

On the road to Kubo > 1:

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On the road to Kubo > 1: Quasi-linear theory in 1D plasma

Alejandro Guillevic

M. Lesur, X. Garbet, A. Ghizzo, E. Gravier, G. Lo-Cascio, T. Réveillé, D. Mandal, and open to contributions July 7, 2022 In a nutshell:

Diffusion scales as $E^{3/2}$ at high amplitude turbulence

- Charged particles in an turbulent *E* field
 - > Diffusion in v: $\dot{v} = E$
- At small $E: D \propto E^2$
- For larger Kubo and longer time scales -



Context Turbulence in nature

• Rapid fluctuation of physical parameters



[Lecture, Yale univ., 2014]

> In plasmas:



[F. Califano, Frontiers, 2020]





Context

Collision-less 1D Plasma turbulence

 \mathcal{V}

- Geometry:
 - Dynamics happen in 1D
 - > Periodic limits
- In a 1D plasma
 - \succ Diffusion in velocity \boldsymbol{v}
 - \rightarrow Plasma heating
 - \rightarrow Instability triggering
- Types of 1D turbulence:
 - > Ion-acoustic
 - > Langmuir
 - $\succ \omega = C^{onst}$ (Artificial)

[F. Doveil & D. Gresillon, PoF, 1982]







Analytical model 1D random motion of charged particles



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Analytical model

Quasi-linear diffusion: Particles dynamics

[A. Vedenov et al., 1962]



Analytical model Quasi-linear diffusion $K \ll 1$

$$D_{0}(v) = \frac{q^{2}}{m^{2}} \int_{0}^{+\infty} \int_{-\infty}^{+\infty} dt \, dx \, \delta(x - vt) \langle E(0,0)E(x,t) \rangle$$
• Prescribe homogeneous steady
state turbulence
 \rightarrow Sin waves with random initial
phases

$$D_{0}(v) = \frac{q^{2}}{m^{2}} \int_{0}^{+\infty} dt \sum_{k} \frac{\hat{E}^{2}}{2} \cos[(kv - \omega)t]$$

For a prescribed turbulent E field





Numerical simulations Statistics: Quasi-linear regime

- Quasi-linear regime: First diffusion
 - Th. & simulation agreement
 - *K* < 0.01



Analytical model Limits on Quasi-linear theory: Resonance broadening







Analytical model

Resonance broadening

[T. H. Dupree, PoF, 1966] [J. Weinstock, PoF, 1968]

- **D** : Iterative method
 - > Distribution of particles around v

$$D_{0}(v) = \frac{q^{2}}{m^{2}} \int_{0}^{+\infty} \int_{-\infty}^{+\infty} dt \, dx \, \delta(x - vt) \langle E(0,0)E(x,t) \rangle$$

$$\delta(x - vt) \rightarrow Ae^{\frac{(x - vt)^{2}}{2\sigma_{x,n-1}^{2}}}$$

$$D_{n}^{RB}(v) = \frac{q^{2}}{m^{2}} \int_{0}^{+\infty} dt \sum_{k} \frac{\hat{E}^{2}}{2} e^{-\frac{\sigma_{x,n-1}^{2}k^{2}}{2}} \cos[(kv + \omega)t]$$

$$D_n^{RB}(v) \xrightarrow[n \to +\infty]{} D^{RB}(v)$$





Numerical simulations Intermediate Kubo number



- Th. & Simulation Diff. agreement
- RB effets: *K* few precents
- D flattens K ↗

- Problems :
 - Discrepancy at large and small v

Analytical model Limits on resonance broadening



D = f(K) ?





Numerical simulations Large Kubo number

- Study at fixed K
- QL & RB fails for large K
 Large v
- RB Th: Order of magnitude
- *D* converges ∀*K* Finite periodic system







Numerical simulations Remark: Two diffusions

• First diffusion regime:









Numerical simulations First and second diffusion

- Study at fixed *v*
- *D* evolves as a power Kubo: $K^{\beta} = E^{\beta/2}$



Future prospects **1D Plasma turbulence and transport**

- PS structures generated by turbulence
 - Modify turbulence
 - → Non-linear effect
 - \rightarrow Transport & diffusion

Structures need to be taken

into account



Position x [M. Lesur, P. H. Diamond, PPCF, 2014]





V_i

 V_2

 V_1

Future prospects Conclusion

- We verified that QL and RB predict diffusion for small *K*, for realistic dispersion relation and spectrum.
- We observed the limits on RB for :
 - High and low velocities
 - High Kubo number
- We observed two diffusions at different time scales, where

diffusion evolves as a power of Kubo number:

$$\succ \beta = 3, \qquad \frac{5}{2}, \qquad \frac{3}{2}$$



