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# Fully carbon metasurface: absorbing coating in microwaves

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The microwave-absorbing properties of a heterostructure consisting of an ordered monolayer of porous glassy carbon spheres were experimentally and theoretically investigated in the Ka-band (26-37 GHz) frequency range. The electromagnetic response of such “moth-eye”-like all-carbon metasurface at a normal incidence angle was modelled on the basis of long-wave approximation. Modelling parameters in the Ka-band were used to estimate and predict the absorption properties of monolayers in free space in the range 1-40 GHz. Experimental and theoretical results demonstrate that a metasurface based on porous glassy carbon spheres is an **inert**, lightweight, compact and perfectly absorbing material for designing new effective microwave absorbers in various practically used frequency ranges.

Keywords: Radar absorbers, antireflective coatings, microwave absorption, glassy carbon, Ka-band, moth-eye structure

## I. INTRODUCTION

Until now, artificial metamaterials proposed by Pendry et al.<sup>1</sup> and realised experimentally by Smith et al.<sup>2</sup> were always hybrids based on dielectric and metal elements of sophisticated geometries. Recently, Liu et al.<sup>3</sup> have proposed a fully dielectric metasurface which has some advantages, including high absorption of electromagnetic radiation of particular frequency by very small volume and simple geometry. In the present paper, the alternative idea and the practical realisation of an all-carbon metasurface made of glassy carbon spheres (GCSs) is presented. Such GCSs were simply organised in periodic arrays and could provide a perfect absorption of microwaves. The individual GCSs have an average diameter about  $\sim 1$  mm and consist of porous glassy carbon. In terms of pore size their internal structure is in-between that of carbon foams<sup>4-6</sup> and aerogels<sup>7</sup>. **Glassy carbon is a non-graphitizing, highly disordered, carbon with features that make it definitely different from graphite: it is hard and brittle with a conchoidal fracture, shiny and isotropic, and with a density typically 30% lower than that of graphite. Its electrical conductivity is isotropic and may be as high as  $30 \times 10^3$  S/m after pyrolysis at  $3000^\circ\text{C}$ <sup>8</sup>. This material is commonly used for producing inert and thermally stable electrodes in electrochemistry<sup>9</sup>.** The combination of good electrical conductivity of glassy carbon and the spherical shape can be very useful for practical applications, particularly for those related to the absorption of electromagnetic (EM) radiation. **Many researchers world-**

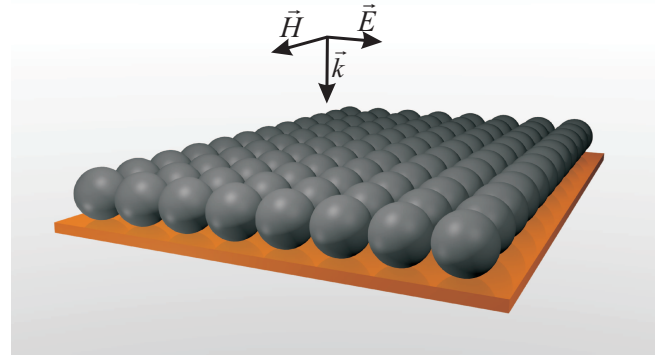


FIG. 1. Monolayer of porous glassy carbon spheres on a PEC plate.

**wide are concentrated on the design of broadband absorbers. Generally, the following mechanisms of EM absorption are used for practical applications: ferromagnetic resonance<sup>10,11</sup>, Ohmic losses<sup>12,13</sup>, dipole relaxation<sup>14</sup> and lossy scattering in metamaterials<sup>15</sup>. At present, many groups focus on the investigation of carbon-based polymer composites for developing effective microwave absorbers<sup>16-18</sup>. In this paper, we considered the features of normal scattering of microwave radiation on an ordered monolayer of porous carbon spheres on a Perfect Electrically Conducting (PEC) plate, schematically shown in Fig.1.**

Materials based on spherical particles are attracting interest of many research groups worldwide. In the recent decade there has been a considerable effort devoted to the investigation of electromagnetic properties of similar structures, including: metasurfaces formed by planar arrays of spherical particles<sup>19</sup>, lossless magneto-dielectric

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spheres embedded in a background matrix<sup>20,21</sup>, as well as two-dimensional lossy heterostructures<sup>22</sup>. In most of the cases the investigations involved modelling based on the earlier work of Lewin<sup>23</sup> for sparse arrays of spherical particles. In turn, the materials considered here are formed by highly lossy glassy carbon spheres ordered in a close-packed array. In our recent report<sup>12</sup> we considered a similar structure but based on hollow carbon spheres (HCSs). Compared to the latter, the GCSs are much more mechanically resistant, which is especially important for further practical use.

The analysis of the electromagnetic response of non-uniform periodic structures may be significantly simplified when the wavelength of the external electromagnetic wave is much larger than the characteristic lateral dimensions of the structure. Moreover, non-homogeneous structures with graded refractive index are widely used in the industry for designing and developing various types of microwave absorbers<sup>24–29</sup> and the long-wave approximation<sup>30–33</sup> is commonly applied to describe and predict their electromagnetic properties in the microwave frequency range.

The present paper is organized as follows. The details of preparation of GCSs and of **the characterisation techniques as well of experimental microwave measurements** are given in Section II. In Section III, **we provide the materials main characteristics**. In Section IV, we describe the homogenisation technique which is used to obtain the equivalent material properties and the electromagnetic response of the GCS monolayer. Herein we also compare the experimental data with the results of modelling. Theoretical predictions of the absorption properties in free space of the GCS-based metasurface are discussed in Section V. Finally, the Conclusions section summarises the findings and gives an outlook on potential application of such metasurfaces.

## II. EXPERIMENTAL

### A. Preparation of materials

The synthesis of porous glassy carbon spheres is based on several main components including: sodium alginate (Algin Texturas), calcium chloride (Roth), resorcinol (Alfa Aesar), and a 37% aqueous solution of formaldehyde (Roth). All these chemicals were used “as is” without further purification. First, a 20 mL aqueous solution containing 12.8 g resorcinol, 9.43 g formaldehyde solution and 2.22 g of CaCl<sub>2</sub> was prepared. Dropwise addition of 5 mL of a 0.5 wt.% sodium alginate in water, using a syringe of volume 10 mL having a needle of diameter and length 0.8 mm and 50 mm, respectively, to the former solution heated at 60° C under magnetic stirring, instantaneously induced gelation and led to polymer beads of size about 2.1 mm. The beads were recovered by filtration after 1 h of stirring at the same temperature of 60° C, and then treated in hot pressurised water (180° C,

24h) for hydrothermal carbonisation (HTC) in an autoclave. The aim of HTC was to stabilise the spheres and increase their carbon content. Finally, the beads recovered after HTC were submitted to pyrolysis at 900° C (2° C/min, 2h dwell time).

Whereas the size of the final carbon spheres did not significantly depend on the experimental conditions, their density could be tuned through the concentration of the reactants. Given the carbon precursor used here, i.e., resorcinol-formaldehyde resin, the spheres were made of glassy carbon, **a material rather similar to the one with which hollow spheres were prepared from another non-graphitizing precursor and reported recently for EM applications<sup>12</sup>.**

### B. Characterisation of materials

Carbon spheres were observed without preliminary metallisation with a FEI Quanta 600 FEG scanning electron microscope (SEM). Elemental analysis was performed with an elemental analyser Vario EL Cube (Elementar). The contents of C, H, N and S were measured through the combustion of 3 identical samples in a quartz tube at 1150° C under helium and oxygen in excess, and the average was calculated for each element. The oxygen content was estimated by difference.

Raman spectroscopy was carried out using an XploRa Raman spectrometer (Horiba) without sample preparation. The spectra were collected under a microscope using a 50× objective. The Raman-scattered light was dispersed by a holographic grating with 1200 lines/mm and detected by a CCD camera. Three lasers were used, having wavelengths of 532, 638 and 785 nm, thus corresponding to incident energies of 2.33, 1.94 and 1.58 eV, respectively. The lasers were filtered at 10% of their nominal power for avoiding any heating or damage of the samples. Each spectrum was obtained by accumulation of 2 spectra recorded from 800 to 2200 cm<sup>-1</sup> over 120 s. It was systematically checked that no significant difference was observed when the analysis was performed in different areas of the same sample, suggesting the excellent homogeneity of the materials.

Finally, the textural properties were determined from nitrogen adsorption-desorption isotherms at -196° C, using an ASAP 2020 surface area analyser (Micromeritics). The samples were out-gassed overnight under vacuum at 250° C prior to analysis. Micropore volume,  $V_{\mu}$ , and surface area,  $S_{BET}$ , were determined by application of Dubinin-Radushkevich and BET methods, respectively. The total pore volume measurable by adsorption,  $V_T$ , was defined as the volume of liquid nitrogen corresponding to the amount adsorbed at a relative pressure  $P/P_0 = 0.99$ . The

mesopore volume,  $V_m$ , was calculated as the difference  $V_T - V_\mu$ . The pore size distribution was determined by application of the non-linear density functional theory (NLDFT).

### C. Ka-band measurements

The electromagnetic response of a GCS-based monolayer was experimentally investigated in the Ka-band (26 - 37 GHz) using a scalar network analyser ELMIKA R2-408R. All measurements were carried out in a  $7.2 \times 3.4$  mm waveguide system. For testing the model presented below in Section III, two types of experiments were performed. In one type, the GCSs were initially packed to form a close-compact single layer which was then carefully fixed inside the waveguide between two 1mm-thick layers of Styrofoam® (Dow Chemical), a trademarked brand of closed-cell extruded polystyrene foam transparent to microwave. Due to the unavoidable, slight distribution of GCS sizes and due to some defects in the packing, the as-obtained 2D ordering was closer to a square-shaped lattice. The electromagnetic response of the GCS-based monolayer was obtained as amplitude ratios of transmitted to input ( $S_{21}$ ) and reflected to input ( $S_{11}$ ) signals. In the second type of experiment, the layer of Styrofoam® behind the sample was replaced by the PEC-plate (i.e., behaving as a mirror with a reflection coefficient of 100%). In that case, only the  $S_{11}$ -parameters were measured. Reflection and transmission coefficients were then obtained from S-parameters:  $R = S_{11}^2$ , and  $T = S_{21}^2$ , respectively. The absorption coefficient was then calculated as  $A = 1 - R - T$  and  $A = 1 - R$  in the first and second types of experiments, respectively.

## III. MATERIALS CHARACTERISTICS

Scanning Electron Microscopy (SEM) of typical samples of GCSs are presented in Fig.2 (a)-(b). **A photo of the GCSs monolayer formed “as is” is presented in Fig.2 (c). The order of real GCS-arrays is in between cubic or hexagonal.**

From SEM analysis the average diameter of the spheres was found to be around  $d = 0.79$  mm. The inner structure was relatively homogeneous and close to that of glassy carbon aerogels with a typical pore size less than  $1 \mu\text{m}$ , as evidenced by SEM images at higher magnification (not shown). Based on the average diameter and on the weight of a number of carbon spheres, their average density was found to be  $\rho = 0.39 \text{ g/cm}^3$ . Taking a value of  $1.55 \text{ g/cm}^3$  for the skeletal density of glassy carbon<sup>12,34</sup>, the porosity of the GCS was estimated as 75%.

The elemental weight composition was the following: **91.70 ± 0.50% carbon; 0.80 ± 0.15% hydrogen; 0.21 ± 0.10% nitrogen; and 0.00% sulphur.** The deduced oxygen content was then around 7%. Those values are quite typical for

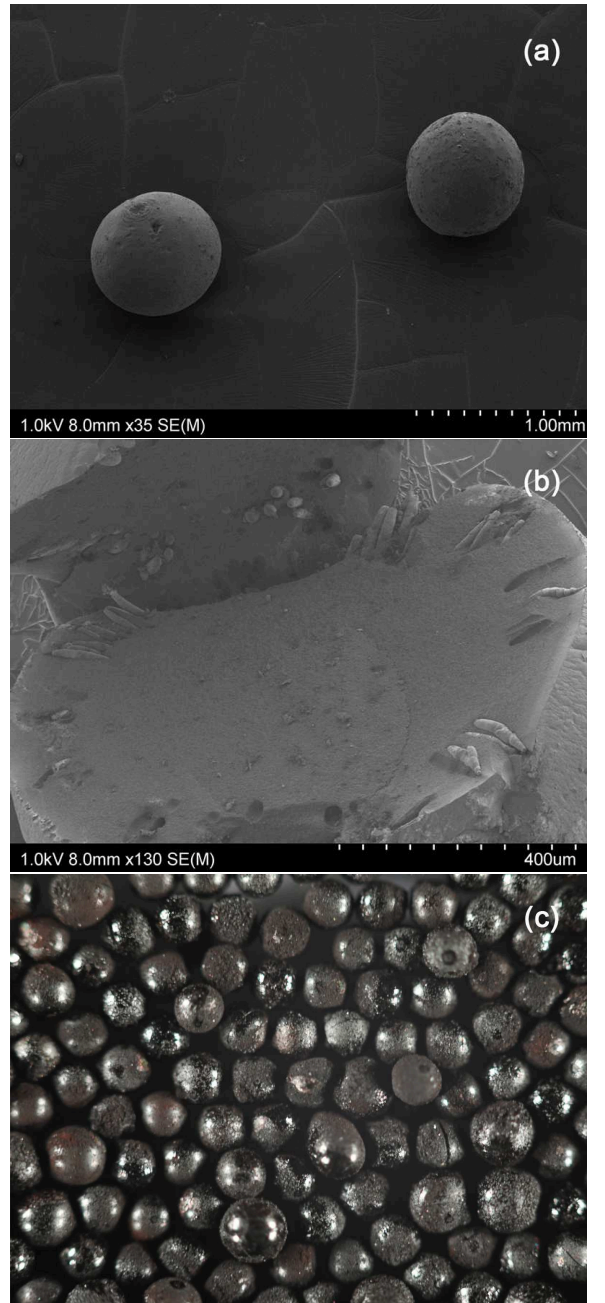


FIG. 2. SEM images of: (a) porous glassy carbon spheres, and (b) inner structure of a broken sphere; (c) **Photo of real GCSs monolayer.**

a carbon material derived from phenolic resin and other oxygenated precursors such as those reported in the synthesis<sup>34,35</sup>. As a result, the carbon was expected to be highly disordered, hence the name “glassy” it was given, and this was proved by Raman spectra shown in Fig.3.

It can indeed be seen in Fig.3 that the spectrum obtained at an energy of 2.33 eV presents a broad D band centred on  $1340 \pm 2 \text{ cm}^{-1}$  and a slightly narrower G band of rather similar intensity at

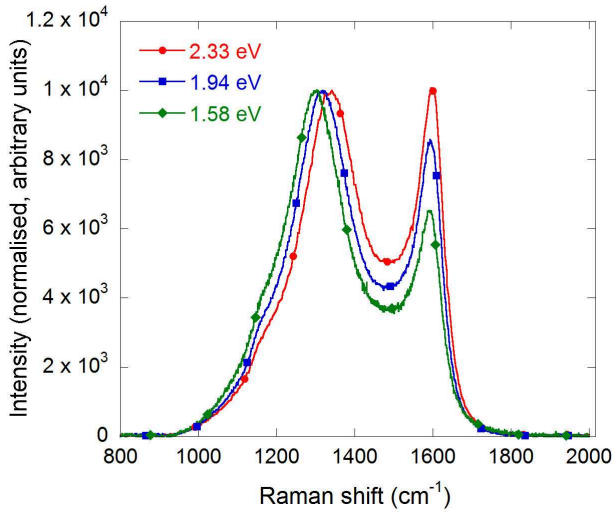


FIG. 3. First-order Raman spectra of glassy carbon spheres as a function of laser incident energy.

$1595 \pm 2 \text{ cm}^{-1}$ . A shallow valley between them and a shoulder at around  $1200 \text{ cm}^{-1}$ , accounted by contributions called D3 and D4, respectively, are also observed. Besides, the positions of D and G bands, their general shapes and their FWHM values (close to  $135$  and  $70 \text{ cm}^{-1}$ , respectively) fully match those already reported for glassy carbon derived from phenolic/furanic resins pyrolysed below  $1000^\circ \text{ C}$  (see for instance<sup>36–40</sup>). Decreasing the laser energy,  $E_L$ , from  $2.33$  to  $1.58 \text{ eV}$  produced the expected phenomena, i.e., a shift of the D band to lower wavenumbers whereas the G band remained at the same position but with a relatively lower intensity. Although only three incident energies were available for establishing quantitative trends, the intensity ratio of D to G bands was found to vary as  $I_D/I_G \simeq E_L^{-1.13}$ , and the D band was seen to shift with the increasing excitation energy at a rate of  $48 \text{ cm}^{-1}/\text{eV}$ . The latter values and the aforementioned ones (band positions and widths) are consistent with each other and are typical of highly disordered carbons having crystallite size close to - or lower than -  $5 \text{ nm}$ <sup>41</sup>, an order of magnitude already reported for similar carbon materials<sup>35</sup>.

Although the texture of such carbon is highly disordered, the electrical conductivity remains rather high, around  $200 \text{ S/m}$ , see next section. This value is lower but still consistent with the one reported elsewhere for non-porous glass-like carbon pyrolysed at  $900^\circ \text{ C}$ , around  $7000 \text{ S/m}$ <sup>36</sup>. The present material indeed has a porosity  $\Phi = 75\%$  and, assuming that the simplest relationship for the conductivity of metal foams holds<sup>42</sup>, i.e.,  $\sigma = \sigma_{\text{bulk}}(1 - \Phi)^{3/2}$ , then the conductivity is one order of magnitude lower than that of the bulk.

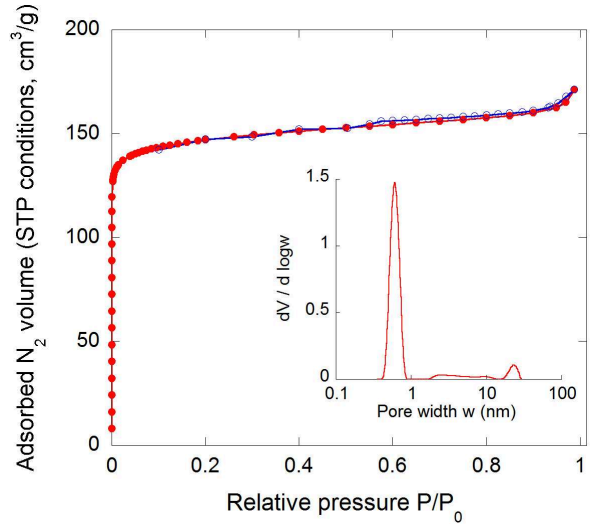


FIG. 4. Adsorption-desorption isotherm (full and empty symbols, respectively) of glassy carbon spheres, and corresponding pore-size distribution (inset).

The present conductivity value is even lower than that, for at least two additional reasons expected to decrease the conductivity further: (i) the presence of alginate of natural origin in the synthesis should have introduced impurities in the carbon matrix; and (ii) the porosity is far narrower than that of a foam, in favour of a much higher scattering of charge carriers within the material.

Indeed, the adsorption-desorption given in Fig. 4 is typical of a highly microporous solid (pore size  $< 2 \text{ nm}$ ) with a very low amount of mesoporosity ( $2 - 50 \text{ nm}$ ), as confirmed by the pore-size distribution shown in the inset. Moreover, the corresponding surface area was  $S_{\text{BET}} = 588 \text{ m}^2/\text{g}$ , whereas micropore and mesopore volumes were  $V_\mu = 0.22 \text{ cm}^3/\text{g}$  and  $V_m = 0.04 \text{ cm}^3/\text{g}$ , respectively. As a result, the macropore volume ( $> 50 \text{ nm}$ ) was therefore deduced to be predominant and equal to  $1/\rho_1/\rho_c - V_m V_\mu = 0.75 \text{ cm}^3/\text{g}$ .

#### IV. MODELLING

The wavelength of the radiation in the Ka-band ( $1 \text{ cm}$  at  $30 \text{ GHz}$ ) exceeds considerably the GCS diameter. Hence the calculations can be significantly simplified by applying a homogenisation procedure to the given structure and using the long-wave approximation. This methodology is traditionally used in optics for modelling antireflective coatings<sup>30,32</sup>, and was successfully applied in our recent works<sup>12,27</sup>.

It is important to note that the primitive homogenisation used in<sup>12</sup> for a monolayer of hollow spheres, consisting in averaging non-conductive air regions with highly conductive carbon regions according to their relative vol-



ume fractions, was not successful in describing the experimental data in the case of the present porous spheres. Simple averaging indeed gave correct results in the case of hollow spheres monolayer because the shell thickness of HCS was much smaller than their diameter, and because the effective dielectric permittivity in the middle part of the layer remained constant. For a monolayer made of GCSs, the spatial distribution of effective dielectric permittivity is much more non-uniform, thus the homogenisation procedure had to be modified to account for these variations.

To model the electromagnetic response of an ordered monolayer of conducting spherical particles on a metal surface, we followed homogenisation methods which are widely used for designing microwave absorbers<sup>24,26,28</sup>. These methods are generally based on the application of equivalent circuits for calculating the effective dielectric permittivity of the structure, and are valid for a wide range of absorber geometries. After homogenisation, the electromagnetic response of the investigated structure in the long-wave approximation was considered to be equivalent to that of a layer of bulk material of the same thickness but with graded effective dielectric permittivity.

### A. Homogenisation procedure

The general principles of the homogenisation procedure used in this work are detailed in<sup>24,28</sup>. Throughout the article we use SI units and assumed an  $\exp[i\omega t - ikz]$  harmonic time convention.

Let us consider the side projection of a GCS monolayer along the  $xz$ -plane as shown in Fig.5(a). The origin of the coordinates is located in the middle of the monolayer. The wave vector of the initial radiation is parallel to the  $x$ -direction. Fig.5(b) presents the monolayer cross-section along the  $yz$ -plane at the coordinate  $x$  ( $|x| < D/2$ ), where  $D$  is the GCS diameter. This cross-section consists of round-like carbon regions of radius  $r = \sqrt{D^2/4 - x^2}$  and air regions. Due to the symmetry of the system, only one quarter of the unit cell (the square of side  $D/2$  and thickness  $dx$  presented in Fig.5(c)) may be considered to calculate the effective dielectric permittivity of the layer at coordinate  $x$ . Let us examine a thin slice of it, having a thickness  $dy$ . It consists of carbon and air regions, which are equivalent to two capacitors in series (Fig.5(d)). The stack of such carbon-air capacitors in parallel contributes to the effective capacitance of the layer. Now, this parameter may be easily calculated by integration over the  $y$ -coordinate within the unit cell and then converted into effective dielectric permittivity of the layer at coordinate  $x$ :

$$\varepsilon_{eff}(x, \nu) = \frac{D - \sqrt{D^2 - 4x^2}}{D} +$$

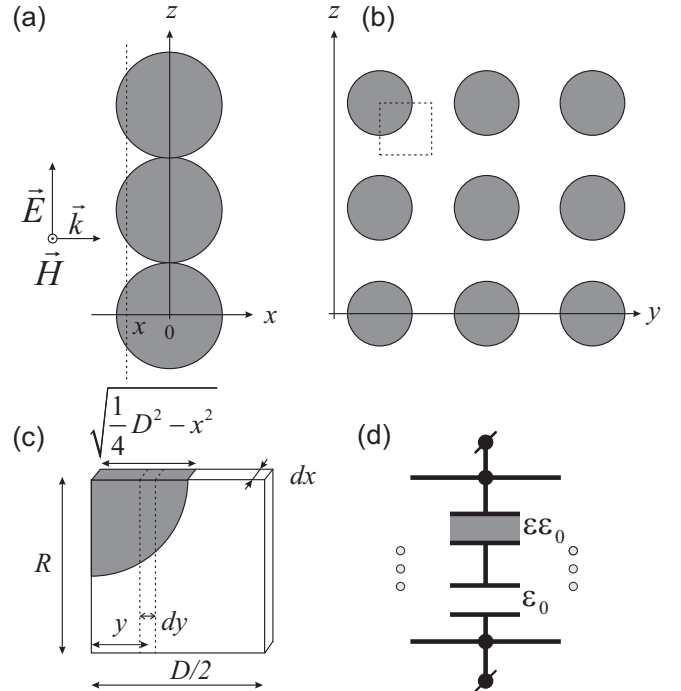


FIG. 5. (a) Side projection of a GCS monolayer along the  $xz$ -plane; (b) cross-section along the  $yz$ -plane at the coordinate  $x$  ( $|x| < D/2$ ); (c) quarter of unit cell used for the calculation of the equivalent material constants; (d) equivalent capacitance model of the layer.

$$+ \int_0^{\sqrt{\frac{D^2}{4} - x^2}} \frac{\varepsilon(\nu) dy}{\varepsilon(\nu) \left( \frac{D}{2} - \sqrt{\frac{D^2}{4} - x^2 - y^2} \right) + \sqrt{\frac{D^2}{4} - x^2 - y^2}}, \quad (1)$$

where  $\varepsilon(\nu) = 1 - \frac{i\sigma}{2\pi\nu\varepsilon_0}$  is the dielectric permittivity of glassy carbon,  $i$  being the imaginary unit,  $\sigma = 200$  S/m the quasi-static bulk electrical conductivity,  $\nu$  the frequency and  $\varepsilon_0 = 8.85 \times 10^{-12}$  F/m the permittivity of vacuum. The value of  $\sigma$  was obtained by fitting the experimental data below, and seems realistic for porous glassy carbon with density  $\rho = 0.39$  g/cm<sup>3</sup> since it is in good agreement with recent published results<sup>6,43</sup>. The spatial distribution of effective dielectric permittivity (1) calculated at 30 GHz is presented in Fig.6.

From Fig. 6 we can see that the absolute values of both real and imaginary parts of effective  $\varepsilon$  are rather low in the outer regions of the GCS monolayer, and increase towards the centre. Nevertheless, in the middle region where the glassy carbon fraction is high and where the contribution of conductive losses dominates, the real part of effective  $\varepsilon$  decreases and has a minimum in the centre of the monolayer. It should be noted that this complex distribution of dielectric permittivity is formed by combination of insulating ( $\varepsilon = 1$ ) and conducting ( $\varepsilon(\nu) = 1 - \frac{i\sigma}{2\pi\nu\varepsilon_0}$ ) media. It is also interesting to see that, if we apply Eq.(1) to a monolayer of lossless dielectric spheres, for example with  $\varepsilon = 2$ , we obtain a spatial

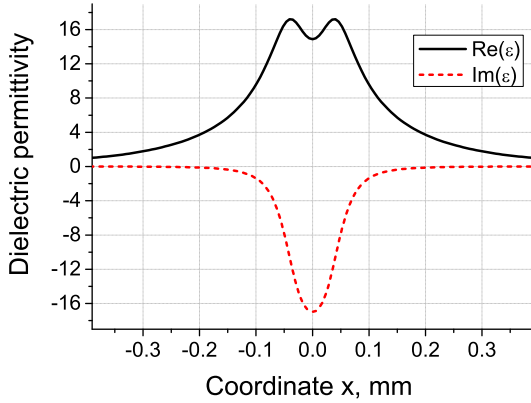


FIG. 6. Spatial distribution of the homogenised effective dielectric permittivity of GCS-based monolayer calculated using Eq.(1) at 30 GHz.

distribution very close to the parabolic one used in<sup>12,30</sup>.

To conclude this section, we should point out that the homogenisation procedure presented above is valid as far as the wavelength of the initial radiation considerably exceeds the GCS diameter. In this case, we can assume that the periodic GCS-based monolayer structure (or GCS metasurface) presents the same electromagnetic response as an effective medium with a spatial distribution of effective dielectric permittivity (1).

## B. Multi-layered medium

For calculating the EM response of a structure having the spatial dispersion described by Eq.(1), we used the model of wave distribution in a multi-layered medium<sup>31,44</sup>.

Let us consider a layer of bulk material with the spatial dispersion obeying Eq. (1). For calculating its coefficients of reflection  $R$ , transmission  $T$  and absorption  $A$ , the following procedure was applied<sup>12</sup>. The layer was first divided into  $N$  parts. When  $N$  is high, it can be assumed that the refractive index inside each part is constant.

Using Maxwell equations, it is possible to obtain the direct solutions for electric and magnetic fields at the boundaries of each thin layer. Written in matrix notations, they have the following form<sup>12,31,44</sup>:

$$\begin{bmatrix} E_1 \\ H_1 \end{bmatrix} = \begin{bmatrix} \cos(k_t \tau_0) & i \sin(k_t \tau_0) k_0 / k_t \\ i \sin(k_t \tau_0) k_t / k_0 & \cos(k_t \tau_0) \end{bmatrix} \begin{bmatrix} E_2 \\ H_2 \end{bmatrix}, \quad (2)$$

where  $E_1, H_1$  and  $E_2, H_2$  are electric and magnetic fields in the left and right sides of a layer of thickness  $\tau_0$ , respectively,  $k_t = \frac{2\pi}{\lambda a} \sqrt{n(x)^2 a^2 - \lambda^2 / 4}$  and  $k_0 = \frac{2\pi}{\lambda a} \sqrt{n_0^2 a^2 - \lambda^2 / 4}$  are the wave vectors in the layer of refractive index  $n(x)$  and in air (refractive index  $n_0 = 1$ ) inside the waveguide of width  $a = 7.2$  mm, respectively,

$\lambda$  being the wavelength. The first term in the right part of Eq. (2) is known as the characteristic matrix of the layer.

In the case of a multi-layered structure, the characteristic matrix of the whole layer is the product of all single layer matrices. The  $R, T$  coefficients of the  $N$ -layered subsystem inside the waveguide can be calculated as:

$$R = S_{11}^2 = \left( \frac{n_0 - C/B}{n_0 + C/B} \right)^2, \quad (3)$$

$$T = S_{21}^2 = \left( \frac{2n_0}{n_0 B + C} \right)^2, \quad (4)$$

where

$$\begin{bmatrix} B \\ C \end{bmatrix} = \left\{ \prod_{t=1}^N \begin{bmatrix} \cos(k_t \tau) & i \sin(k_t \tau) k_0 / k_t \\ i \sin(k_t \tau) k_t / k_0 & \cos(k_t \tau) \end{bmatrix} \right\} \begin{bmatrix} 1 \\ n_0 \end{bmatrix}. \quad (5)$$

For the numerical calculations, we used  $n(x, \nu) = \sqrt{\varepsilon_{eff}(x, \nu)}$  to obtain the refractive index inside the GCS-monolayer region  $|x| < D/2$ .

The aforementioned equations were applied in the next section to the description and to the analysis of the experimental data.

## C. Comparison between experiment and modelling

The electromagnetic response of the GCS-based monolayer without metal plate, either measured in waveguide or modelled in the Ka-band, is given in Fig. 7(a). From this figure, it can be seen that the free-standing monolayer absorbed about 24% of the initial radiation power. However, the absorption properties of the monolayer could be significantly improved when a metal plate is located beneath the monolayer. The corresponding  $S_{11}$ -parameters are presented in Fig.7(b). In this case, the absorption coefficient  $A = 1 - S_{11}^2$  indeed varied in the range 30-94%. Additionally, the interference minimum of the signal reflected from GCS-monolayer could be shifted by varying the width of the air gap between the monolayer and the metal plate (Fig.7(c)). The combination of GCS-based monolayer, an air gap ( $l = 6.1$  mm) and a metal plate thus allows observing experimentally an asymmetric and sharp absorption peak with a maximum at about  $A = 84\%$ . The position of this peak was quite well predicted by the modelling.

In Fig.7(a)-(c), a good agreement can be observed between experiments and modelling for the three independent measurements. **The maximum absolute difference between experimental data and results of theoretical modeling in Fig.7 (a), (b), (c) is 0.09, 0.04, 0.27, respectively. We can see that the best correlation between experiment and modeling is for GCS monolayer located on a metal plate.**

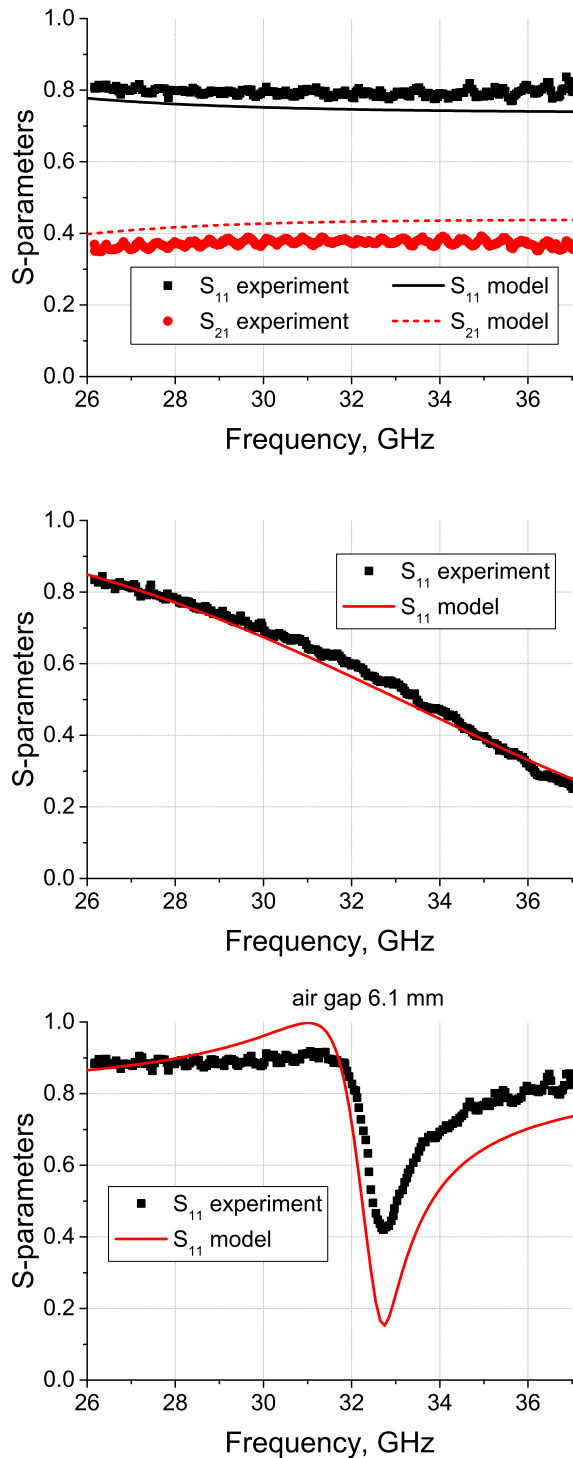


FIG. 7. Comparison of experimental (full circles and squares) and theoretical (lines) results in waveguide: (a)  $S_{11}$ - and  $S_{21}$ -parameters of a free-standing 0.79-mm thick GCS-monolayer; (b)  $S_{11}$ -parameters of the same GCS monolayer located on a metal plate; (c)  $S_{11}$ -parameters of the GCS monolayer separated from the metal plate by an air gap of width  $l = 6.1$  mm.

When the GCS is in the form of a monolayer separated from the metal plate by an air gap of width 6.1 mm, the divergence near 33 GHz is maximal but the shape of the peak and its position still are in good agreement with the modelling. The possible reason for some deviation between modelled and measured S-parameters in Fig.7 is the inhomogeneity of diameters of the real porous GCSs forming the monolayer. Nevertheless, the obvious coincidence between experiment and theory confirms the relevance of the model presented here, and allows using it to predict the electromagnetic response as well as the absorption properties in free space and in a broader frequency range, as discussed below.

## V. ABSORPTION PROPERTIES IN FREE SPACE

(b)

The results presented above were obtained with waveguide-based measurements. These are indeed the most accurate and widely developed techniques for investigating electromagnetic properties in dielectric spectroscopy. However, the most important practical use of microwave absorbers is associated with the free space applications. Eq.(4)-(5) can be also applied in free space but, in such a case, wave vectors  $k_z = 2\pi/\lambda$  and  $k_{2z} = 2\pi\sqrt{\epsilon}/\lambda$  should be used.

To investigate the absorption properties of GCS-based monolayers on a PEC plate at a normal incidence angle in free space, we varied parameters such as the diameter of the GCS and the width of the air gap between the monolayer and the PEC plate. Additionally, for better understanding the absorption properties, we extended the modelling from the relatively narrow Ka-band to the frequency range from 1 up to 40 GHz. This allowed having an overall view of the expected microwave absorbing properties and estimating the optimal parameters for a further practical use of GCS metasurfaces.

(c)

It is worth noting that diameter of GCS is the most important geometrical parameter in the considered system. Additionally, air gap is the most flexible, “easy to change” parameter defining electromagnetic response. The variation of both parameters significantly affects the electromagnetic response of GCS monolayer and presents the general features of absorbing properties of GCS-monolayers in microwaves.

### A. Diameter dependence

The dependence of the absorption coefficient of a GCS-based monolayer on frequency and diameter in free space is presented in Fig.8.

It can be seen from Fig.8 that the first absorption maximum (wherein absorption is 100%) is shifted towards lower frequencies when the GCS diameter increases. Both width and height of such peak remain prac-



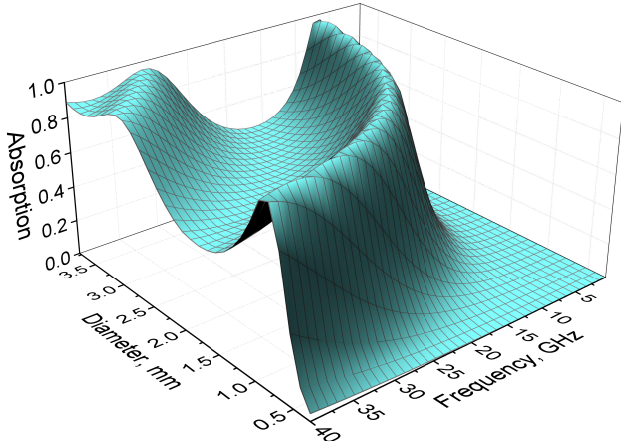


FIG. 8. Dependence of absorption coefficient of GCS-monolayer on frequency and diameter in free space.

tically constant. For larger diameters, a second, wider maximum appears. This maximum may be used in practice for designing broadband absorbers.

It is interesting to compare those results with the absorbing properties of a lossy homogeneous plane parallel plate of thickness  $\tau$  and permittivity  $\varepsilon = 1 - i\sigma/\omega\varepsilon_0$  located on a PEC plate. In Fig.8 the first maximum in the Ka-band can be achieved with spheres of diameter about 1 mm. The modelling of a plane parallel plate with  $\varepsilon = 1 - i\sigma/\omega\varepsilon_0$  shows that, in this case, the same first maximum may also be achieved in the Ka-band only for a minimal thickness of about 2.5-3 mm. The latter result shows that the GCS-based monolayer is much more compact than a plane parallel plate. Such advantage of GCS metasurface may be very important for aerospace applications for example.

Additionally, from the symmetry of the 3D-surface presented in Fig.8 we can see that a change of diameter is equivalent to a change of frequency. This result is evident because, in the case of free space, Eq.(5) depends only on the simple product of thickness  $\tau$  and frequency  $\nu$ . Therefore, the variations of both parameters in free space are equal. As in the case of hollow carbon spheres<sup>12</sup> we see from Fig.8 that for broadband absorption applications the spheres with larger diameter are preferable.

### B. Air gap dependence

The dependence of the absorption coefficient of a GCS-based monolayer on frequency and air gap width in free space is presented in Fig.9.

Fig.9 shows that the increase of the air gap makes the first absorption maximum decrease and be shifted to lower frequencies. The second maximum is clearly asymmetric, and sharper than the former one. This second

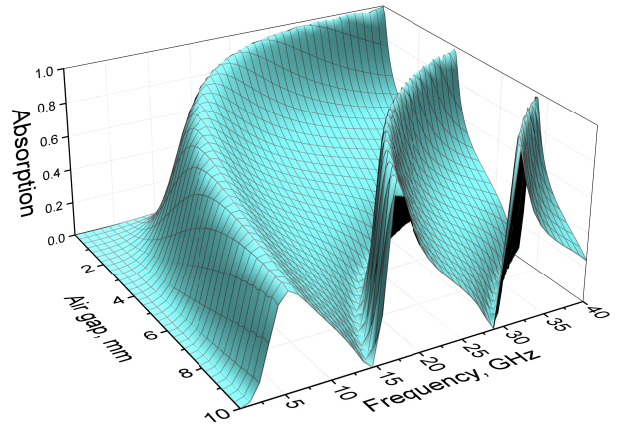


FIG. 9. Dependence of absorption coefficient of GCS-monolayer on frequency and air gap width in free space.

maximum was exactly the one observed experimentally in the waveguide (Fig. 7(c)) at a frequency near 33 GHz. In Fig.9 it is shifted to a lower frequency (near 26 GHz) due to the difference of wave vectors in free space and in a waveguide. Usually, if the interference absorption maximum is observed in the waveguide at a frequency  $\nu_{wg}$ , it is also expected in free space at a frequency  $\nu_{fs}$ . In most cases, such shift of frequency can be roughly estimated by the following equation<sup>45</sup>:

$$\nu_{wg}^2 - \nu_{fs}^2 = \frac{c^2}{4a^2}, \quad (6)$$

where  $c$  is the speed of light in vacuum and  $a$  is the width of the waveguide. At highest values of air gap, a third maximum also appears. The latter is even sharper than the second peak. The asymmetry and the variations between first, second and third maxima are important differences between the GCS metasurface presented here and traditional lossy homogeneous plane parallel plate of thickness  $\tau$  and dielectric permittivity  $\varepsilon = 1 - i\sigma/\omega\varepsilon_0$ . In the case of plane parallel plate, the first maximum indeed does not decrease with air gap and the second and third maxima are symmetric and equivalent to the first one. We assume that this special feature of GCS-based monolayer may find some practical applications in the future, for example for designing frequency-selective filters.

Also noteworthy is that the microwave absorption performances of the GCSs monolayers considered here are generally comparable with those of other absorbers presented recently<sup>16-18</sup> (the absorption mechanism is classical Ohmic losses in conductive medium). These recent reports generally deal with materials based on polymer matrix and their operating temperature range is usually limited below 200-300° C. In contrast, the glassy

carbon considered here is thermally stable in air up to a temperature of 400° C, and even up to 3000° C in vacuum<sup>46</sup>.

## VI. CONCLUSIONS

Porous glassy carbon spheres (GCSs), assumed to have a purely imaginary dielectric permittivity  $\varepsilon = 1 - i\sigma/\omega\varepsilon_0$ , were used for obtaining a microwave-absorbing metasurface. Spherical particles arranged in a periodic structure indeed allowed obtaining a metamaterial with graded real and imaginary parts of effective dielectric permittivity (see Fig.6).

A detailed comparison of the absorption properties of the aforementioned GCS-based metasurface with those of a homogeneous lossy plane parallel plate of thickness  $\tau = D$  and permittivity  $\varepsilon = 1 - i\sigma/\omega\varepsilon_0$  located on a PEC plate led to the following differences, features and advantages of the new heterostructure presented here:

- the experimental waveguide measurements showed that GCS monolayers absorb up to 92% of the initial microwave radiation power in the Ka-band;
- theoretical predictions showed that absorption peaks in free space may be effectively tuned by varying the width of the air gap and the diameter of the GCSs;
- the GCS monolayer is a compact absorber. The same absorbing parameters can indeed only be achieved with a conductive plane parallel plate presenting a significantly higher thickness;
- the carbon material presented in this manuscript may be applied as broadband or as resonant absorber, depending on the width of the air gap;
- tuning the air gap allows obtaining asymmetric absorption peaks, which might be potentially used in microwave filter applications.

Finally, it is also worth mentioning that the material considered here is thermally stable, inert, easy to prepare and cheap. These features of GCS make them very attractive for designing new, effective microwave-absorbing coatings.

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