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Drying in nanoporous media with Kelvin effect: capillary imbibition against evaporation by smoothed particle hydrodynamics method.

Nathan Amrofel^{1,*}, Magdalena Dymitrowska², Amaël Obliger³, Anne-Julie Tinet¹ and Fabrice Golfier¹

¹ Université de Lorraine, CNRS, GeoRessources, F-54000 Nancy, France

² PSE-ENV/SPDR/LETIS, Institut de Radioprotection et de Sécurité Nucléaire (IRSN), Fontenay-aux-Roses, France

³ Institut des Sciences Moléculaires, Université de Bordeaux – Bordeaux INP – CNRS, UMR 5255, F-33400 Talence, France

* Corresponding author: Bâtiment E - 2 rue du Doyen Marcel Roubault - 54505 Vandoeuvre-lès-Nancy CEDEX - France • 0.(033)7.50.90.42.72 • nathan.amrofel@univ-lorraine.fr

Understanding drying processes in nanoporous media is of great importance in many technological and industrial situations. To better understand how gas moves through clayey rocks, of interest for underground disposal of radioactive wastes, we propose using pore-scale direct numerical simulations. In this study, we use the Smoothed Particle Hydrodynamics method, which has proved to be an effective approach for simulating complex fluid dynamics within porous media at the nanoscale. Our simulations consider capillary-dominated two-phase flow with evaporation and condensation at liquid-gas interfaces, coupled to the diffusion of water vapor in the gas phase, as well as the Kelvin effect, which is a specific feature of nanopores. Our evaporation-condensation model is validated against analytical solutions. The size of the compact support of kernel function and the particle density required to obtain accurate and stable results of capillary pressure are investigated. Drying regimes, capillary-driven and evaporated-driven, are explored. A specific effort is made to highlight the influence of the Kelvin effect on desaturation and the creation of preferential paths for gas flow, as well as its impact on drying rate. The role of condensation due to local vapor concentration conditions is also emphasized.

Keywords: Liquid dynamics - Nanoporous media – Kelvin effect – Evaporation – Condensation

- 1 1. Introduction
- 2 Deep geological radioactive waste disposal projects usually foresee the burial of large quantities of
- 3 metallic materials used for waste packaging and support elements, or incorporated as waste itself.

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4 After closure of a repository, a significant amount of hydrogen is expected to be produced by both
5 anaerobic corrosion and water hydrolysis [38]. In the case of the French Cigéo project, it is estimated
6 that gas production will exceed the diffusion capabilities of the Callovo-Oxfordian (COx) host rock and
7 that a distinct gas phase will appear [3,14]. For the long-term safety assessment of a repository, it is
8 essential to thoroughly investigate how gas generation, accumulation and migration can affect its
9 predefined properties. In particular, heat and mass transfer between the gas phase and the water-
10 saturated pores of the host rock are expected, leading to progressive desaturation of some pores.
11 Mass transfer of water from the liquid to the gas phase can facilitate gas phase propagation into the
12 clay matrix and lead to formation of new percolating pathways that would otherwise be unavailable
13 due to insufficient gas pressure as compared to the gas entry pressure [32]. On the opposite, pore
14 resaturation may also occur locally through condensation, driven by changes in relative humidity or
15 temperature differences between the gas phase and the rock surface, which would contribute to
16 stabilizing the advancement of the drying front.

17 Mass transfer phenomena between phases are controlled by thermodynamic conditions at the liquid-
18 vapor interfaces within the pores, and these evaporation-condensation processes have been largely
19 studied in the context of porous media drying [2,24,32,40,45]. Direct numerical simulation methods
20 are still being developed and improved to simulate the process of evaporation, such as the volume-
21 of-fluid method[11,41,43], molecular dynamics[6,23,55], the level set method[31,37] and Smoothed
22 Particle Hydrodynamics (SPH)[50,53]. However, the competition between drying forces (driven by
23 vapor-liquid equilibrium conditions and thus by the equality of chemical potentials) and capillary forces
24 (i.e., surface tension) becomes exacerbated as pore size decreases. Evaporation is also closely
25 linked to diffusion, which usually prevails for low-permeability materials, since diffusion defines the
26 ability of the gas phase to transport water vapor molecules away from the fluid interface and hence
27 may limit the evaporation rate. As a consequence, the prediction of drying patterns in nanoporous
28 materials remains particularly challenging and not fully understood [2,32]. The equilibrium vapor
29 concentration, and therefore the capacity of the gas phase to accommodate water molecules in the
30 vicinity of the water-gas interface, is generally defined through the Kelvin-Laplace equation [4]. This

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31 relationship links thermodynamic conditions and capillary phenomena. In other words, the ability of
32 the gas phase to contain water molecules at a given scale is depends on temperature and the local
33 pressure difference between phases [15]. Also, some extensions of the Kelvin equation have been
34 developed, taking into account multicomponent fluids and real gas effects [51]. For pores smaller than
35 8nm diameter, it is accepted that fluid properties vary across the pore, which strongly influences the
36 validity of the Kelvin equation [4,56]. However, Boğan et al. [8] have recently demonstrated using
37 molecular dynamics simulation the relevance of the continuous medium hypothesis for pore diameter
38 greater than 3nm within a clayey material when slip conditions are used. This finding was supported
39 experimentally by Yang *et al.* [52], who have shown that the Kelvin equation remains valid at a
40 scale comparable to the size of water molecules in strongly hydrophilic capillaries.

41 Up to now, many studies have investigated fluid behavior and vapor transport in nanopores. Various
42 and complex evaporation models have been developed where interfacial tension, disjoining pressure,
43 rarefaction effect, and real gas effect [20] are taken into consideration under thermodynamic
44 equilibrium or non-equilibrium conditions [28,30,47] but Kelvin effect has still been neglected. In
45 contrast, other researchers [33,51] have focused on the capillary condensation phenomenon driven
46 by the Kelvin effect. Nanopore deformation induced by condensation has been also revealed by
47 Günther et al. [22]. Their works have provided insights into the influence of nanopore geometry on
48 gas dynamics coupled with liquid-vapor mass transfer. However, all of these studies remain limited to
49 a single nanopore and cannot capture the dynamics of evaporation fronts at the pore network scale.
50 The main purpose of this study is to address this limitation.

51 The COx claystone presents a large pore size distribution centered between 1-100 nm, and the
52 mesopores, i.e., between 2 and 50 nm [3] are likely to dominate its flow and transport properties.
53 Thus, they remain within the range of validity of the Kelvin-Laplace equation. Modeling the
54 evaporation process independently aims to study its role in easing gases migration into the clay rock
55 in spite of important capillary pressure. Several approaches can be used for extensive pore-scale
56 modeling. For the smallest pore sizes, molecular dynamics is preferred when validity the validity of
57 continuum approaches is questionable, but is limited to single or double nanopores [54] due to

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58 excessive computational costs. On the other side, pore network models (PNM) are largely used to
 59 simulate drying patterns in larger mesoporous systems, but this phenomenological approach suffers
 60 from limitations due to physical or geometrical simplifications when it comes to the understanding of
 61 the drying mechanism [27,32]. A recent PNM study including Knudsen and Kelvin effects [32] has,
 62 however, highlighted drastic impact of the latter phenomenon on drying patterns. In our work, the SPH
 63 method has been used because of its ability to deal with interface problems while preserving a fine
 64 description of physical processes [29,34,36]. An in-house SPH code has been recently developed at
 65 IRSN, capable of simulating two-phase flow in a 3D porous medium sample [17,18,39]. A drying
 66 algorithm with Kelvin effect, vapor diffusion, and water evaporation-condensation has been
 67 implemented for the purpose of this study. The objective is to examine the contribution of various
 68 mechanisms at stake and the role of coupling between these processes into the drying pattern
 69 dynamics. To our knowledge, such study has never been conducted at the pore scale.

70 The structure of the article is as follows. The physical phenomena that our model takes into
 71 consideration are presented in Section 2. Section 3 provides numerical discretization of the model
 72 equations. In Section 4, after preliminary validation tests, we investigate the impact of the Kelvin effect
 73 impact on 2D pore networks through simulations and present a sensitivity analysis of model
 74 parameters. Finally, in Section 5 we resume our conclusions and discuss some perspectives for
 75 application of our work within radioactive waste geological disposal projects.

76 2. Conceptual model

77 We consider hereafter a rigid porous medium whose solid skeleton constitutes s -phase, such as the
 78 one sketched in Figure 1. The pore space is composed of mesopores, large enough so that a
 79 continuum approach can be applied everywhere. The medium is initially fully saturated with liquid
 80 (wetting phase, denoted by subscript w) in contact with gas (non-wetting phase, denoted by subscript
 81 g). Figure 1 illustrates the overall phenomena at the scale of an idealized 2D pore network and with
 82 a focus on an isolated pore. The phenomena considered at the pore scale in the present model are

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83 vapor diffusion in the gas phase, the capillary effects (contact angle, surface curvature and tension
84 resulting in pressure difference), evaporation and condensation including Kelvin effect,

85 Due to low permeability of the CO_x host rock, we consider the assumption of slow drying so that we
86 have low Reynolds and Péclet numbers during our simulations. Given small characteristic length scale
87 of the computational domain (less than a micrometer), gravity effect, density and temperature
88 gradients are neglected. Fluid-solid interactions and the resulting disjoining pressure are also not
89 taken into account [26]. Temperature is assumed to be constant in the system.

90 Water is present in gaseous (vapor) and liquid phases, and mass transfer process at gas/water
91 interfaces is controlled by Kelvin-Laplace equation. Gas phase is considered to be composed of two
92 components: water vapor and hydrogen. In nano- and micropores, water vapor partial pressure is
93 much too low to maintain mechanical equilibrium at liquid-gas interface. Therefore, the total pressure
94 in the gas phase will be treated as constant, irrespective of variations in vapor concentration. In
95 addition, low solubility of hydrogen allows us to neglect its dissolution and diffusion in liquid phase.
96 Finally, owing to strong adsorptive surface forces present in the CO_x rock, it is expected that thin
97 water films subsist at the surface of clay minerals even after drainage [21]. While not directly
98 considered in our model, slippage characteristic length at the gas/fluid interface should be relatively
99 small, and thus we will neglect rarefaction effects. According to [32], the Knudsen effect does not
100 have either a significant influence on the resulting gas invasion pattern which supports this
101 assumption. In any case, considering Knudsen diffusion would lead to reduce the diffusion coefficient.
102 Such parameter variation effect on the evaporation rate and the drying pattern can be analyzed
103 through the modification of the governing dimensionless numbers as discussed hereafter (see Section
104 5)

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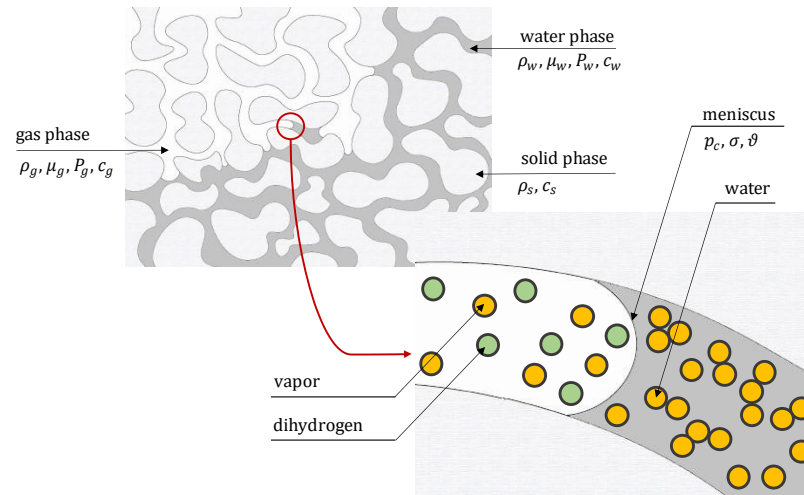


Figure 1: Schematic description of the nano-porous system as considered in this work. Gas phase progresses into clay matrix due to evaporation and diffusion of pore liquid in the form of vapor from liquid/gas interfaces.

105 In the following sections, the physical model and the associated equations will be detailed. We will
 106 start by presenting how the flows are modeled, taking into account transfer processes. Then, we will
 107 focus on the boundary and interface conditions.

108 2.1. Pore-scale equations

109 Description of motion of fluids as continuous phases is useful to establish force equilibrium at
 110 liquid/gas interface. At pore scale, Navier-Stokes equations in their simplified forms [42] are used to
 111 model two-phase flow of weakly compressible fluids at low Reynolds numbers. There is no external
 112 pressure acting as a driving force for fluid motion. However, particle displacements still occur, induced
 113 by capillary forces either locally from the deformation of the liquid-gas meniscus, or at the scale of the
 114 pore network where a pressure gradient may be generated by difference in capillary pressures
 115 between pore throats of different diameters. Note that all mass balance equations will be expressed

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116 in Lagrangian formulation with the material derivative denoted D/Dt . The mass conservation for fluid
 117 phases is then stated as:

$$118 \quad \frac{D\rho_{w,g}}{Dt} = -\rho_{w,g}\nabla\cdot\mathbf{v}_{w,g} \quad (1)$$

119 with ρ density and v velocity of fluid. Indices w or g indicate the phase described (w liquid, g gas).

120 For Newtonian fluids, the momentum equations can be expressed as:

$$121 \quad \rho_{w,g}\frac{D\mathbf{v}_{w,g}}{Dt} = -\nabla p_{w,g} + \mu_{w,g}\Delta\mathbf{v}_{w,g} \quad (2)$$

122 with μ the dynamic viscosity of fluid and p local pressure of the fluid. Equation (2) can be also
 123 presented in its dimensionless form as:

$$124 \quad Re_{w,g}\frac{D\mathbf{v}'_{w,g}}{Dt'} = -\frac{1}{Ca_{w,g}}\nabla p'_{w,g} + \Delta\mathbf{v}'_{w,g} \quad (3)$$

125 with $Re_{w,g} = \rho_{w,g}v_{int}L/\mu_{w,g}$, $Ca_{w,g} = \mu_{w,g}v_{int}/\sigma_{wg}$, L is the characteristic length (i.e., pore-throat
 126 size), v_{int} is an average drying velocity and σ_{wg} is the surface tension coefficient between gas and
 127 water phases. We used the following variables: $x' = x/L$, $t' = t v_{int}/L$, $\mathbf{v}'_{w,g} = \mathbf{v}_{w,g}/v_{int}$ and $p' =$
 128 $p_{w,g} L/\sigma_{wg}$. Similar definitions hold for momentum equation in gas phase, but we will only use Re_w
 129 and Ca_w in our analysis since we will keep the density and viscosity ratio (or mobility defined as $M =$
 130 μ_w/μ_g) equal to one in our simulations. Such an assumption allows for a more efficient computation
 131 using SPH and remains acceptable as gravitational and viscous effects (low capillary number) are
 132 negligible compared to other phenomena in the present study. The interface displacement velocity
 133 v_{int} being expected to be very low, Reynolds number will be low enough to neglect inertial terms. In
 134 addition, the continuity of the viscous stress tensor will be ensured at fluid-fluid interfaces. The
 135 pressure p will be linked to density ρ using a linear compressibility relation :

$$136 \quad p_{w,g} = c_{w,g}^2(\rho_{w,g} - \rho_{w,g}^0) \quad (4)$$

137 with c speed of sound, often used as a numerical parameter [12,13], and ρ^0 some reference fluid
138 density.

139 The vapor can be considered as a tracer component, and we will solve mass transport by using a
140 simple advection-diffusion equation. The most important physical parameter is then the saturated
141 vapor concentration C_s , which is the maximum vapor concentration possible in the system at a given
142 temperature. To model the diffusion of vapor in gas phase, Fick equation is used [7,16] as follows:

$$143 \quad \frac{DC}{Dt} = \nabla \cdot (D_v \nabla C) \quad (5)$$

144 with C vapor concentration in gas phase and D_v vapor diffusion coefficient. The dimensionless form
145 of equation (5) is:

$$146 \quad \frac{DC'}{Dt'} = \nabla \cdot \left(\frac{1}{Pe} \nabla C' \right) \quad (6)$$

147 where Péclet number is defined by $Pe = v_{int} L / D_v$ and dimensionless vapor concentration C' is
148 equivalent to relative humidity such as $C' = C / C_s$.

149 Finally, to further interpret and identify the drying patterns, a dimensionless evaporation-capillary
150 number ε will also be introduced. It is calculated as ratio between characteristic times of evaporation
151 and capillarity. Inspired by [5,25,46], the formulation was modified to take into account pore-scale
152 features and Kelvin effect. It can be written as follows:

$$153 \quad \varepsilon = 12 \frac{Ca_w}{Pe} \Delta C' C'_s \quad (7)$$

154 with $\Delta C' = \frac{C_{eq} - C_{in}}{C_s}$ and $C'_s = \frac{C_s}{\rho_w}$. A construction of ε can be found in Appendix A.2.

155 2.2. Boundary conditions

156 Given mostly nanometric pore size distribution of COx and our model assumptions, we will use Kelvin
157 equation (8) to locally define equilibrium vapor concentration at each liquid-gas interface. It defines

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158 the change in ability of gas phase to accommodate water molecules, making a link between
159 thermodynamic conditions and capillary phenomena:

$$160 \quad \frac{C_{eq}}{C_s} = \exp\left(-\frac{P_c M}{\rho_w R T}\right) \quad (8)$$

161 where C_{eq} is equilibrium vapor concentration induced by capillary forces at curved meniscus, C_s is
162 saturated vapor concentration, P_c capillary pressure, M is molecular weight of vapor, ρ_w density of
163 liquid water, R universal gas constant, and T temperature. As stated before, we consider liquid phase
164 to be saturated with all other components of the gas phase so that gases dissolution and diffusion in
165 water can be neglected.

166 The difference in intermolecular interactions and/or density between two immiscible fluids causes
167 surface tension effects at the interface between them. The resulting macroscopic force acting on
168 particles near this interface tends to minimize its surface, and in presence of a solid surface with a
169 wettability difference, it generates a pressure jump P_c between the two fluids. In presence of a solid
170 phase forming a capillary tube, the law describing capillary pressure is classically written as [19]:

$$171 \quad P_c = p_g - p_w = \sigma_{wg} \nabla \cdot \hat{\mathbf{n}} \quad (9)$$

172 where surface tension σ_{wg} is considered constant along the interface with $\hat{\mathbf{n}}$ unit vector normal to the
173 interface. The description of interfaces between two immiscible fluids is a critical point of multiphase
174 flow modeling by continuous methods. Capillary pressures generated at the scale of nanoscopic pores
175 are significant (up to several tens of MPa). Under such conditions, a redistribution of pore water from
176 larger to smaller pores occurs. Finally, at the fluid/solid interface a no-slip condition is imposed:

$$177 \quad \mathbf{v}_{w,g}(\mathbf{r}_i) = 0 \quad (10)$$

178 where $\mathbf{v}_{w,g}$ denotes velocity of the fluid. Zero flux conditions are therefore applied to the walls, and
179 mass is perfectly conserved in the system. No vapor mass transfer is supposed between gas and
180 solid phases, and we have:

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181
$$D_v \nabla C \cdot \mathbf{n}_s = 0 \quad (11)$$

182 where \mathbf{n}_s is normal unit vector orthogonal to interface and pointing toward solid wall. Dirichlet condition
183 will be applied to one external surface of porous medium:

184
$$C = \gamma \quad (12)$$

185 where γ is a constant. This condition will simulate contact with controlled-humidity air, while a no-flux
186 condition will be imposed on the opposite side. The boundary conditions presented above, for each
187 phase and for each phenomenon considered, will be applied in all simulations presented in this article.

188 3. Numerical model

189 In this section, a brief introduction to basic principles of SPH method will be provided, and the set of
190 equations for evaporation-condensation model that has been presented above will be discretized.
191 The flow equations and the curvature model have been previously presented in detail [39] and will be
192 only briefly recalled.

193 3.1. SPH method

194 Among the methods for simulating the hydro-mechanical behavior of continuous media, the SPH is
195 characterized by the absence of fixed mesh, its Lagrangian nature, and its remarkable adaptability to
196 massive parallelization due to its quasi-local structure. Indeed, the medium is discretized by a cloud
197 of material points of constant mass, and for each equation of movement is solved. In the case of
198 fluids, these material points are often referred to as particles.

199 The starting point of SPH method is a convolution of a function $f(\mathbf{x})$ by Dirac delta function δ as
200 follows:

201
$$f(\mathbf{x}) = \int_{\Omega} f(\mathbf{x}') \delta(\mathbf{x} - \mathbf{x}') d\mathbf{x}' \quad (13)$$

202 where \mathbf{x} and \mathbf{x}' denote positions. The properties of the Dirac delta function being $\delta(\mathbf{x} = 0) = +\infty$,
 203 $\delta(\mathbf{x} \neq 0) = 0$ and $\int_{-\infty}^{+\infty} \delta(\mathbf{x}) d\mathbf{x} = 1$. To create a numerically useful approximation of $f(\mathbf{x})$ denoted $\langle _ \rangle$,
 204 the singular form of δ is replaced by a smoothing kernel function $W(\mathbf{x} - \mathbf{x}', h)$ such as:

$$205 \quad \langle f(\mathbf{x}) \rangle = \int_{\Omega} f(\mathbf{x}') W(\mathbf{x} - \mathbf{x}', h) d\mathbf{x}' + O(h^2) \quad (14)$$

206 with h the smoothing length, and such that:

$$207 \quad W(\mathbf{x} - \mathbf{x}', h) = 0 \quad (15)$$

208 for $(\mathbf{x} - \mathbf{x}') \geq h$.

209 To ensure the consistency of the method, the kernel function $W(\mathbf{x} - \mathbf{x}', h)$ must also fulfill the
 210 following conditions:

$$211 \quad \left\{ \begin{array}{l} \lim_{h \rightarrow 0} W(\mathbf{x} - \mathbf{x}', h) = \delta(\mathbf{x} - \mathbf{x}') \\ \int_{\Omega} W(\mathbf{x} - \mathbf{x}', h) d\mathbf{x}' = 1 \end{array} \right. \quad (16)$$

212 Finally, discrete approximation $\langle _ \rangle$ of equations (14) is constructed by replacing the continuous
 213 form by a sum over a set of material points such that:

$$214 \quad \langle \langle f(\mathbf{x}_a) \rangle \rangle = \sum_{b=1}^N \frac{m_b}{\rho_b} f(\mathbf{x}_b) W(\mathbf{x}_a - \mathbf{x}_b, h) \quad (17)$$

$$215 \quad \langle \langle \nabla f(\mathbf{x}_a) \rangle \rangle = \sum_{b=1}^N \frac{m_b}{\rho_b} f(\mathbf{x}_b) \nabla W(\mathbf{x}_a - \mathbf{x}_b, h) \quad (18)$$

$$216 \quad \langle \langle \nabla \cdot f(\mathbf{x}_a) \rangle \rangle = - \sum_{b=1}^N \frac{m_b}{\rho_b} f(\mathbf{x}_b) \cdot \nabla W(\mathbf{x}_a - \mathbf{x}_b, h) \quad (19)$$

217 with $V_b = m_b/\rho_b$ the volume associated with the material point b , m_b its mass, and ρ_b its density.

218 The cubic B-spline function proposed by Monaghan et al. [35] has been used as kernel W :

$$219 \quad W(\mathbf{x}_a - \mathbf{x}_b, h) = \xi \begin{cases} \frac{2}{3} - r^2 + \frac{1}{2}r^3 & 0 \leq r < 1 \\ \frac{(2-r)^3}{6} & 0 \leq r < 2 \\ 0 & r \geq 2 \end{cases} \quad (20)$$

220 where r is the normalized spacing between particles given by $\|\mathbf{x}_a - \mathbf{x}_b\|/h$, and ξ is a parameter
 221 depending on whether the domain is defined in one, two, or three dimensions (respectively $1/h$,
 222 $15/(7\pi h^2)$, and $3/(2\pi h^3)$).

223 3.2. Flow equations

224 SPH version of the continuity equation can be written as:

$$225 \quad \frac{D\rho_a}{Dt} = \rho_a \sum_b \frac{m_b}{\rho_b} (\mathbf{v}_a - \mathbf{v}_b) \cdot \nabla W(\mathbf{x}_a - \mathbf{x}_b, h) \quad (21)$$

226 It is common to replace it by a simpler formulation, the SPH discretization equation (1) of the density
 227 field, which guarantees an exact conservation of the mass:

$$228 \quad \rho_a = \sum_b m_b W(\mathbf{x}_a - \mathbf{x}_b, h) \quad (22)$$

229 The momentum conservation equation can be written as follows:

$$230 \quad \frac{D\mathbf{v}_a}{Dt} = - \sum_b \left(\frac{p_b}{\rho_b^2} + \frac{p_a}{\rho_a^2} \right) m_b \nabla W(\mathbf{x}_a - \mathbf{x}_b, h) \\ + \sum_b \frac{4\mu_a\mu_b}{\mu_a + \mu_b} \frac{m_b}{\rho_b\rho_a} \frac{\mathbf{v}_a - \mathbf{v}_b}{\|\mathbf{x}_a - \mathbf{x}_b\|} \frac{\partial W(r_{ab}, h)}{\partial r_{ab}} + \frac{\mathbf{F}_s}{\rho_a} \quad (23)$$

231 Combined with a method to determine forces at the interfaces, presented hereafter, the Navier-Stokes
 232 equation solved in both phases allows the establishment of a smooth fluid-fluid interface.

233 3.3. Curvature

234 We use the continuum surface force (CSF) model initially developed by Brackbill et al. [10] and widely
 235 adapted and used in the SPH framework [48]. It assigns a constant color value to each particle in a
 236 given phase (liquid, gas, solid). The most straightforward approach is to assign to liquid and gas SPH

237 particles color parameters $c_w = -1$ and $c_g = 1$, respectively. Then constant color value assigned to
 238 the solid phase is:

$$239 \quad c_s(\mathbf{x}) = \cos(\vartheta) \quad (24)$$

240 with ϑ contact angle between liquid and solid phases. Then it is possible to calculate $\hat{\mathbf{n}}$, the unit vector
 241 normal to the interface:

$$242 \quad \hat{\mathbf{n}} = \frac{\nabla c(\mathbf{x})}{\|\nabla c(\mathbf{x})\|} \quad (25)$$

243 The local curvature of the interface κ can be calculated as:

$$244 \quad \kappa = -\nabla \cdot \hat{\mathbf{n}} \quad (26)$$

245 To generate curvature at the liquid-gas interface, a volumetric surface tension force $\mathbf{F}_{ts}(\mathbf{r})$ is
 246 computed, the magnitude of which is proportional to the local curvature of the interface κ :

$$247 \quad \mathbf{F}_{ts}(\mathbf{x}) = \frac{1}{2} \sigma_{wg} \kappa \mathbf{n} \quad (27)$$

248 For improved precision, special treatment following [1,44] is added to the color fields and to forces
 249 applied at the triple contact line (2D) to obtain equilibrium contact angle ϑ .

250 Within the SPH method, the color field is obtained as follows:

$$251 \quad c(\mathbf{x}_a) = \sum_{b=1}^N \frac{m_b}{\rho_b} c_b W(\mathbf{x}_a - \mathbf{x}_b, h) \quad (28)$$

252 The color function gradient vector is calculated by discretizing equation (28) as:

$$253 \quad \mathbf{n}(\mathbf{x}_a) = \sum_{b=1}^N \frac{m_b}{\rho_b} (c(\mathbf{x}_b) - c(\mathbf{x}_a)) \nabla W(\mathbf{x}_a - \mathbf{x}_b, h) \quad (29)$$

254 This allows us to determine the interface local curvature κ given by (26) as:

$$\kappa(\mathbf{x}_a) = \frac{1}{\|\mathbf{n}(\mathbf{x}_a)\|^2} \sum_{j=1}^N \frac{m_b}{\rho_b} (\mathbf{n}(\mathbf{x}_b) \|\mathbf{n}(\mathbf{x}_a)\| - \mathbf{n}(\mathbf{x}_a) \|\mathbf{n}(\mathbf{x}_b)\|) \cdot \nabla W(\mathbf{x}_a - \mathbf{x}_b, h) \quad (30)$$

256 Following the calculation of κ , the local resultant force $\mathbf{F}_{ts}(\mathbf{r})$ is calculated using equation (27). The
 257 spatial distribution of particles near interfaces is then ruled by the CSF model, taking into account the
 258 contact angle between the wetting and the solid phases.

259 3.4. Evaporation-condensation model

260 In this section, we present the general idea of the evaporation algorithm in which a conversion of
 261 liquid particles into gas ones takes place, as illustrated by Figure 2. We start with diffusive flux from
 262 Eq. (5) that can be discretized as follows:

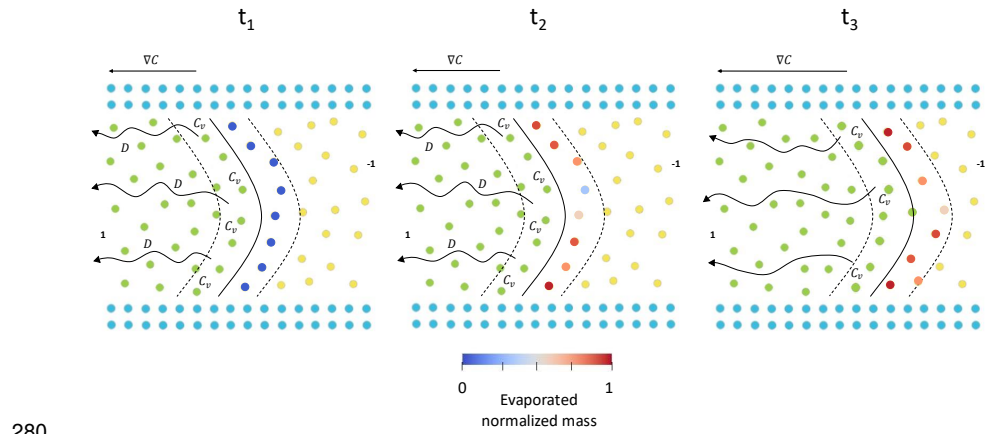
$$\frac{DC}{Dt}(\mathbf{x}_a) = \sum_{b=1}^N \frac{m_b}{\rho_b} 2D_v \frac{(C_a - C_b)}{\|\mathbf{x}_a - \mathbf{x}_b\|} \frac{\partial W(\mathbf{r}_{ab}, h)}{\partial \mathbf{r}_{ab}} \quad (31)$$

264 where $\mathbf{r}_{ab} = \mathbf{x}_a - \mathbf{x}_b$. At each time step, vapor concentration C_{eq} (Eq. 8) driven by the interface
 265 curvature is imposed on gas particles located in the transition band near the liquid interface. The
 266 vapor mass injected at a gas particle i is calculated as $m_{inj} = (C_{eq}(x_i) - C(x_i)) * \frac{m_g}{\rho_g}$, where $C(x_i)$ is
 267 the preexisting vapor concentration at the particle i , m_g is the mass of gas particles and ρ_g is the
 268 density of gas particles. This mass gain is then deduced uniformly from mass counters associated
 269 with fluid particles present around x_i within the compact support of size h so that the total mass
 270 balance is verified. A similar algorithm holds for condensation. This local loss or gain of mass counters
 271 allows, in particular, for proper triggering of particle conversions to minimize mass balance
 272 instantaneous disequilibrium. The ability of gaseous particles to accommodate vapor is renewed by
 273 diffusion of the latter through the gas phase.

274 When the mass counter of a liquid particle reaches a mass loss equivalent to the mass of a liquid
 275 particle, a conversion into a gaseous particle is made and evaporation occurs. Similarly, when a
 276 counter of liquid particle reaches a mass gain equivalent to mass of liquid particle, the nearest
 277 gaseous particle is converted into liquid particle, and condensation occurs. The mass of a newly

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278 condensed water particle is then uniformly subtracted from the mass counters of surrounding
 279 particles.



280

Figure 2: Illustration of SPH evaporation model. Green particles represent vapor-carrying gas, yellow particles represent water, and blue particles are solid rigid walls. The transition band is between the dashed lines. The solid line is the interface. Time t_1 is the initial time, counters are initialized to zero. The time t_2 shows the intermediary time before particle conversion. The time t_3 shows the interface moved after the conversion of some particles.

281 3.5. Numerical stability conditions

282 In the presence of viscous flow, pressure gradients, and capillary effects, minimum time step
 283 conditions must be respected to ensure stability of explicit time integration schemes. The
 284 corresponding CFL condition is detailed below:

285

$$\min \left\{ \begin{array}{l} \Delta t \leq 0.125 \frac{h^2}{9D}, \Delta t \leq \sqrt{\frac{1}{2}(\rho_f + \rho_g)} \frac{h^3}{2\pi\sigma}, \Delta t \leq 0.125 \frac{\rho h^2}{\mu}, \\ \Delta t \leq 0.25 \frac{h}{3c}, \Delta t \leq 0.25 \frac{h}{\|v_{max}\|}, \Delta t \leq 0.25 \frac{h}{\|a_{max}\|} \end{array} \right\} \quad (32)$$

286 4. Validation Tests

287 To verify correct implementation of momentum and mass balance equations in our SPH model, we
 288 compared the numerical predictions to analytical solutions for a series of test cases and assessed the
 289 models' sensitivity to the compact support size h and the number of particles.

290 Each mechanism was first evaluated independently to guarantee the overall performance of the SPH
 291 model. For the sake of comparison, all results and variables will be presented dimensionless, as
 292 defined in Section 2. The different test cases with the corresponding parameter values used in the
 293 simulations are gathered in Table I. The numerical values are set so that dimensionless characteristic
 294 numbers are as close as possible to the real conditions (argillite host-rock in a disposal) while boosting
 295 calculation times and improving convergence. A sensitivity analysis of physical parameters governing
 296 evaporation and condensation processes will be performed in section 5. Some physical values will
 297 be kept constant (e.g., contact angle) for computational purposes but results will be interpreted in
 298 terms of dimensionless numbers to entangle the contribution of different mechanisms and physical
 299 parameters to the drying pattern.

Physical parameters	Symbol	Value	Unit
Liquid dynamic viscosity	μ_w	10^{-3}	Pa.s
Gas dynamic viscosity	μ_g	10^{-4}	Pa.s
Density ratio	ρ_w / ρ_g	1	/
Fluids sound velocities	$c_{w,g}$	5.0×10^{-1}	m.s ⁻¹
Vapor saturation concentration	C_s	19.7	kg.m ⁻³
Surface tension	σ_{wg}	2×10^{-6}	N.m ⁻¹
Contact angle	α	20	°
Characteristic length	L	1×10^{-2}	m
Diffusion coefficient	D_v	1.25×10^{-5}	m ² .s ⁻¹

Table I: Parametrization of studied test cases.

300 4.1. Test case 1: Equilibrium capillary pressure between parallel plates

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301 In order to rigorously calculate Kelvin equation at mesoscopic scale that drives evaporation, the SPH
 302 model must be capable of precisely determining the capillary pressure at liquid-gas interface in
 303 contact with solid walls. The Young-Laplace equation provides an analytical solution for simple
 304 geometries such as the 2D slit:

$$305 \quad P_c = \frac{\sigma_{wg}}{R_c} = \frac{\sigma_{wg} \cos(\vartheta)}{R} \quad (33)$$

306 with R_c radius of curvature of meniscus and R pore radius. The calculation of capillary pressure based
 307 on this equation and using mean curvature is evaluated in our SPH code.

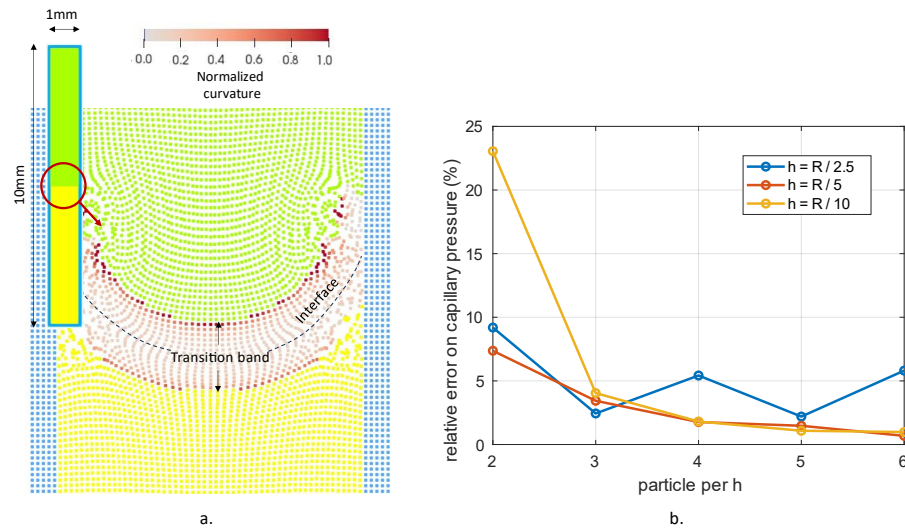


Figure 3: Verification of the SPH capillary model. a) Computational domain with a zoom on the gas-liquid interface with the solid phase in blue, the gas phase in green, and the liquid phase in yellow and red for curvature values inside the transition band. b) Relative error of numerical capillary pressure with respect to the Young-Laplace formula as a function of particle density.

308 We start from a closed, non-equilibrium system with two non-miscible phases (gas and water)
 309 separated by an initially flat interface. The two-dimensional simulation domain is shown in Figure 3a.

310 The pressure is initially the same for both fluids, and we let the system converge to mechanical
 311 equilibrium. For a given contact angle, surface tension, and constant total mass within the system,
 312 the interface between two fluids gets deformed as a result of the influence of surface tension on each
 313 phase. A pressure difference then arises at the curved interface, as predicted by the Young-Laplace
 314 equation (33). After smoothing and normalizing the curved interface using the CSF model, as detailed
 315 in Section 3.3, we infer the computed curvature radius from the 2D image, and hence the numerical
 316 value of capillary pressure from Eq. (33). A sensitivity analysis of the numerical parameters of the
 317 SPH model, namely the size of the compact support h and the initial particle density, is also carried
 318 out. For the sake of calculation time, the interface has the same behavior whatever the dimension
 319 studied, the capillary tube measures 1mm wide by 10mm long. The capillary number is set so that
 320 $Ca \ll 1$. The evolution with time of relative error between analytical and numerical capillary pressure
 321 values is illustrated in Fig. 3b. For sufficient high radii of compact support over pore radius (to avoid
 322 wall effects), accuracy increases with increasing number of particles. Results indicate that the
 323 precision of the computed capillary pressure vapor concentration is numerically acceptable (relative
 324 error less than 4%) for at least 5 h along the pore radius and 3 particles per h (i.e., about 28 particles
 325 per compact support of radius h). We will respect these numerical constraints in further simulations.

326 4.2. Test case 2: Evaporation in nanocapillary slit without capillarity and Kelvin effect

327 After validation of the capillary pressure evaluation for two fluids in equilibrium between flat plates, in
 328 this section the evaporation process is investigated separately. In the first step, we neglect both the
 329 Kelvin effect and capillary forces. In the absence of capillary effects, the interface between fluids is
 330 flat, and material points are not subjected to any force and therefore remain immobile. The two-
 331 dimensional simulation geometry is displayed in Figure 4. As depicted, we consider the evaporation
 332 of liquid phase through a flat and quasi-static interface coupled with the diffusion of vapor within the
 333 gas phase. The drying front behavior can therefore be considered unidimensional and can be
 334 compared with the following analytical solution (based on [7], details can be found in Appendix A.1.),
 335 which assumes a sharp transition at the interface and bulk liquid phase in which the concentration
 336 gradients are negligible:

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337
$$d(t) = H \left(\sqrt{1 + 2 \frac{D}{H^2} \frac{C_s}{\rho_w} t} - 1 \right) \quad (34)$$

338 with $d(t) = z_1(0) - z_1(t)$ and $H = z_2 - z_1(0)$, where $z_1(t)$ is the position of the interface at time t and
 339 z_2 is the position of the boundary condition in concentration far from the liquid-gas interface. The
 340 evaporated mass and the vapor flux can be simply determined according to equation (34).

341 The simulation parameters are defined as follows: $C_s = 10 \text{ kg}\cdot\text{m}^{-3}$ is the saturated vapor concentration,
 342 $D = 1.25 \times 10^{-5} \text{ m}^2\cdot\text{s}^{-1}$ the coefficient of vapor diffusion in gas phase and $H = 10^{-3}\text{m}$ the distance
 343 between the interface $z_1(0)$ and z_2 , where the vapor concentration is set to zero. The fluids are each
 344 discretized into 600 particles.

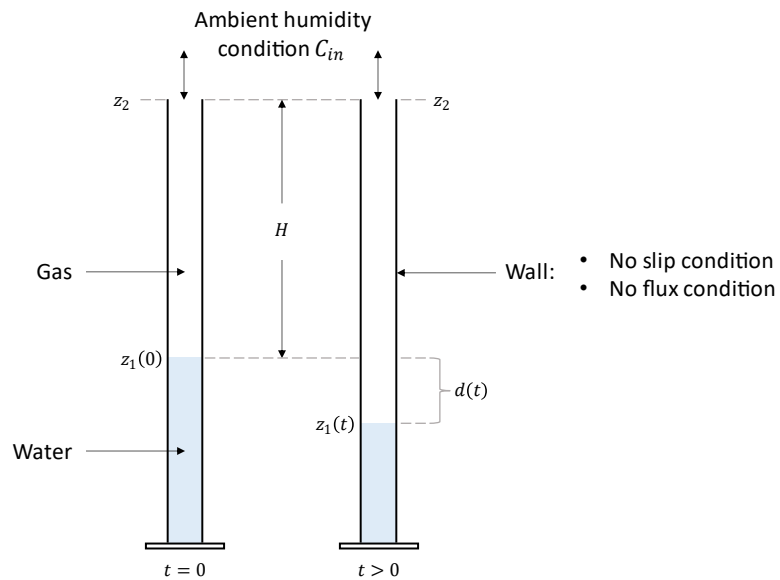


Figure 4: Geometry for simulation of evaporation between plates with quasi-stationary diffusion. The water level decreases very slowly due to evaporation and diffusion of water vapor in gas.

345 Figure 5 shows the relative error of the vapor mass evaporated at the interface. It is defined as the
 346 ratio between the total error of the vapor mass (i.e., the difference between the analytical and

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347 computed vapor mass at a given time at the liquid-gas interface) and the computed value. After some
 348 initial equilibration time, the error drops to values less than 1%. The relative error on the evaporation
 349 length $d(t)$ also tends toward the error on diffused mass. The total mass conservation is automatically
 350 preserved by SPH – which is a significant asset of this method – since the particles themselves carry
 351 the mass, however, the residual error observed here comes from the choice of the evaporation
 352 algorithm and the discrete nature (mass, location) of fluid particles. Indeed, the phase conversion
 353 criterion was set at 0.5 times the mass of a water particle. Uncertainty in mass conservation is thus
 354 of the order of 0.5 of water particle mass, generating oscillations around the exact solution, as
 355 observed in Figure 5b. Another remarkable feature of the SPH method is the non-sensitivity of this
 356 technique to point organization with respect to principal axes, as illustrated in Figure 5a. The same
 357 error is found regardless of the spatial orientation of the domain, even for very small numbers of
 358 particles at the interface.

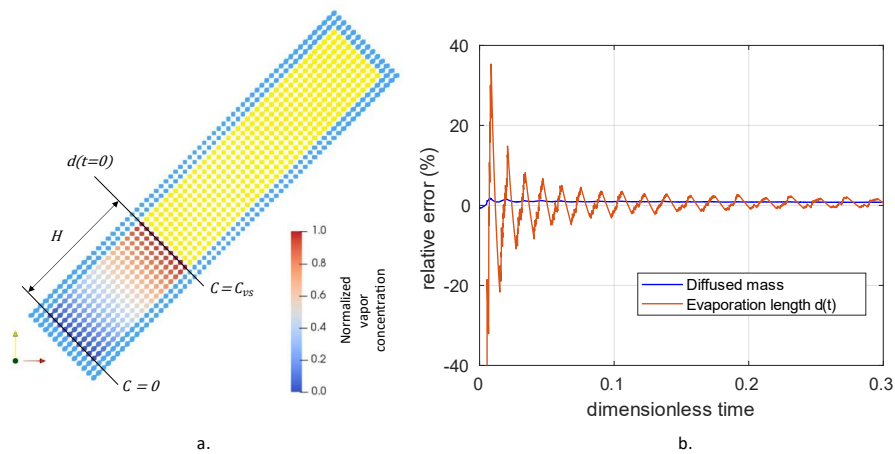


Figure 5: Verification of the SPH evaporation model without capillarity or Kelvin effect. a) simulation domain and dimensionless vapor concentration field. b) time variation of the relative error of evaporation length and vapor mass using the dimensionless time $t' = \frac{t v_{int}}{L_{domain}}$.

359 4.3. Test case 3: Evaporation in nanocapillary slit with capillary effect and Kelvin effect

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360 This test case is similar to the previous one and based on the same numerical parameters but we
 361 take into consideration capillary and Kelvin effects as well. The analytical solution is modified by
 362 replacing the saturated vapor concentration by the equilibrium vapor concentration (7) as follows:

$$363 \quad d(t) = H \left(\sqrt{1 + 2 \frac{D}{H^2} \frac{C_{eq}}{\rho_w} t} - 1 \right) \quad (35)$$

364 With parametrization chosen to reduce computational costs, the capillary pressure was too low for
 365 the Kelvin effect to be visible. Thus, the molar mass M in Eq. (8) has been artificially modified by a
 366 scaling factor of 3.25×10^8 to increase the Kelvin effect in this test case.

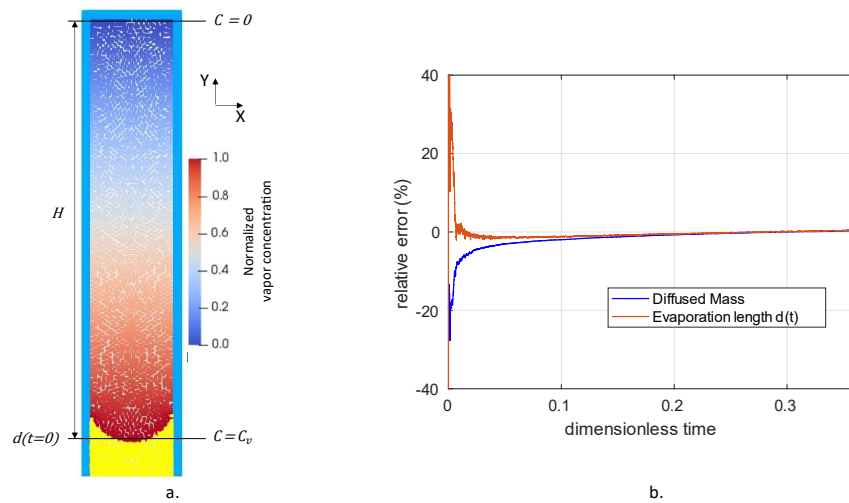


Figure 6: Verification of the SPH evaporation model with capillary and Kelvin effect. a) Geometry of the domain and dimensionless vapor concentration field. b) Relative error on the evaporation length function of dimensionless time $t' = \frac{t v_{int}}{L_{domain}}$.

367 To increase drying rate and to speed up simulations, the saturated vapor concentration is fixed at
 368 $C_s = 19.7 \times 10^{-2} \text{ kg.m}^{-3}$ so that the dimensionless equilibrium vapor concentration is then $C_{eq}/C_s =$

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369 0.88. For this test, 9000 fluid particles are set. The results obtained with this set of numerical
 370 parameters are presented in Figure 6. The observed behavior is similar to the one observed without
 371 the Kelvin effect: the relative error of evaporation length tends towards the relative error of the mass
 372 conservation at the interface, both are lower than 1%. As expected, the increase in number of particles
 373 contributes to reducing the numerical error. In addition, the capillary forces tend to promote uniform
 374 displacement of the drying front and reduce the discretization effect related to SPH since the interface
 375 is smoothed between each conversion of particles.

376 5. Application to nanometer-size pore networks

377 The geometry of the computational domain relies on idealized structures of connected pore networks
 378 due to the complexity of imaging clayrock pore spaces with narrow pores of a few nanometers. We
 379 will take advantage of this simplification to conduct a sensitivity analysis of physical parameters
 380 governing evaporation and condensation processes. Note that all the dimensionless numbers
 381 presented hereafter may vary locally since they are expressed at pore scale level. However, for the
 382 sake of simplicity, we only consider the averaged value of these dimensionless numbers at the
 383 network scale.

384 5.1. Evaporation patterns and regime diagram

385 In order to observe the impact of capillary and Kelvin effects on drying patterns, we focused first on
 386 2D heterogeneous arrays of narrow pores. A 3x2 pore network is used as a representative case for
 387 evaporation. Interfaces labelling algorithm can be found in Appendix A.3. The channel diameters are
 388 distributed between 5 and 10 nm (i.e., between $5h$ and $10h$ per radius, h being the compact support
 389 length) as presented in Figure 7. Working with this type of distribution allows us to study the drying of
 390 a network not accessible to gas drainage without fracturing the medium, i.e., typically for pore
 391 diameters less than 20nm [9], for which the Kelvin effects are significant. The network is discretized
 392 by 145000 particles, including 92000 fluid particles. For these simulations, density (ρ_w/ρ_g) and
 393 viscosity (μ_w/μ_g) ratios are fixed to 1. Periodic conditions are applied to the lateral sides of the
 394 domain. Gas is present at the domain top with a constant humidity condition. At the bottom boundary
 395 a no-flux condition is set. A series of simulations is carried out to study the evaporation pattern's

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396 dependence on capillary forces, diffusion and evaporation rates. This influence is evaluated through
 397 different values of the following dimensionless numbers: Pe , Ca and the vapor density ratio $\Delta C' =$
 398 $\frac{C_{eq} - C_{in}}{C_s}$ (equivalent to ε), with C_{in} the vapor concentration fixed in gas phase at the top boundary. All
 399 different cases with corresponding dimensionless parameter values used in the simulations are
 400 gathered in Table II. For some of them, the Kelvin effect was switched off and the saturated vapor
 401 concentration was used at all interfaces (cases *b.*, *e.*, *j.* and *l.*) The most representative desaturation
 402 patterns are illustrated in Figure 8 (corresponding to the cases highlighted in red in Table II).

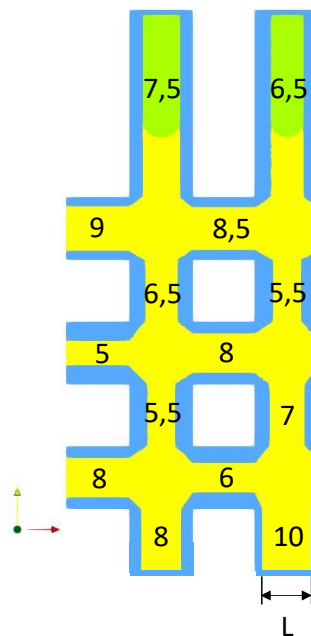


Figure 7: Initial geometry and phase distribution in the model network. The aperture is expressed in terms of compact support length h . yellow zone represents the water phase, and green ones the gas phase. Both fluid phases are surrounded by solid, rigid phase, in blue. Pores are connected laterally through periodic conditions.

403

	ϵ	Ca_w	Pe	$\Delta C'$	C'_{in}	Kelvin effect
in-situ	1.5×10^{-4}	5.5×10^{-10}	3.3×10^{-9}	4.0×10^{-1}	0.6 - 0.98	Yes
a.	1.4×10^{-3}	1.1×10^{-5}	1.7×10^{-4}	8.8×10^{-1}	0.00	Yes
b.	1.6×10^{-3}	1.1×10^{-5}	1.7×10^{-4}	8.8×10^{-1}	0.00	No
c.	1.9×10^{-3}	2.5×10^{-5}	4.1×10^{-4}	1.2×10^{-1}	0.76	Yes
d.	1.4×10^{-2}	1.1×10^{-4}	1.7×10^{-3}	8.8×10^{-1}	0.00	Yes
e.	1.6×10^{-2}	1.1×10^{-4}	1.7×10^{-3}	8.8×10^{-1}	0.00	No
f.	1.9×10^{-2}	2.5×10^{-4}	4.1×10^{-3}	1.2×10^{-1}	0.76	Yes
g.	4.5×10^{-2}	4.2×10^{-4}	6.8×10^{-3}	2.8×10^{-1}	0.70	Yes
h.	6.2×10^{-2}	8.2×10^{-4}	4.1×10^{-3}	1.2×10^{-1}	0.76	Yes
i.	1.2×10^{-1}	1.6×10^{-3}	8.2×10^{-3}	1.2×10^{-1}	0.76	Yes
j.	1.4×10^{-1}	1.1×10^{-3}	1.7×10^{-2}	8.8×10^{-1}	0.00	Yes
k.	1.6×10^{-1}	1.1×10^{-3}	1.7×10^{-2}	8.8×10^{-1}	0.00	No
l.	4.4×10^{-1}	3.4×10^{-3}	1.7×10^{-2}	8.8×10^{-1}	0.00	Yes
m.	5.0×10^{-1}	3.4×10^{-3}	1.7×10^{-2}	8.8×10^{-1}	0.00	No
n.	1.6×10^0	1.1×10^{-2}	1.7×10^{-3}	1.0×10^0	0.00	Yes

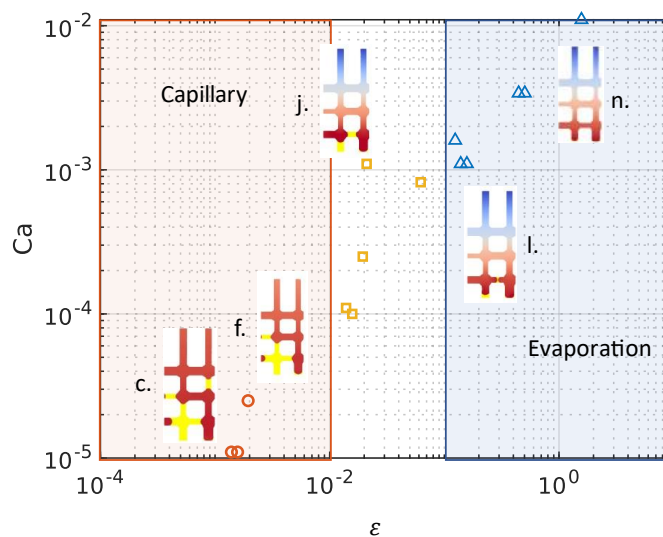
Table II: Dimensionless parametrization for studied cases sorted by increasing ϵ . The cases colored in red correspond to patterns illustrated in Figure 9. For the sake of comparison, the expected in situ conditions for COx are also given.

404 A regime diagram $Ca - \epsilon$ is illustrated in Figure 8 and confirms the role of ϵ in delineating the drying
 405 patterns. Note that each of the dimensionless parameters has varied by several orders of magnitude
 406 to demonstrate the unique dependency on the evaporation-capillary number at this scale (see Table
 407 II). For the sake of comparison, the ϵ value for the representative in situ conditions in COx formation
 408 (based on data from [3,9]) is also indicated in Table II. It is quite remarkable to observe that, in spite
 409 of drastically different values for Ca and Pe , the ϵ value for in situ conditions is quite similar to the
 410 range of values explored in our study (10^{-4} against 10^{-3} for the lowest value simulated numerically),

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411 and hence, the expected evaporation pattern (corresponding to the capillary dominated regime) can
 412 be inferred from these simple simulations. Similar reasoning holds for the impact of parameter
 413 variations. For instance, reducing the contact angle will increase the capillary pressure and the
 414 meniscus curvature at the interface. From Eq. (8), it will decrease the equilibrium vapor concentration
 415 C_{eq} and slow down the local evaporation rate by exacerbating the Kelvin effect. As a consequence, it
 416 will enhance front instability and so a transition towards capillary dominated regime (lower ϵ).



417

Figure 8: Drying regimes diagram as a function of capillary-evaporation number for evaporation simulations with capillary and/or Kelvin effects.

418 As depicted in Figure 8 and highlighted in Figure 9 with the two most extreme cases, two
 419 representative regimes are revealed: the capillary-dominated regime (e.g. case *g.* with a high ambient
 420 humidity condition) and the evaporation-dominated regime (e.g. case *n.*). The temporal evolution of
 421 water desaturation for the two most extreme cases, representative of evaporation and capillary
 422 regimes exhibits strong heterogeneity in the capillary-dominated regime while demonstrating a
 423 homogeneous desaturation front for the evaporation regime. Of course, boundaries shown in Figure

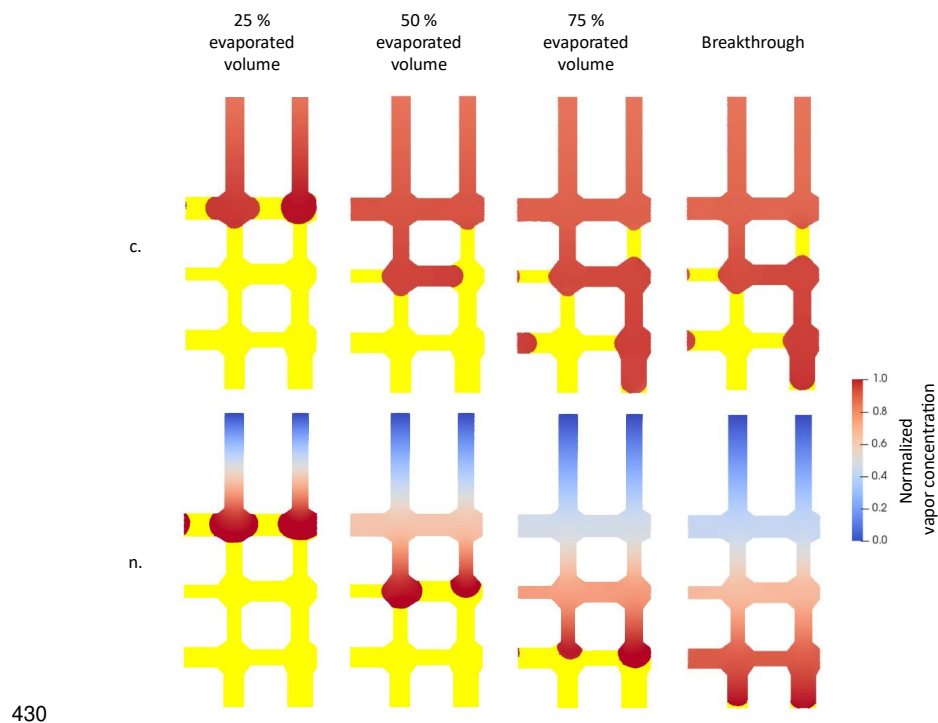
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424 8 have been drawn between the different regimes based on a qualitative observation of the
 425 evaporation structures and some uncertainties may be associated with the transition lines.

426 The concentration field will be crucial as it will significantly accentuate the presence of heterogeneities
 427 in the patterns, especially when surpassing the local vapor equilibrium conditions at the interfaces.

428 The evaporation rate is also critical as it will determine whether or not liquid redistribution occurs
 429 within the network.



430

Figure 9: Evolution with time of vapor concentration fields and fluid distribution patterns for the test cases c) and n). The comparison is made at equivalent evaporated volumes and on a normalized vapor concentration scale. The liquid phase is represented in yellow.

431 The capillary-dominated drying regime corresponds to conditions of very low ε ($\varepsilon < 1 \times 10^{-2}$).

432 Capillary forces are high enough to prevent evaporation in the smallest pores, which remain saturated.

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433 The equilibrium vapor concentration at the liquid-gas meniscus in such pores is lower than the vapor
434 concentration in the surrounding gas, and vapor cannot be diffused away from the meniscus. This
435 results in the formation of preferential evaporation pathways (Figure 9c). This phenomenon is
436 accentuated by the Kelvin effect. A similar situation takes place with increased inlet vapor
437 concentration and hence, reduced evaporation rate. The higher the ambient humidity conditions, the
438 fewer pores will have the ability to empty and the more heterogeneous the drying pattern will be
439 (Figure 9c). At the macroscale, the residual water saturation is higher (Figure 10). It may also facilitate
440 the formation of disconnected water clusters if the pore size distribution is large enough.

441 In contrast, for high values of ε ($\varepsilon > 1 \times 10^{-1}$), evaporation rate and viscous forces have taken
442 advantage over capillary forces. All the pores in contact with the gas front evaporate at the same time.
443 A uniform drying pattern is observed with practically no residual water saturation (Figure 9n, 10). This
444 is an evaporation-dominated regime. The impact of the Kelvin effect is negligible at low ambient
445 humidity, with the drying front being uniform (Figure 9.n).

446 Between these two values ($1 \times 10^{-2} > \varepsilon > 1 \times 10^{-1}$), the gas invasion pattern becomes transient
447 between capillary-dominated and evaporation-dominated. In this intermediate regime, both capillary
448 forces and the evaporation rate are competing. Small desaturation front inhomogeneities may appear,
449 but they do not propagate very far (Figure 8.j), as we can also see later (Figure 11).

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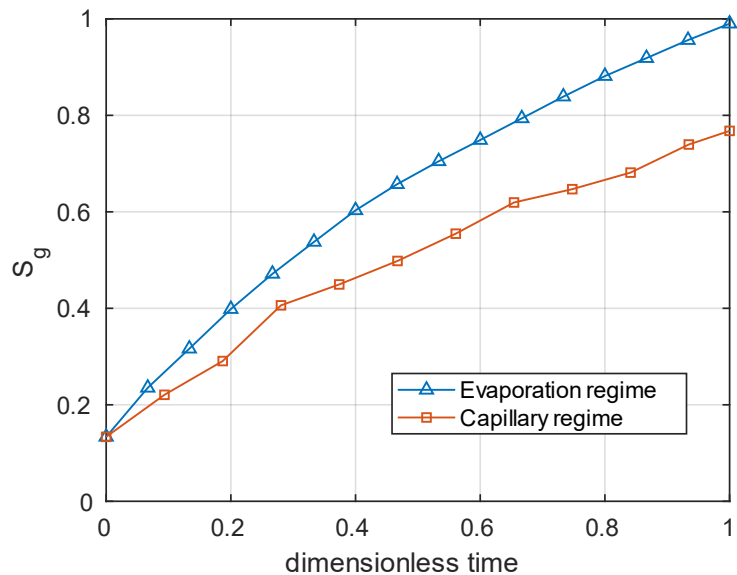


Figure 10: Evolution of gas saturation with dimensionless time for capillary-dominated (case c.) and evaporation-dominated (case n.) regimes.

450 This discrepancy between these two contrasted drying regimes is also visible in the drying dynamics.
 451 As illustrated in Figure 10, the evolution of gas saturation S_g with dimensionless time changes
 452 drastically from the evaporation to the capillary-driven regime. For the first one, gas saturations
 453 increases like a 1D analytical solution ($\sim\sqrt{Dt}$) with time and slows down only close to breakthrough
 454 time due to mass transfer limitations [7]. In contrast, in the capillary-driven regime, gas saturation at
 455 breakthrough is significantly lower (75% against 100%) due to the formation of preferential pathways
 456 for drying and the presence of residual water clusters. The heterogeneity of pore size distribution in
 457 the medium, combined with the low value of capillary number and the Kelvin effect, results in the
 458 strong variability of the equilibrium vapor concentration at different gas-liquid menisci along the drying
 459 front. It thus induces variations in drying rates with time, as shown in Figure 10.

460 5.2. Kelvin effect on gas invasion pattern

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461 In addition to the previous test cases summarized in Table I, we performed supplementary simulations
462 on one larger pore network in order to investigate further the impact of Kelvin effect and to determine
463 to what extent it may affect gas invasion patterns and to avoid possible boundary effects. These
464 simulations were carried out with or without Kelvin effect on a 5x5 heterogeneous network with mean
465 pore radius of 7.78 nm and a standard deviation of 1.64 nm (corresponding to a range of pore sizes
466 from 5 to 10 nm) under the same conditions that were presented for cases j. and k. in Section 5.1.
467 We set the density and viscosity ratio to one, the capillary number is around 10^{-3} and the Péclet
468 number is about 10^{-2} , with a constant vapor concentration imposed at the inlet, corresponding to
469 $C'_{in} = 0.75$. Such conditions lead to an evaporation-capillary number equal to $\varepsilon \approx 1.4 \times 10^{-1}$ and $\varepsilon \approx$
470 1.6×10^{-1} for the simulations with and without the Kelvin effect, respectively. Based on these values,
471 we expect a capillary-dominated regime, more pronounced with the Kelvin effect. In addition, Kelvin
472 effect induces a significant decrease in equilibrium vapor concentration, which varies over the range
473 of pore sizes from $0.77C_s$ to $0.88C_s$ at different menisci.

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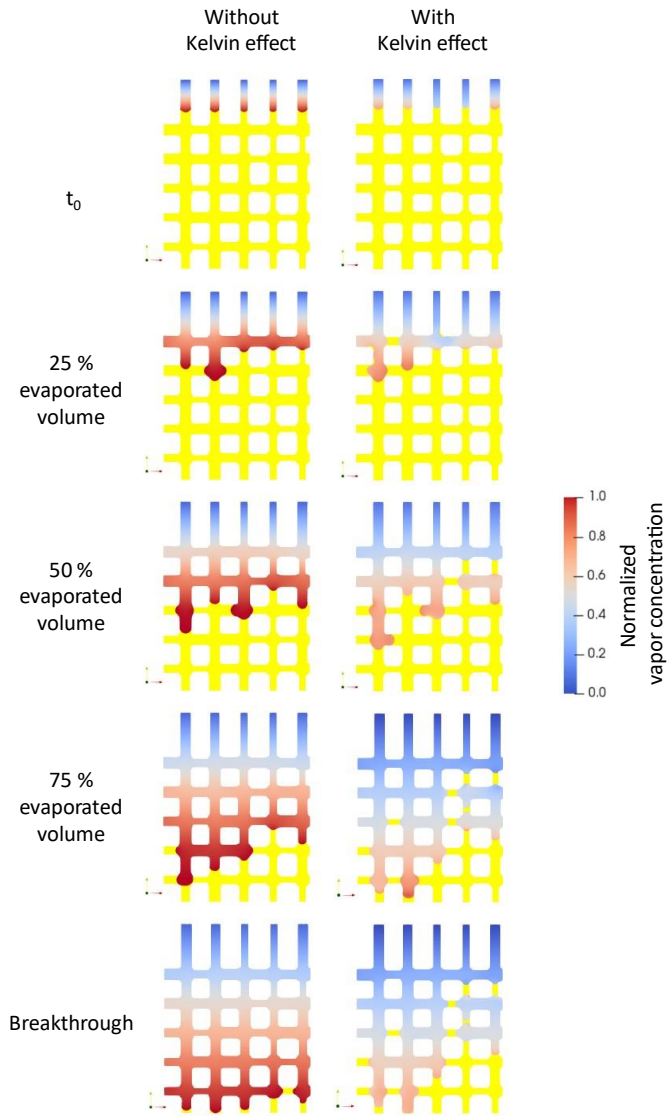


Figure 11: 5x5 network. Comparison of evaporation fronts without (left) and with Kelvin effect (right) at two different equivalent evaporated volumes and on a normalized vapor concentration scale. The water phase is represented in yellow. Periodic conditions are applied to side domain boundaries. Gas invasion is made from the top with $C'_{in} = 0.75$. The domain is closed at the bottom.

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474 In order to highlight the Kelvin effect's impact on drying patterns, Figure 11 compares, at equivalent
 475 gas saturation, the fluids' distributions within the pore space in the presence (right) or absence (left)
 476 of the Kelvin effect. The network is obviously less saturated with water vapor from the initial time. It
 477 generates competition between channels with variable drying front velocities from one pore to
 478 another, leading to complex fluid redistribution. As expected, front inhomogeneities appear to be more
 479 important with the Kelvin effect, but they remain limited due to the small size of the domain. From
 480 25% evaporation, the Kelvin effect modifies the drying pattern by closing the smallest pores, due to
 481 local vapor concentration conditions. The most advanced front is located in a different pore. A pore
 482 channel that is dried slower may catch up the head of the front at a later stage (e.g., between 50%
 483 and 75% for the cases presented in Figure 11), and a quasi-uniform gas front can even be recovered
 484 when the breakthrough is occurring. This last phenomenon is largely accentuated by the absence of
 485 the Kelvin effect. In the presence of the Kelvin effect, the front is much less uniform. Between 50%
 486 and 75% evaporation, we can have up to three channels of difference in drying, or half of the network.
 487 Also, many channels remain filled with water upstream of the network. As on the smaller networks,
 488 the Kelvin effect with high ambient humidity significantly accentuates heterogeneities, with the
 489 appearance of disconnected clusters of the liquid phase (Figure 11), so that breakthrough occurs at
 490 78.6% of gas saturation compared to 97.8% without the Kelvin effect.

491 Another remarkable finding, not highlighted in previous studies, is the impact of condensation on the
 492 gas invasion pattern, made possible by Kelvin effect. Due to possibility for equilibrium vapor
 493 concentration at the meniscus will become lower than the ambient vapor concentration flowing
 494 through the pore space, residual water clusters trapped behind the front may promote condensation.
 495 We have illustrated this mechanism in Figure 12 for test case h. where we have represented at
 496 different times the mass transported by liquid particles close to the interface in the transition band (a
 497 negative value implies vapor loss and so, water condensation) and the relative humidity within the
 498 gas phase (the color scale ranges between the relative humidity at equilibrium and the highest value
 499 in the gas phase). In the presence of Kelvin effect, capillary forces induced by the throat size of 5.5
 500 nm reduce equilibrium relative humidity to 0.79. In addition, the vicinity of the drying front in the lower

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501 part favors high ambient vapor concentrations in the gas phase (Figure 12, time t_1). This results in a
 502 displacement of vapor from higher (gas phase) to lower (gas-liquid interface) concentrations, and
 503 hence, condensation occurs (Figure 12, time t_2). The liquid cluster expands, but in the upward
 504 direction, because of capillary forces that force water to move into the narrowest pore (Figure 12, time
 505 t_3). This mechanism can be quite fast, with local condensation rates much higher than the average
 506 drying rate. The velocity v at which the interface moves to fill the pore by condensation is of the same
 507 order as the velocity v_{int} at which the drying front moves in the system such that $v/v_{int} \sim 1$. It could
 508 contribute to reducing the vapor concentration at the front head, and hence, increasing the vapor
 509 gradient, and speed up the evaporation breakthrough.

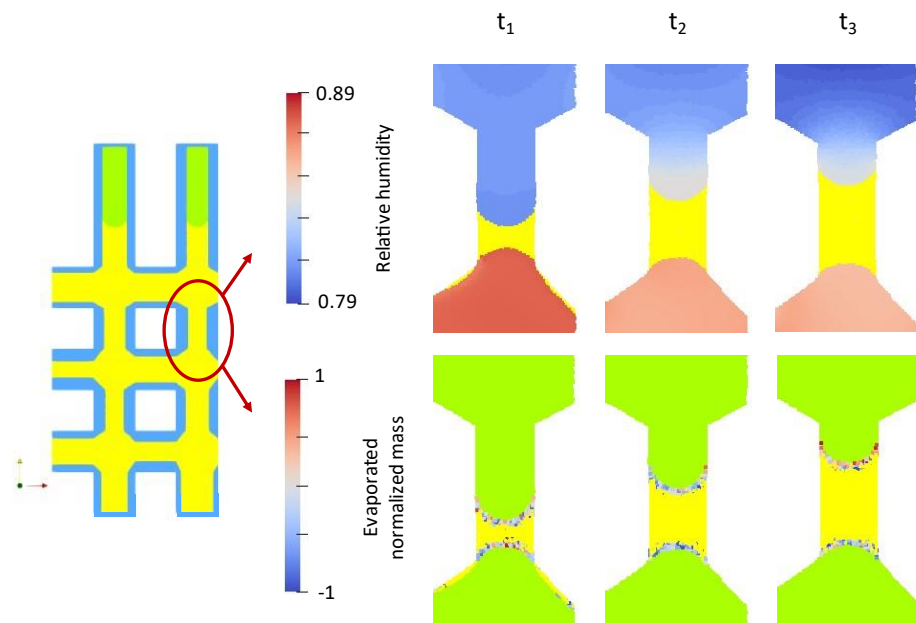


Figure 12: Evidence of the filling of the smallest pores by condensation at different times. Top: Concentration fields of dimensionless vapor concentration (relative humidity) in the gas phase. Bottom: The water phase is in yellow. The color field shows the local mass balance per liquid particle in the transition band before conversion. A positive balance leads to evaporation. A negative balance leads to condensation.

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510 Finally, as expected, these differences in evaporation patterns also affect the dynamics of drying. The
 511 evolution of gas saturation with dimensionless time, illustrated in Figure 13, shows a similar trend for
 512 both curves but with a lower gas saturation to breakthrough in the presence of the Kelvin effect. Note
 513 that the dimensionless time is here defined for both simulations using the front velocity v_{int} without
 514 the Kelvin effect. The impact of mass transfer limitations is more pronounced than in Section 5.1 due
 515 to the larger pore network size, but no fluctuation of front velocity occurs, probably because the
 516 heterogeneity of the pore size distribution is not large enough. The drying rate is also reduced
 517 because equilibrium vapor concentrations are smaller than the saturated vapor concentrations, and
 518 in spite of preferential pathways. This is consistent with the experimental results of Thiery et al. [45].
 519 Note that PNM simulations by Maalal *et al.* [32] predict the opposite result of the Kelvin effect on time
 520 to breakthrough, probably because the impact of pattern instabilities prevails. This competition, driven
 521 by the Kelvin effect between the reduction of local equilibrium vapor concentration and the
 522 development of preferential pathways, will require further investigation.

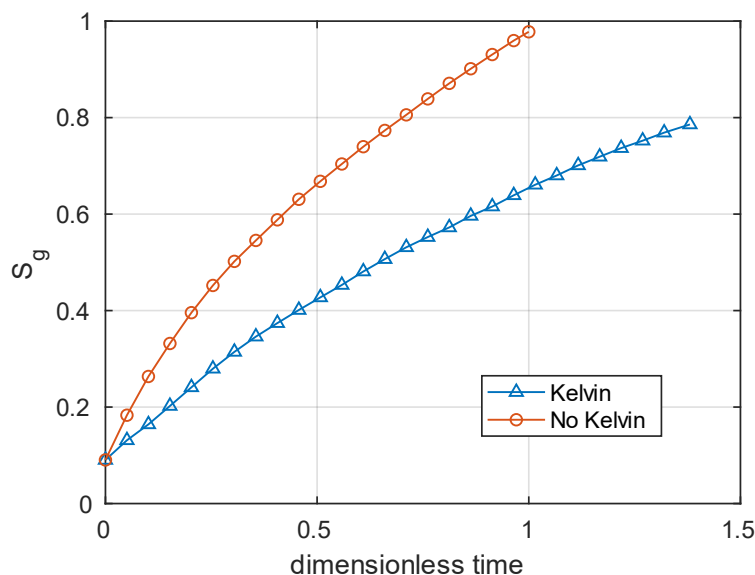


Figure 13: Evolution of gas saturation with dimensionless time with and without the Kelvin effect.

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523 6. Conclusion

524 The desaturation process in nanoporous rocks can be considerably affected by liquid evaporation,
525 especially when the smallest pores cannot be dewatered due to insufficient gas pressure to overcome
526 capillary barriers. This mechanism is usually neglected or oversimplified in models investigating gas
527 drainage. Consequently, in this article, we built an evaporation model to predict gas dynamics at pore
528 scale. All key mechanisms are considered, including mass transport of vapor in gas phase, capillary
529 forces, and the Kelvin effect. The present work also takes into account fluids and solid properties, and
530 ambient humidity in the evaporation process.

531 We have used a SPH code to enhance multiphase modeling. Accurate calculation of capillary
532 pressures at interfaces allowed us to correctly estimate liquid redistribution in the porous medium and
533 local equilibrium vapor concentration at curved menisci according to Kelvin equation. We were able
534 to estimate the minimum size of the compact support and particle density required to obtain stable
535 and accurate results (relative errors of less than 1%).

536 We were able to demonstrate the ability of our continuous SPH model to simulate evaporation-
537 condensation phenomena driven by Kelvin effect and vapor diffusion through gas phase. This model
538 has been validated using analytical solutions. Drying simulations of small pore networks allowed us
539 to highlight two desaturation regimes separated by an intermediate regime for ε parameter between
540 10^{-3} and 1. Kelvin effect has been shown to drastically influence both gas distribution patterns and
541 drying dynamics within the capillary-dominated regime. A comparative analysis of our results and
542 those from the literature revealed that Kelvin condition induces contrasted behavior with a reduction
543 of equilibrium vapor concentration and the development of preferential gas pathways. They may affect
544 gas dynamics in opposite ways and result in increasing or decreasing time to breakthrough. The
545 condensation phenomenon has also been observed in the vicinity of drying front and, depending on
546 the local vapor saturation conditions, may slow down or block gas invasion into smallest pores. In
547 some cases, pores may even refilled with water.

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548 As a final word, we have highlighted in this paper the importance of the Kelvin effect on the formation
 549 of gas percolation channels, particularly in high-humidity conditions. These findings align with existing
 550 literature, encompassing both numerical and experimental studies. They underscore the significance
 551 of considering nanoscopic phenomena, such as the Kelvin effect, when upscaled studies are
 552 conducted. In the future, we would like to couple evaporation to drainage flow and to consider hydro-
 553 mechanical coupling that may promote creation of dilatant pore pathways and thus gas migration
 554 [14,39]. Improving description of evaporation and capillary condensation processes into the smallest
 555 pores when the Kelvin equation fails by bridging the gap between molecular methods and continuous
 556 methods is also an avenue for future work.

557

558 **Appendices**

559 A. Analytical solution of evaporation with quasi-steady-state diffusion

560 In order to find the 1D analytical solution for the problem in Figure 4, we define the diffusive flux
 561 as:

$$562 \quad \varphi_w = -D_v \nabla C \cdot \mathbf{n}_s \quad (36)$$

563 With $\frac{\partial C}{\partial x} = \frac{\partial C}{\partial y} = 0$ and D_v the diffusion of vapor in gas. At the water/gas interface, at $z = z_1$, equation
 564 (36) can be written as:

$$565 \quad \varphi_w|_{z=z_1} = -D_v \left. \frac{\partial C}{\partial z} \right|_{z=z_1} = \frac{D_v}{z_2 - z_1(t)} (\rho_{eq} - \rho_{in}) \quad (37)$$

566 Considering a very slow liquid retreat, we use the quasi-steady state method:

$$567 \quad -\rho_w \frac{dz_1}{dt} = \frac{D}{z_2 - z_1(t)} (\rho_{eq} - \rho_{in}) \quad (38)$$

568 so that we have the following equation:

569
$$(z_2 - z_1(t))dz_1 = \frac{D}{\rho_w} \rho_{eq} dt \quad (39)$$

570 We use $d(t) = z_1(0) - z_1(t)$ and $H = z_2 - z_1(0)$ to integrate equation (39) as:

571
$$\int_0^d (H + d) dd = \frac{D}{\rho_w} \rho_{eq} \int_0^t dt \quad (40)$$

572 Therefore :

573
$$\frac{1}{2}(H + d)^2 - \frac{1}{2}H^2 = \frac{D}{\rho_w} \rho_{eq} t \quad (41)$$

574 Finally, the analytical solution for the interface displacement is written as follows:

575
$$d(t) = H \left(\sqrt{1 + \frac{D \rho_{eq}}{H^2 \rho_w} t} - 1 \right) \quad (42)$$

576 B. Evaporation-capillary number definition

577 Considering only diffusion, flux at liquid-gas interface can be written as:

578
$$\varphi_w = -D_v \nabla C \cdot \mathbf{n}_s \quad (43)$$

579 By using quasi-steady-state assumption, we can write from (38) the dimensionless variation of the
580 position due to evaporation as:

581
$$\frac{dz_1'}{dt'} = -\frac{D_v}{v_0 L} \frac{C_{eq} - C_{in}}{C_s} \frac{C_s}{\rho_w} \nabla C' = -\frac{1}{Pe} \Delta C C_s' \nabla C' \quad (44)$$

582 The dimensionless Navier-Stokes equation can be written as:

583
$$Re \frac{D\mathbf{v}'}{Dt} = -\frac{1}{Ca} \nabla p' + \Delta \mathbf{v}' \quad (45)$$

584 By solving this equation with Washburn assumptions [49], we can write the dimensionless variation
585 of the position due to capillary effects as:

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586
$$\frac{dz_1'}{dt'} = -\frac{\nabla p'}{12Ca} r'^2 \quad (46)$$

587 From equation (37) and (39) we can assess the characteristic time of imbibition and evaporation. By
 588 dividing the first by the second, we obtain the following equation:

589
$$\frac{\tau_{imbib}}{\tau_{evap}} = 12 \frac{Ca}{Pe} \frac{C_{eq} - C_{in}}{C_s} \frac{C_s}{\rho_w} \frac{\partial C'}{r' \partial p'} \quad (47)$$

590 Here we can recognize the dimensionless evaporation-capillary number.

591 C. Interface particle labelling

592 Evaporation in COx clayey rock is influenced by nanoscopic effects. In order to take these effects into
 593 account, the Kelvin equation has been implemented in the SPH method. To remain consistent with
 594 the assumption of the surface tension independent of the distance to the solid wall and to damp any
 595 non-physical local fluctuations, the capillary pressure is averaged over each liquid-gas interface. To
 596 be able to determine the mean capillary pressure per interface, we must be able to discriminate the
 597 particles according to the interface to which they “belong”. Figure 14 presents the overall concept of
 598 the algorithm performing this task.

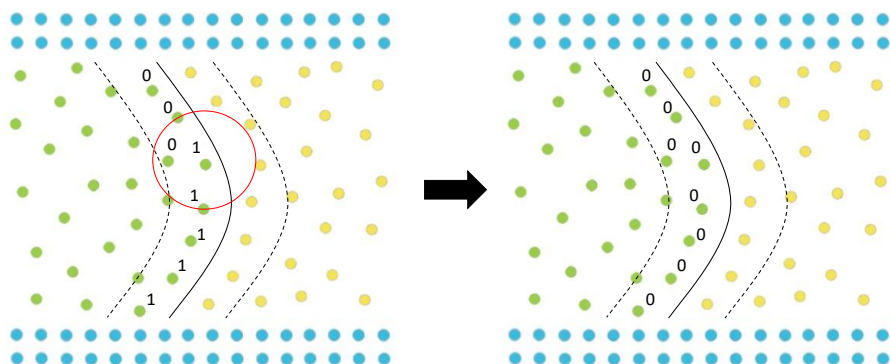


Figure 14: Labelling steps of interfaces particles when two labels are on the same compact support.

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599 The principle is the following: we loop over all the particles belonging to a transition band, assigning
600 them a label. During this loop, two cases can happen:

601 ➤ The particle had not yet been labeled; in which case it was given a new label ($N+1$, N being
602 the highest existing label).

603 ➤ The particle has already been labeled (label M); nothing happens.

604 Each time a particle is labeled, particles on its compact support are checked:

605 ➤ The particle had not yet been labeled; in which case it is given same label as the central
606 particle (M or $N+1$)

607 ➤ The particle has already been labeled (label K); the particle having the highest label of the two
608 turns into the smallest label, as shown figure 14.

609 This algorithm leads to distinguished interfaces if they are separated by a distance bigger than h .

610 The characteristic time of evaporation must be greater than the characteristic time of establishment
611 of the interface in order not to degrade the calculus of capillary pressure. If this condition is fulfilled,
612 the capillary effects will allow smoothing of the interface.

613 **Acknowledgments**

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615 grant agreement N°847593 (EURAD) and from NEEDS programme (MECHE).

616

617 **Data Availability Statement**

618 The data that support the findings of this study are available from the corresponding author upon
619 reasonable request.

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