt.%Co while its counterpart with WC-20wt.%Co decreases to converge towards 1.16 from 250 338
- grains. For microstructures larger than 250 grains, the standard deviations of  $\psi$  for both grades are less 339 340 than 0.01.

341 According to the different criteria defined above, an RVE with a number of grain greater than 250 can

- be selected with confidence. A RVE with 275 WC grains is selected in the following. This number is 342
- 343 comparable to the one found by Chen et al. Sadowski et al. [22] for a RVE with a size of  $40x40 \mu m$
- 344 and an average tungsten carbide grain size of 2.35 µm (i.e. 290 WC grains for a cobalt-free
- 345 composite).

#### 5. Results and discussion 346

347 The RVE being defined, the numerical model is tested to validate its ability to reproduce the elastic 348 and elasto-plastic experimental behaviours of the composite.

#### 349 5.1 Elastic behaviour validation of the model

350 The validation of the elastic behaviour of the model consists in predicting the Young's moduli of composites containing 6, 10, 12 and 20 wt.% Co (0.9, 0.83, 0.8 and 0.675 WC volume fraction 351 352 respectively) and comparing them with experimental data obtained in the literature [48-51], see Figure 353 12.

354 For each composite, four quasi-realistic microstructures have been generated. The calculated 355 maximum deviation is less than 0.6%. Consequently, the error bar corresponding to the dispersion of the results of the realizations is not visible on Figure 12. A good agreement between the calculated and 356 measured Young's moduli is obtained, in particular with the data provided by Schwartzkopf and 357 358 Kieffer [48]. The numerical results are included in the scatter of the experimental data set which is of the order of about 50 GPa for the same cobalt content. The increase in Young's modulus as a function 359 360 of WC volume fraction is also well reproduced. This test was often used in the literature by Jaensson and Sundström [19], and Tkalich et al. [24] to evaluate the robustness of the model. 361

#### 362 5.2 Elastoplastic behaviour validation of the model at room temperature

363 The second validation is the reproduction of the stress-strain curve measured by Teppernegg et al. [30]

up to a total strain of 2% for a WC-6wt.%Co composite in uniaxial compression at room temperature, 364

- 365 see Figure 13. In Figure 13, the simulated stress-strain curves with the hardening parameters taken
- from the work of Tkalich et al. [24] ( $Q_{WC} = 3000 MPa$  and  $b_{WC} = 10$ ) reproduce the experimental 366

- 367 data up to 0.5% strain. Beyond this deformation, the hardening of the composite calculated by the
- model is lower than that observed on the experimental curve. The stress is underestimated up to 33%
- 369 of the measured value for a 2% deformation. The hardening parameters used do not seem adequate to
- reproduce the experimental data. However, the stress-strain curves of the composite depend on the
- WC grain size [40]. The experimental curves measured by Teppernegg et *al.*, used as a reference for
- this study, were measured on composites with a grain size of about  $1\mu m$ . Therefore, the hardening
- parameters  $Q_{WC}$  and  $b_{WC}$  of the carbide phase must be redefined so that the simulated curve
- 374 corresponds to that measured on the composite knowing that the elastoplastic behaviour of cobalt is

already defined. Although the WC grain size effect on the composite is beyond the scope of the

- 376 present paper, this one would be considered by Hall-Petch type relationships in the elasto-plastic
- models [52, 53]. Indeed, this size cannot be considered using the geometry of the microstructure
- generated in Section 3 because the models are based on the continuum mechanics theory insensitive to
- the absolute size, [21].

- 380 The first parameter  $Q_{WC}$  represents the difference between the maximal compressive stress that the
- WC phase can achieve and its compressive yield stress  $R_{WC}$ . If  $Q_{WC}$  is zero, the material is perfectly
- 382 plastic. The second parameter  $b_{WC}$  controls the growth rate of the stress in the elastoplastic regime of
- the WC. These parameters, despite of the presence of the cobalt, seems to have the same influence on
- the composite behaviour. Indeed, when only  $Q_{WC}$  increase up to 6000 MPa with  $b_{WC} = 10$ , the stress
- of the composite rises from 3925 MPa to 4200 MPa for strain of 2%, see Figure 13. If  $b_{WC}$  is
- multiplied by 50, the stress increases rapidly. For a strain of 1%, the slope of the curve for  $b_{WC} = 500$
- is equal to 2520 MPa/% versus 570 MPa/% for  $b_{WC} = 10$ . The combination  $Q_{WC} = 3000 MPa$  and
- 388  $b_{WC} = 500$  has been found by trial and error to be in good agreement with the experimental
- counterpart and will be use in the following of this paper. By comparison with the values of  $Q_{WC}$  and
- 390  $b_{WC}$  proposed by Tkalich et *al.* [24, 25], only the last parameter changes.
- 391 In conclusion of this section, the mechanical behaviour of the composite can be represented from these
- 392 phases and especially from the carbide phase which is fully defined at room temperature. The stress-
- 393 strain curves of Co and WC are the lower and upper limits, respectively, of the composite behaviour as
- shown in Figure 14. If both phases are considered elastic, this assumption is valid for deformations of
- less than 0.4% as shown in the WCECoE curve (WC elastic; Co elastic). In the case where only cobalt
- has an elasto-plastic behaviour (see the WCECoP (WC elastic; Co plastic) curve in Figure 14) as in
- the studies of several authors [19, 21, 32, 40], this model is valid up to deformations of 0.6%. Beyond
- this deformation, the plasticity of the cobalt in the model is no longer sufficient to reproduce the
- 399 experimental curve of the composite. This observation shared by Faksa et *al.* [26] led the authors to
- 400 introduce the plasticity of the carbide. Poech et *al.* [21], indicated that it is necessary to take into
- 401 account the plasticity and/or damage processes in the carbide phase after the initial plasticity of the
- 402 composite. However, according to the results of Tkalich et *al.* [24], plasticity is activated in the WC

- 403 phase well after that of cobalt in the composite due to the lower yield stress of cobalt. This tendency is
- also observed in the present model because the curve considering the plasticity of the two phases
- 405 (WC-CoP) merges with the WCECoP curve before a deformation of 0.6%. Finally, the WC-CoP
- 406 deformation curve reproduces the response of the WC-Co composite under uniaxial compressive
- 407 loading up to 2% deformation.

## 408 **5.3** Simulation of the composite at different temperatures

So far, simulations previously carried out have been limited to room temperature. As presented in the
 introduction, the composite WC-Co used in cutting tools are subjected to different temperatures during

411 machining. Therefore, the effect of temperature must be taken into account in this modelling. The

412 Young's modulus and the thermal expansion of Co and WC are already dependent on temperature as

- 413 well as the elastoplastic behaviour of the Cobalt phase, see Section 2. In order to complete the present
- 414 modelling, it is necessary to have compressive stress-strain curves of the WC for different

temperatures which are scare in the literature. To overcome this obstacle, a strategy similar to that

416 proposed by Faksa et al. [26] was adopted by reconstructing the WC behaviour from Co and a

- 417 composite WC-6wt.%Co. For the composite, the compressive stress-strain curves were measured by
- Teppernegg et *al.* [30] up to 2% strain at temperatures of 25, 200, 400, 600, 800 and 900°C, see Figure
  16.

In order to take temperature into account in the plastic regime of the carbide phase, the followingmodification of the yield criterion was introduced :

422

$$f_{WC}(\boldsymbol{\sigma}, \boldsymbol{p}, T) = \sigma_{eq} - R_{WC}(T) - \alpha_2(T)Y_{WC}(\boldsymbol{p})$$
(12)

423 with  $R_{wc}(T)$  defined as following :

424

$$R_{wc}(T) = \alpha_1(T)R_{wc}(T = 25^{\circ})$$
(13)

425  $\alpha_1(T)$  and  $\alpha_2(T)$  control the temperature dependence of the yield stress  $R_{wc}(T)$  and the isotropic 426 hardening of the WC material, respectively. Note that for  $T = 25^{\circ}C$ ,  $\alpha_1 = \alpha_2 = 1$ . This modification 427 is valid for both von Mises and Drucker Prager criteria since their compressive stress-strain curves are 428 equivalent changes. The parameters  $\alpha_1$  and  $\alpha_2$  will implicitly include the observed modifications in 429 the behaviour of WC-Co with increasing temperature. Mari [15], this change occurs from 527°C and is 430 explained by an increase in toughness induced by the softening of cobalt under limited plastic

- 431 deformation. The sliding of WC grain boundaries is one of the mechanisms involving this softening as
- 432 reported by several authors [15, 54]. Above 827 °C, the behaviour of the composite is entirely plastic.

433 For the reconstruction of the elasto-plastic behaviour of the WC, the temperature-dependent evolution

- 434 of one of the parameters will be imposed while the other will be defined from the compressive stress-
- 435 strain curves of the composite for different temperatures.

- $\alpha_1(T)$  has been calculated assuming that the evolution of the ratio  $\sigma_{wc-Co}(T = 25^{\circ}C)$  of 436
- the composite is the same as that of the WC material.  $\sigma_{wc-Co}(T)$  and  $\sigma_{wc-Co}(T = 25^{\circ}C)$  are the 437
- 438 stresses of the composite measured at a given temperature and at room temperature, respectively, for a
- 439 plastic deformation of 0.2%. This assumption may be rough, but it ensures that the yield stress of WC
- is always higher than that of the composite. Indeed, as shown in Figure 14, the behaviour of the composite is between that of carbide and cobalt. It allows the cobalt to deform plastically over a wide 441
- 442 range of strains before the carbide deformations occur in the composite.  $\alpha_2(T)$  have been determined
- 443 by performing several simulations to reach, by trial and error, a good agreement with the experimental
- 444 stress-strain curves of the composite, see Figure 16. The values of  $\alpha_1(T)$  and  $\alpha_2(T)$ , shown in Figure
- 15, decrease gradually as the temperature increases. Nevertheless, their respective evolutions are 445
- independent although  $\alpha_1(T)$  and  $\alpha_2(T)$  are close for 200, 400, 800°C. In other words, the evolution of 446
- 447 the yield stress as a function of temperature is not dependent on that of the hardening.
- 448 The plastic stress-strain curves of the WC in compression can be plotted for different temperatures as
- 449 shown in Figure 17 and compared with the results obtained by Faksa et al. [26]. Let us recall that these
- authors determined the behaviour of the WC, with a similar strategy, more precisely, from those of the 450
- composite WC-6wt.%Co and a cobalt alloy. The orders of magnitude of the stresses are almost 451
- similar, except for the shape of the curves and the yield stress. The shape of the curves in this case is 452
- 453 imposed by the relation (4), while those of Faksa et al. are obtained directly from the simulation
- 454 results. The yield stresses of WC obtained by these authors overestimates by 1 GPa those of this paper
- for temperatures of 25°C, 200°C, 400°C. However, they are almost identical for temperatures above 455
- 600°C. It can be noted that the determination of the yield stress of WC is not obvious because 456
- 457 according to Csanádi et al. [55], the tolerance in its measurement can reach 1 GPa.
- 458 As the parameters  $\alpha_1(T)$  and  $\alpha_2(T)$  are determined from the data of the composite WC-6 wt.%Co, the
- 459 model is applied to compression tests of a composite WC-10.5wt.%Co measured by Teppernegg et al.
- 460 [30] for different temperatures, see Figure 18. All model parameter values are summarised in Table 1.
- For temperatures above  $600^{\circ}$ C, the model overestimates the experimental curves for a strain of 0.25% 461
- 462 at T=900°C. On the other hand, for temperatures less than or equal to 600°C, the simulations
- underestimate the experimental data with a maximum error of 30 % for a strain of 0.3% at T=600°C. 463
- 464 Note that the difference between the calculated and measured curves reduces as the temperature
- 465 decreases. The modelling correctly predict the measured stress-strain curves, especially for strains
- greater than 1% (except for the one obtained at 900°C). After 800°C, the elasto-plastic laws used in 466
- the present modelling seem less appropriate as the material becomes more sensitive to strain rate 467
- (Smith and Wood 1968). Teppernegg's et al. (Teppernegg et al. 2016) obtained experimental data with 468
- an imposed strain rate of  $5.10^{-3}$  s<sup>-(-1)</sup> corresponding to that encountered in creep tests (Sakuma 469
- and Hondo 1992). For high temperatures, visco-plastic models would be more suitable to reproduce 470
- 471 the behaviour of carbide and cobalt phases.

# 472 5.4 Comparison between the models using von Mises and Drucker Prager criteria for 473 WC

474 So far, simulations presented above have been performed with the von Mises criterion applied to the 475 carbide phase. The hardening parameters  $Q_{WC} = 3000 MPa$  and  $b_{WC} = 500$  as well as the parameters  $\alpha_1(T)$  and  $\alpha_2(T)$  found previously have been also applied for the Drucker Prager criterion. Figures 19 476 477 and 20 show a comparison between these two criteria on the stress-strain curves computed at different 478 temperatures for the carbide grades WC-6wt.%Co and WC-10.5wt.%Co, respectively. The curves 479 computed with both criteria for the WC-6wt.%Co composite are almost identical, when the behaviour of the WC phase is determined with the von Mises criterion, the average stress tensor, shown by the 480 481 relation (14), is close to a state of uniaxial compressive stress.

482 
$$\boldsymbol{\sigma} = \begin{pmatrix} 241 & -4.4 & 0.9 \\ -4.4 & -6106 & -1.3 \\ 0.9 & -1.3 & 278 \end{pmatrix} MPa$$
(14)

This tensor has been computed at room temperature and for a strain of 2%. The same case for thestress tensor was computed with the Drucker Prager criterion, see relation (15).

485 
$$\boldsymbol{\sigma} = \begin{pmatrix} 150 & -5.9 & 0.7 \\ -5.9 & -5946 & -0.9 \\ 0.7 & -0.9 & 170 \end{pmatrix} MPa$$
(15)

As mentioned in Section 2.2.2 and Appendix A, for this mechanical loading, the two models are
equivalent explaining the curves superpositions of Figure 19.

488 However, the stress states calculated at each integration point are locally different due to the complex shape of the WC phase and can be represented by points in a diagram p - I2 in order to analyse their 489 dispersion. This type of diagram also used by Tkalich et al. [25] is plotted for both criteria in Figures 490 21(a) and (b) at room temperature for a total strain of 2%. Most of these points are concentrated in the 491 vicinity of the bold red line which represents the load path for a uniaxial compression. The green and 492 493 blue lines symbolize the initial and maximum yield stresses, respectively. In Figure 21(b), these last 494 two lines are tilted in the case of the Drucker Prager model because of its dependence on pressure. For 495 this model, the diagram clearly shows the difference between the compressive and tensile yield stress 496 with a shorter load path for the tensile depicted by the blue line. Another difference between these two criteria is that certain stress states may exist in one of these two models and not in the other. For 497 example, in Drucker Prager's model for high pressures, some points are above the maximum yield 498 stress of the Mises model, see Figure 21(a). The opposite can be observed for low pressures, where 499 500 some points calculated with the von Mises criterion are above the maximum yield stress of the

- 501 Drucker Prager criterion. However, this concerns only a few points and has no impact on the stress-
- strain curves of this composite in compression as shown in Figure 19.

As the cobalt content increases, the shape of the WC phase becomes more complex and involves more 503 varied stress states in the microstructure. In the case of the composite WC-10.5wt.%Co, the dispersion 504 of the points is greater with an increase in the number of areas in the microstructure with low plasticity 505 506 in the WC as shown Figures 21(c) and d. For the Drucker Prager model, in Figure 21(d) a shift of most 507 of the points from the compression path towards low pressures in the diagram  $p - J_2$ , is also observed. These data have been calculated for both criteria at room temperature for a total strain of 2%. In this 508 509 case, the average stress state gets away from a uniaxial compressive mechanical load and therefore 510 these models are no longer equivalent. That is why there is a slight difference between the curves in 511 Figure 20 calculated according to these two criteria. The discussions and comments written in the 512 previous section between the experimental data and the results of the von Mises model can be applied 513 to the Drucker Prager model.

514 For future simulations at the microstructural scale, the Drucker Prager criterion is better suited to

represent the behaviour of the WC phase because it can simulate the difference between the tension

and compression behaviours observed in the composite.

517 6. Conclusions and Perspectives

In this paper, a microstructure scale modelling has been proposed to simulate the elastoplastic
behaviour of the WC-Co composite with different contents of cobalt and various temperatures from 25
to 900 °C.

The elastoplastic behaviour of each phase has been identified from the literature. The cobalt has been 521 522 modelled with the von Mises criterion for its plastic behaviour. This criterion and the Drucker Prager 523 one have been used in the first instance for the tungsten carbide phase at room temperature. Although 524 its behaviour is often considered elastic, it has been extended to the field of plasticity to simulate the 525 compression of the composite for strains greater than 0.6%. The properties at the WC-WC and WC-Co 526 interfaces as well as the WC grain size effect have not been considered. Thereafter, realistic microstructures have been generated by an algorithm inspired from the work of Tkalich et al. [25] to 527 control the grain number of WC and the cobalt content. 528

529 Then, a study has been led to determine the WC grain minimum number in a representative volume

530 element to reproduce the macroscopic behaviour of the composite in compression. The convergence of

- the criteria as the isotropy of the elastic behaviour, the Young's modulus, the ratio between the
- 532 dissipated plastic energy and the external work and the Hill's criterion have been achieved for
- 533 microstructures which the number of WC grain is larger than 250.
- 534 In the following of this study, the hardening parameter of plastic behaviour models for the carbide
- phase have been determined  $Q_{WC} = 3000 MPa$  and  $b_{WC} = 500$  from the uniaxial compression tests
- performed on a grade WC-6wt.%Co at room temperature. Then, the yield criterion has been extended

- to different temperatures by the introduction of two functions  $\alpha_1(T)$  and  $\alpha_2(T)$ . These two parameters
- represent the dependence of the yield stress and hardening on temperature, respectively. These
- 539 functions have been determined with a microstructure of 275 grains from the elastoplastic behaviour
- of the cobalt and composite WC-6wt.%Co for a temperature range of [20-900°C] with the von Mises
- 541 model.
- 542 Simulations have been performed to predict the stress-strain curves in compression of the composite
- 543 WC-10.5wt.%Co compared with experimental data taken from the work of Teppernegg et *al.* [30]. A
- 544 good agreement was observed for all temperatures for a strain larger than 1% excepted for 900°C.
- 545 Before this strain, the model overestimates and underestimates the experimental curves for
- temperatures larger and lower than 600°C, respectively.
- 547 A comparison between the von Mises and Drucker Prager criteria applied to the carbide phase have
- 548 been also discussed. Both models lead to equivalent results in uniaxial compression. Nevertheless, the
- 549 local stress states between these approaches become different when the cobalt content increases.
- 550 However, it is recommended to use Drucker Prager criterion because it can reproduce the difference
- between yield stress in traction and compression observed in the composite.
- 552 The model presented in this work assumes that the decrease in the stress rate for large deformations is
- only due to plastic deformations. Possible extensions and improvements can be proposed in
- 554 forthcoming work, such as considering the damage and the visco-plastic behaviour of the composite
- 555 phases. In addition, the used plastic models neglect the WC and Co grain size and their orientation. It
- would be interesting to use the crystal plasticity for both phases for a more accurate description of the
- 557 composite behaviour.
- 558
- 559

561

562

563

564

# 566 Appendix A. Proof of the equivalence of the von Mises and Drucker

## 567 **Prager elasto-plastic models under a compression loading**

568 The following appendix shows that the plastic stress-strain curves of the uniaxial compression test 569 obtained in the compression axis are equivalent for the Mises and Drucker Prager models if  $\phi_{WC}$  =

570  $\psi_{WC} = 45^{\circ}$ . Only the quantities useful for this proof are defined. For more information on undefined

571 quantities, please refer to Section 2. The *MS* and *DP* indices attached to the quantities refer to the von

572 Mises and Drucker Prager models.

573 In the uniaxial compressive test, Cauchy stress tensor is written as follow :

574 
$$\boldsymbol{\sigma} = \begin{bmatrix} -\sigma_{com} & 0 & 0\\ 0 & 0 & 0\\ 0 & 0 & 0 \end{bmatrix}$$
(A.1)

575 with  $\sigma_{com} > 0$ , the magnitude of the stress in the direction of compression.

576 The yield surface for both models is

577

$$f_{WC}(\boldsymbol{\sigma}, p) = \sigma_{eq} - (R_{WC} + Y_{WC}(p))$$
(A.2)

578 In the von Mises model, the equivalent stress is  $\sigma_{eqMS} = J_2(\sigma)$ . For the stress state of (A.1),  $\sigma_{eqMS} = \sigma_{com}$ . In the Drucker Prager model, the equivalent stress is  $\sigma_{eqDP} = \frac{J_2(\sigma) + I_1(\sigma) \tan(\phi_{WC})/3}{1 - \tan(\phi_{WC})/3}$  with  $\phi_{WC} = 45^{\circ}$ . For the stress state of (A.1), the equivalent stress is also the one computed with the Mises model, i.e.  $\sigma_{eqDP} = \sigma_{com}$ .

582 In relation (A.2), the accumulated plastic strain *p*, for the von Mises model is defined as follow :

583 
$$p_{MS} = \int_0^t \dot{\varepsilon}_{eqMS} dt = \int_0^t \sqrt{\frac{2}{3}} \dot{\varepsilon}_{MS}^P \vdots \dot{\varepsilon}_{MS}^P dt$$
(A.3)

with plastic strain rate equivalent  $\dot{\varepsilon}_{eq}$  which is computed from the plastic strain rate tensor

585  $\dot{\varepsilon}_{MS}^{P}$  computed from the associate flow rule :

586 
$$\dot{\boldsymbol{\varepsilon}}_{\boldsymbol{MS}}^{\boldsymbol{P}} = \dot{\lambda} \frac{\partial f_i}{\partial \sigma}$$
(A.4)

587 In the case of the stress state given in (A.1), the plastic strain is :

588 
$$\dot{\boldsymbol{\varepsilon}}_{MS}^{\boldsymbol{P}} = -\dot{\boldsymbol{\varepsilon}}_{com} \begin{pmatrix} 1 & 0 & 0\\ 0 & -\frac{1}{2} & 0\\ 0 & 0 & -\frac{1}{2} \end{pmatrix}$$
(A.5)

with  $\dot{\varepsilon}_{com} > 0$  the magnitude of the strain rate plastic deformation in the compressive direction.

590 Therefore, the plastic strain rate equivalent is  $\dot{\varepsilon}_{eqMS} = \dot{\varepsilon}_{com} > 0$ .

591 For the Drucker Prager model, the accumulated plastic strain is defined as :

592 
$$p_{DP} = \int_0^t \dot{\varepsilon}_{eqDP} \, dt = \int_0^t \frac{\sigma \cdot \dot{\varepsilon}_{DP}^P}{\sigma_{eqDP}} \, dt \tag{A.6}$$

593 With equivalent plastic strain rate  $\dot{\varepsilon}_{eqDP}$  which is computed from the plastic strain rate tensor  $\dot{\varepsilon}_{DP}^{P}$ 

594obtained from the flow rule :

595

596 The flow potential for  $\psi_{WC} = 45^{\circ}$  is :

597 
$$g_{WC}(\boldsymbol{\sigma}) = J_2(\boldsymbol{\sigma}) + \frac{1}{3}I_1(\boldsymbol{\sigma})tan(\psi_{WC})$$
(A.8)

 $\dot{\boldsymbol{\varepsilon}}_{\boldsymbol{DP}}^{\boldsymbol{P}} = \dot{\lambda} \frac{\partial g_{WC}}{\partial \sigma}$ 

(A.7)

598 In the case of the stress state given in (A.1), the plastic strain is :

599 
$$\dot{\boldsymbol{\varepsilon}}_{\boldsymbol{D}\boldsymbol{P}}^{\boldsymbol{P}} = -\dot{\boldsymbol{\varepsilon}}_{com} \begin{pmatrix} 1 & 0 & 0\\ 0 & -\frac{15}{12} & 0\\ 0 & 0 & -\frac{15}{12} \end{pmatrix}$$
(A.9)

600 Therefore, the equivalent plastic strain rate is  $\dot{\varepsilon}_{eqDP} = \dot{\varepsilon}_{com}$  which is identical to the one computed 601 with the von Mises model.

602 To conclude, for both models, the accumulated plastic strain is

$$p = \int_0^t \dot{\varepsilon}_{com} dt = \varepsilon_{com} \tag{A.10}$$

as well as the yield surfaces are the same. Consequently, the curves ( $\sigma_{comp}, \varepsilon_{com}$ ) plotted for these models are equivalent.

## 606 Acknowledgment

607 The author wishes to thank the French ministry of higher education, research and innovation for608 financial support.

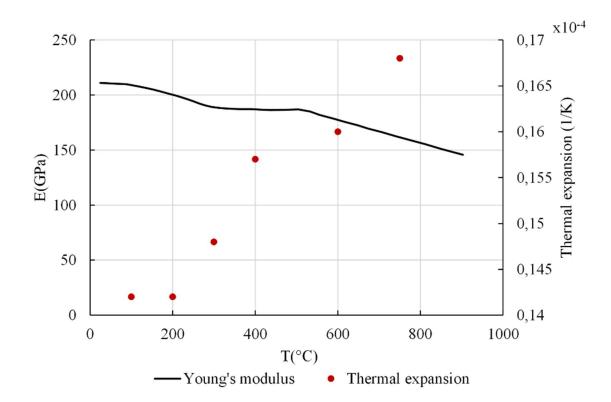


Figure 1. Young's modulus and thermal expansion used for the Co-phase as a function of temperature,[28, 29].

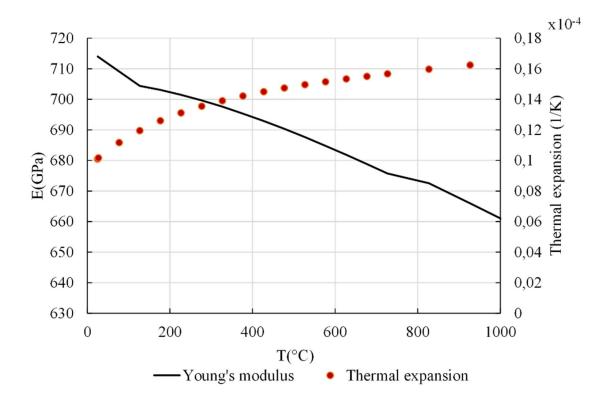
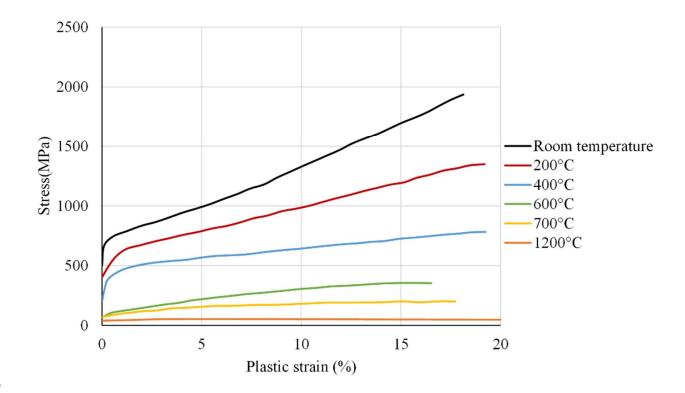


Figure 2. Young's modulus and thermal expansion used for the WC-phase as a function oftemperature, [21, 33, 57].





616 Figure 3. Stress-plastic strain curves of the Co-phase in uniaxial compression for different

617 temperatures, [38].

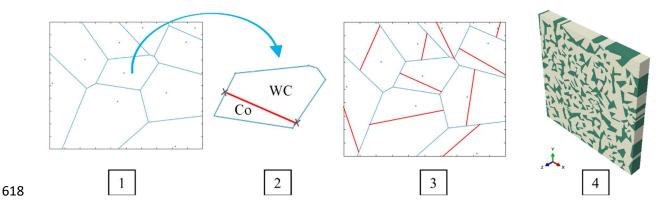
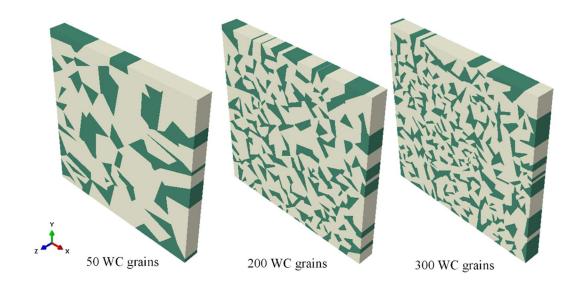


Figure 4. (1) Construction of the Voronoi cells based on random point distribution. (2) Partition of

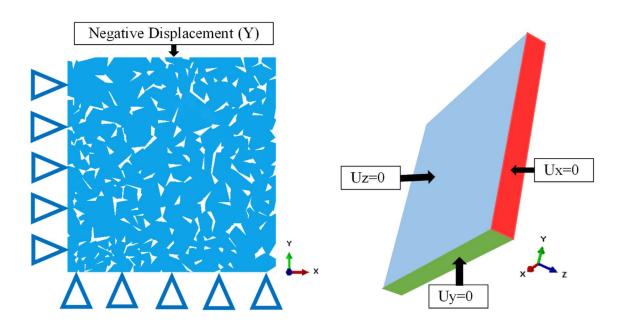
each cell into two phases. (3) Obtained 2D microstructure. (4) Extrusion of the microstructure in the z

621 direction.





623 Figure 5. Representative elementary volumes with different numbers of WC grains (WC-20wt.%Co).



625

Figure 6. Boundary conditions applied on the RVE. Ux, Uy and Uz are the displacements in x, y and z

627 directions, respectively.

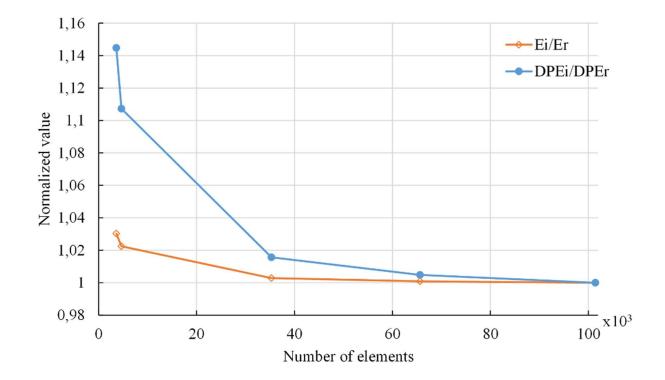


Figure 7. Influence of the number of elements "*i*" on the ratios  $E_i/E_r$  and  $DPE_i/DPE_r$ . The couples  $E_r$ ,  $E_r$  and  $DPE_r$ ,  $DPE_r$  are the Young's moduli and dissipated plastic energies. The r index means that quantities are computed for 100,000 elements.

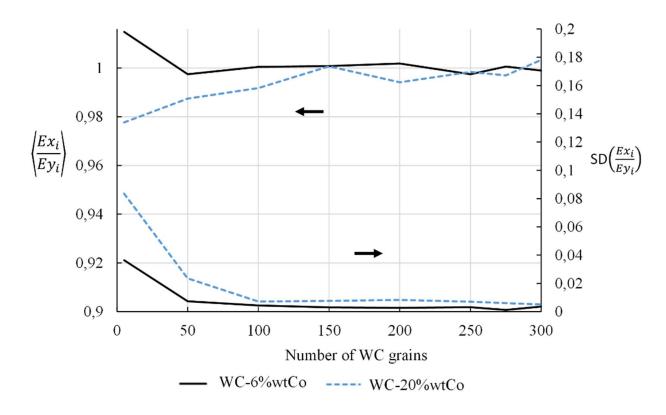
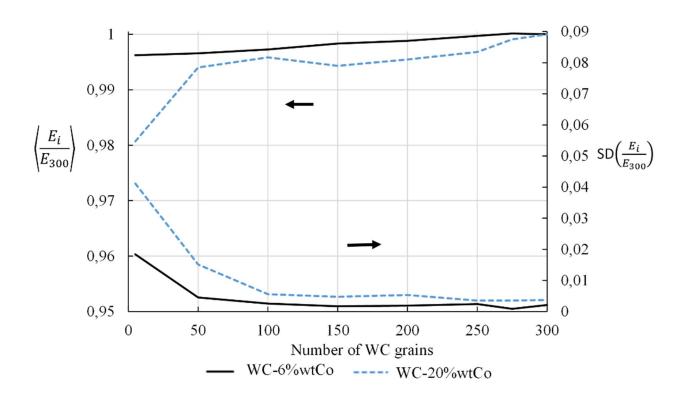


Figure 8. Evolution of the mean (>) and standard deviation (SD) of the ratio  $E_{xi}/E_{yi}$  as a function of the WC grains number "*i*".  $E_{xi}$  and  $E_{yi}$  are the Young's moduli computed in the *x* and *y* directions for "*i*" elements, respectively.



636

637 Figure 9. Evolution of the mean (>) and standard deviation (SD) of the ratio  $E_i/E_{300}$  as a function of

638 number of WC grains "*i*".  $E_i$  is the Young's modulus computed for i grains while  $E_{300}$  is the mean

639 Young's modulus computed for 300 grains.

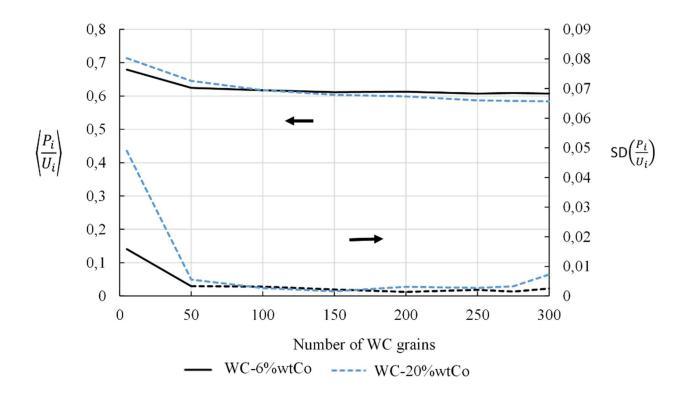




Figure 10. Evolution of the mean (>) and standard deviation (SD) of the ratio  $P_i/U_i$  as a function of the number of grains "*i*".  $P_i$  and  $U_i$  are the dissipated plastic energy and the external work, respectively.

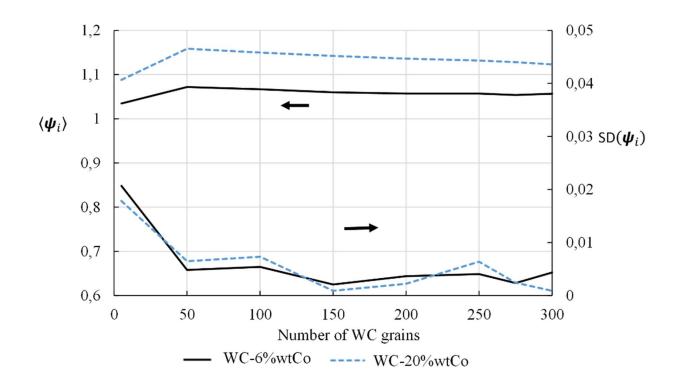
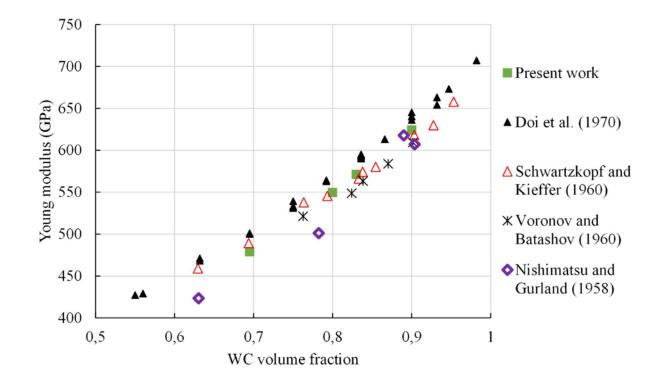


Figure 11. Evolution of the mean ( $\sim$ ) and standard deviation (SD) of Hill criteria  $\psi_i$  as a function of WC grains "i".



648Figure 12. Comparison between the simulated Young's modulus for WC-Co with different WC

649 volume fractions and experimental results [48–51].

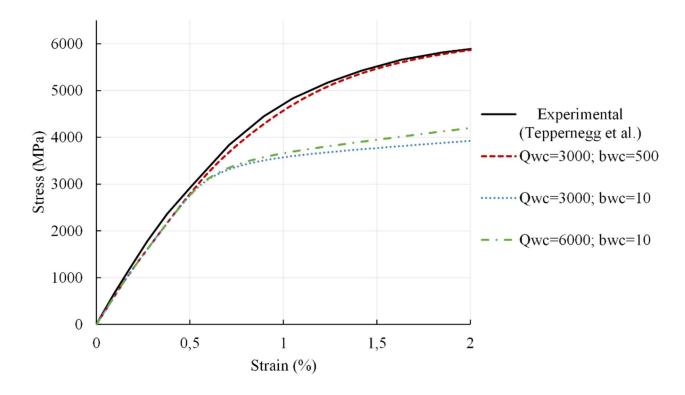
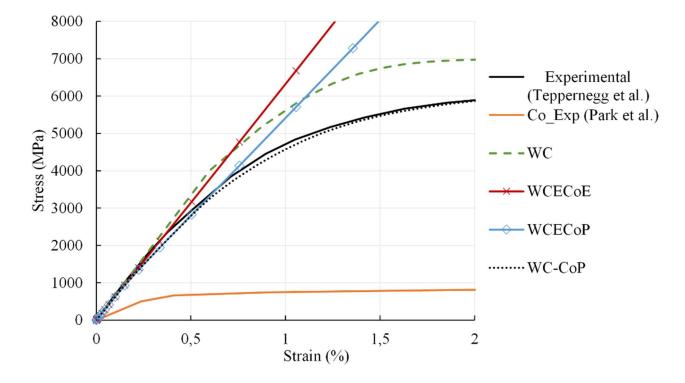


Figure 13. Influence of the hardening parameters  $Q_{WC}$  and  $b_{WC}$  on the computed stress-strain curves

for a composite WC-6wt.%Co in uniaxial compressive test.



653

Figure 14. Comparison between the stress-strain curves for different combinations of phase behaviour in uniaxial compression with experimental data taken from references [30] and [38]. The indices E and P mean that the phases have elastic and elasto-plastic behaviours, respectively. For the WC phase, the selected hardening parameters are  $Q_{WC}$ =3000MPa and bwc=500.

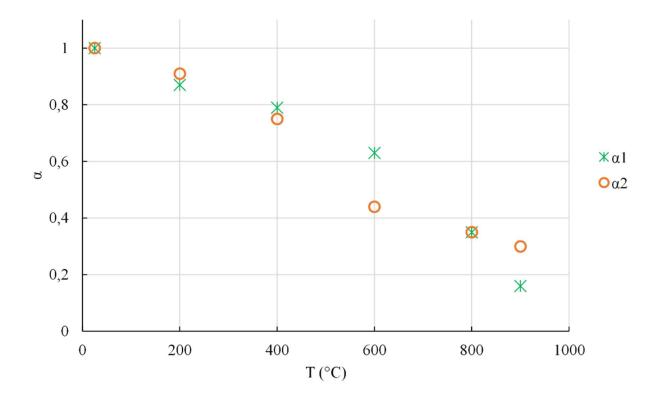


Figure 15. Evolution of  $\alpha_1$  and  $\alpha_2$  parameters as a function of temperature.

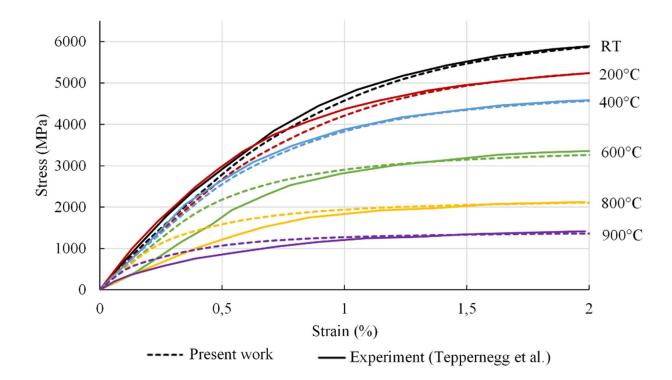


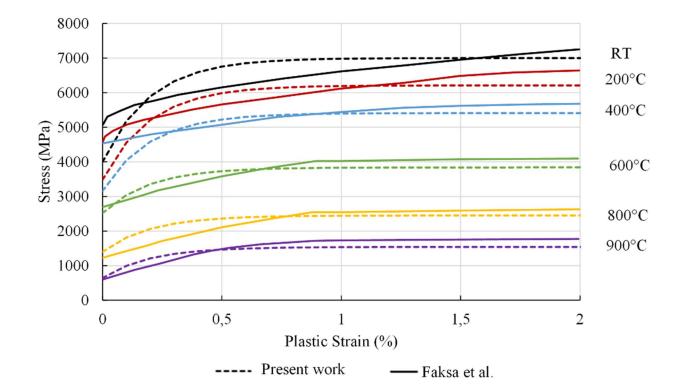
Figure 16. Comparison between experimental results obtained from [30] and computed stress-strain

662 curves at different temperatures for a composite WC-6wt.%Co under uniaxial compression (200°C-

663 900°C).

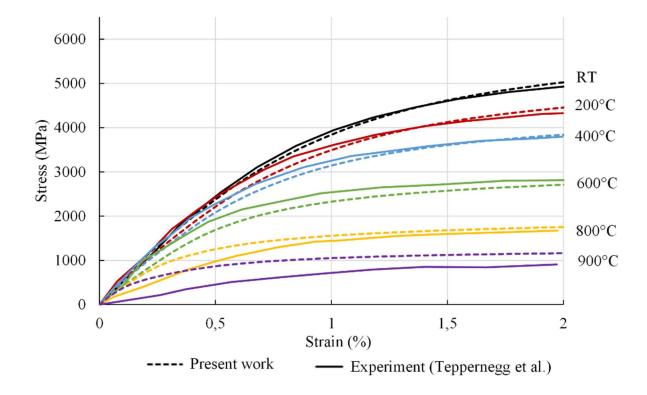
*Table 1 Summary of the model parameters.* 

Cobalt ( $C_o$ )			
Young's modulus	$E_{C_o}$	See Figure 1	
Poisson's ratio	$\nu_{C_o}$	0.31 [21]	
Coefficient of the thermal expansion	$\alpha_{T_{C_{o}}}$	See Figure 1	
Initial yield stress and hardening	-0	See Figure 3	
Tungsten carbide ( <i>WC</i> )			
Young's modulus	$E_{WC}$	See Figure 2	
Poisson's ratio	$v_{WC}$	0.194 [21]	
Coefficient of the thermal expansion	$\alpha_{T_{WC}}$	$\alpha_{TWC}$ See Figure 2	
Von Mises and Drucker Prager models			
Initial yield stress in uniaxial compression	$R_{WC}$	4000 MPa [24]	
Friction angle	$\phi_{WC}$	45°	
Dilatation angle	$\psi_{WC}$	45°	
Hardening constants	$Q_{WC}$	3000 MPa	
-	$b_{WC}$	500	



669 Figure 17. Comparison between stress-plastic strain curves computed in the present work and by

Faksa et al. [26] for the WC phase for different temperatures (200°C-900°C).



671

Figure 18. Comparison between the stress-strain curves computed in the present work and those

673 measured by Teppernegg et al. [30] for a composite WC-10.5wt.%Co under uniaxial compression for

674 different temperatures (200°C-900°C).

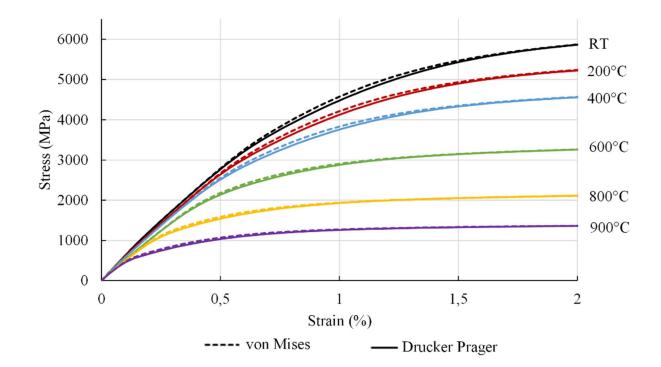
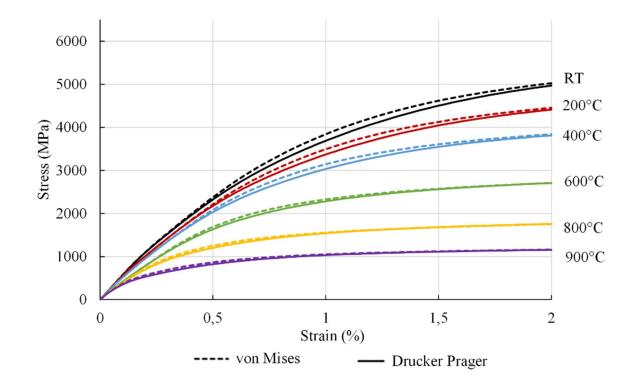




Figure 19. Comparison between the stress-strain curves computed with von Mises and Drucker Prager

677 models applied to the tungsten carbide phase for a composite WC-6wt.%Co under uniaxial

678 compression for different temperatures (200°C-900°C).



679

680 Figure 20. Comparison between the stress-strain curves computed with Mises and Drucker Prager

models applied to the tungsten carbide phase for a composite WC-10.5wt.%Co in uniaxial

682 compression for different temperatures.

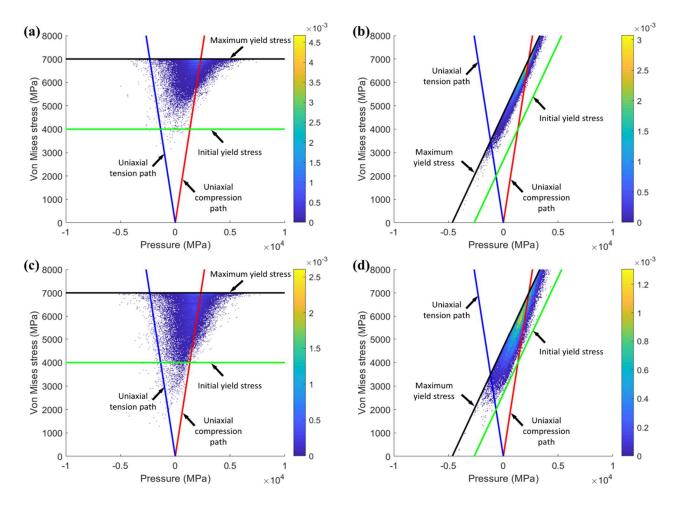




Figure 21. p-J2 Diagram obtained from the stress tensor calculated at each integration point in the carbide phase. p is the pressure and J2 the von Mises stress. Each "point" in the figure corresponds to a rectangle with dimensions of 50x25MPa containing a stress state group. The color of the scale indicates the probability of finding this stress state group in the carbide phase. These data were computed with (a): the von Mises criterion and (b): the Drucker Prager criterion for a WC-6wt.%Co composite, (c): The von Mises criterion and (d) the Drucker Prager criterion for a WC-10.5wt.%Co composite and for a total strain of 2% at room temperature.

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